
oapackage Documentation

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The Orthogonal Array package contains functionality to generate and analyse orthogonal arrays, optimal designs and conference designs.

INTRODUCTION

Orthogonal arrays, optimal designs and conference designs are important tools for the design of experiments [EN95] [HSS99] [WH09]. The Orthogonal Array package contains functionality to generate and analyse these types of designs. To generate the arrays and designs, the package uses the exhaustive enumeration algorithm of [SEN10] and the optimization algorithm of [ES17]. To analyze the arrays and designs, the package includes a wide variety of relevant statistical and combinatorial criteria. A large collection of orthogonal arrays, optimal designs and conference designs generated with the package are available in the Orthogonal Array package website [Een18].

1.1 Example usage

The Orthogonal Array package can be used to generate and manipulate arrays and designs. Additionally, it can calculate some of their statistical properties. The following example shows how to generate an orthogonal array with 8 runs and 2 factors, and calculate three relevant statistical properties:

Calculate D-efficiency

```
>>> import oapackage
>>> array=oapackage.exampleArray(0) # define an orthogonal array
>>> array.showarray()
array:
 0  0
 0  0
 0  1
 0  1
 1  0
 1  0
 1  1
 1  1
>>> D = array.Defficiency() # calculate the D-efficiency for estimating the interaction
                           # effects model
>>> array_rank = array.rank() # calculate the rank of the design
>>> print('D-efficiency %f, rank %d' % (D, array_rank) )
D-efficiency 1.000000, rank 2
>>> gwlp = array.GWLP() # calculate the generalized word length pattern
>>> print('Generalized wordlength pattern: %s' % (gwlp,) )
Generalized wordlength pattern: (1.0, 0.0, 0.0)
```

The statistical properties of the arrays and designs are introduced in *Properties of designs*.

1.2 Interfaces

The Orthogonal Array package has interfaces in C++ and Python for generating, manipulating and analyzing all the types of arrays and designs. In this documentation, you will find references to both the Python and the C++ interface. The package also includes several command line tools.

For the generation of optimal designs [ES17], the Orthogonal Array package has also a Matlab interface; see the documentation [README.Matlab.md](#).

1.3 License

The code is available under a BSD style license; see the file [LICENSE](#) for details. If you use this code or any of the results, please cite this program as follows:

- OApackage: A Python package for generation and analysis of orthogonal arrays, optimal designs and conference designs, P.T. Eendebak, A.R. Vazquez, Journal of Open Source Software, 2019
- *Complete Enumeration of Pure-Level and Mixed-Level Orthogonal Arrays*, E.D. Schoen, P.T. Eendebak, M.V.M. Nguyen, Volume 18, Issue 2, pages 123-140, 2010.

1.4 Acknowledgements

The code and ideas for this package have been contributed by Eric Schoen, Ruben Snepvangers, Vincent Brouerius van Nidek, Alan Roberto Vazquez and Pieter Thijss Eendebak.

1.5 Installation

The packge is continously tested on Linux and Windows. The Python interface is available from the [Python Package Index](#). The package can be installed from the command line using pip:

```
$ pip install OApackage
```

The source code for the package is available on <https://github.com/eendebakpt/oapackage>. The command line tools use a cmake build system. From the command line, type the following:

```
$ mkdir -p build  
$ cd build  
$ cmake ..  
$ make  
$ make install
```

This creates the command line utilities and a C++ library.

To compile the Python interface use

```
$ python setup.py build  
$ python setup.py install --user
```

The Python interface requires Numpy [[TheScipycommunity12](#)], Matplotlib [[Hun07](#)] and Swig. The code has been tested with Python 3.6, 3.7 and 3.8.

The R interface to the optimal design functionality of the package is available from [CRAN](#). For the Matlab and Octave interface to the optimal design functionality see the file README.Matlab.md.

1.6 Related sites of orthogonal arrays

There are several related sites available online which include collections of orthogonal arrays. For instance, the website of Neil Sloane [[Slo14](#)], the website of Hongquan Xu [[Xu18](#)], the SAS website managed by Warren Kuhfeld [[Kuh18](#)], and the R package _DoE.base_ [[GAX18](#)] include lists and surveys of attractive orthogonal arrays gathered from different sources.

EXAMPLE NOTEBOOKS

This section contains several examples for generating, manipulating and analyzing arrays and designs using the Orthogonal Arrays package. The examples are shown using Jupyter notebooks, which can be found on github <https://github.com/eendebakpt/oapackage/tree/master/docs/examples>.

2.1 Example script for Python interface to Orthogonal Array package

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```
[1]: import numpy as np
import oapackage

print("oapackage version: %s" % oapackage.version())
oapackage version: 2.6.0
```

Load an example array.

```
[2]: array = oapackage.exampleArray(0)
array.showarray()

array:
 0  0
 0  0
 0  1
 0  1
 1  0
 1  0
 1  1
 1  1
```

Calculate properties of the array such as the D-efficiency for the main effects model, the generalized word length pattern and the rank.

```
[3]: print("D-efficiency %f, rank %d" % (array.Defficiency(), array.rank()))
print("Generalized wordlength pattern: %s" % str(array.GWLP()))

D-efficiency 1.000000, rank 2
Generalized wordlength pattern: (1.0, 0.0, 0.0)
```

Calculate the generalized word length pattern for another example array.

```
[11]: array = oapackage.exampleArray(11)
print("Generalized wordlength pattern: %s" % oapackage.oahelper.gwlp2str(array.GWLP()))
Generalized wordlength pattern: 1.00,0.02273,0.03926,0.5434,0.8244,2.217,1.043,0.126,0.
→002066
```

2.1.1 Indexing

The `array_link` object can be indexed as a normal array.

```
[12]: array[0:5, 2:3]
```

```
[12]: array_link: 5, 1
```

```
[14]: array[0:5, 2:4].showarray()
```

```
array:
```

```
 1 1
 0 1
 1 0
 0 0
 1 1
```

```
[15]: print(array[0, 2])
```

```
1
```

2.1.2 Numpy

We can convert between Numpy arrays and `array_link` objects. Note that an `array_link` is always integer valued.

```
[19]: X = (4 * np.random.rand(20, 10)).astype(int)
array = oapackage.array_link(X)
array.showarraycompact()
```

```
2003200102
0322120001
3030110033
0311131120
2200100200
2112333121
3110300211
3302313313
2331031302
1212232322
3003330322
0312311331
3222200313
2001123302
2222111302
0020322112
0101223211
```

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```
0223300100
1232030100
0320032113
```

Convert from `array_link` back to Numpy array.

```
[20]: X2 = np.array(array)
```

2.2 Example arrays

The package contains several example arrays and designs. They can be retrieved using the method `exampleArray`.

```
[4]: import oapackage
al = oapackage.exampleArray(-1, 1)

exampleArray 0: array in OA(8,2, 2^2)
exampleArray 1: array 3 in OA(16, 2, 2^5)
exampleArray 2: array 6 in OA(16, 2, 2^6)
exampleArray 3: array ? in OA(32, 3, 2^7)
exampleArray 4: array 4 in OA(16, 2, 2^7)
exampleArray 5: array 0 in OA(24, 2, 4 3 2^a)
exampleArray 6: array in OA(4, 2, 2^a)
exampleArray 7: array 0 in OA(4, 2, 2^a)?
exampleArray 8: array in OA(40, 3, 2^7)
exampleArray 9: array in A(40, 2^7), D-optimal
exampleArray 10: array in OA(9, 3^3)
exampleArray 11: D-optimal array in OA(44, 2^8)
exampleArray 12: even-odd array OA(64, 2^13)
exampleArray 13: array in OA(25, 2^5)
exampleArray 14: design in D(28, 2^5), D-efficiency is low
exampleArray 15: design in D(56, 2^10), D-efficiency is low
exampleArray 16: array in OA(32, 2, 2^5)
exampleArray 17: unique array in OA(64, 4, 2^7)
exampleArray 18: conference matrix of size 16, 7
exampleArray 19: conference matrix of size 4, 3
exampleArray 20: first LMC-0 double conference matrix in DC(24,3)
exampleArray 21: second LMC-0 double conference matrix in DC(16,4)
exampleArray 22: LMC-0 double conference matrix in DC(32,4)
exampleArray 23: LMC-0 double conference matrix in DC(32,6)
exampleArray 24: design in OA(64, 3, 2^16) (even-odd)
exampleArray 25: design in OA(64, 3, 2^16) (even-odd)
exampleArray 26: design in OA(64, 3, 2^16) (even-odd)
exampleArray 27: design in OA(64, 3, 2^16) (even-odd)
exampleArray 28: conference design in C(4, 3) in LMC0 form
exampleArray 29: conference design in C(4, 3)
exampleArray 30: conference design in C(8,4)
exampleArray 31: conference design in C(8,4)
exampleArray 32: first double conference design in DC(18,4)
exampleArray 33: second double conference design in DC(18,4)
exampleArray 34: third double conference design in DC(18,4)
exampleArray 35: first double conference design in DC(20,4)
```

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```
exampleArray 36: second double conference design in DC(20,4)
exampleArray 37: third double conference design in DC(20,4)
exampleArray 38: LMC0 conference design in C(30,3)
exampleArray 39: first LMC0 conference design in C(8,6)
exampleArray 40: first conference design in C(14, 5)
exampleArray 41: second conference design in C(14, 5)
exampleArray 42: third conference design in C(14, 5)
exampleArray 43: 2x2 array with zeros and a singe value -1
exampleArray 44: D-optimal strength 3 ortogonal array in OA(40,3, 2^7)
exampleArray 45: first conference design in C(20,8)
exampleArray 46: second conference design in C(20,8)
exampleArray 47: third conference design in C(20,8)
exampleArray 48: last conference design in C(20,8)
exampleArray 49: array 4347 C(20,8)
exampleArray 50: array 4506 C(20,8)
exampleArray 51: first array in C(12,4)
exampleArray 52: second array in C(12,4)
exampleArray 53: third array in C(12,4)
exampleArray 54: root array in OA(6,2,3^1 2^1)
exampleArray: no example array with index 55 exists
```

Select an example array and show it.

```
[3]: al=oapackage.exampleArray(2, 1)
al.showarray()

exampleArray 2: array 6 in OA(16, 2, 2^6)
array:
 0  0  0  0  0  0
 0  0  0  0  0  0
 0  0  0  1  1  1
 0  0  0  1  1  1
 0  1  1  0  0  1
 0  1  1  0  1  0
 0  1  1  1  0  1
 0  1  1  1  1  0
 1  0  1  0  0  1
 1  0  1  0  1  1
 1  0  1  1  0  0
 1  0  1  1  1  0
 1  1  0  0  1  0
 1  1  0  0  1  1
 1  1  0  1  0  0
 1  1  0  1  0  1
```

2.3 Example to write and read files with arrays from disk

The package can write arrays and designs to a custom file format. There is a text based format (specified by `oapackage.ATEXT`) and a binary format (specified by `oapackage.ABINARY`). See the online documentation for details on the file formats.

```
[1]: import oapackage
import tempfile
```

Create a list of two example arrays.

```
[2]: lst = [oapackage.exampleArray(32), oapackage.exampleArray(33)]
print(lst)

[array_link: 18, 4, array_link: 18, 4]
```

Write the two arrays to a file on disk.

```
[3]: filename = tempfile.mktemp(".oa")
_ = oapackage.writearrayfile(filename, lst, oapackage.ATEXT)
```

Display information about the file written.

```
[4]: oapackage.oainfo(filename)

file C:\Users\EENDEB~1\AppData\Local\Temp\tmpxc4dns16.oa: 18 rows, 4 columns, 2 arrays, ↴
mode text, nbits 0
```

The arrays can be read from disk again using the command `readarrayfile`.

```
[6]: lst2 = oapackage.readarrayfile(filename)
print(lst2)

(array_link: 18, 4, array_link: 18, 4)
```

The first array in the list that was read from disk is:

```
[7]: lst2[0].showarray()
```

```
array:
 0  0  0  0
 0  0  0  0
 1  1  1  1
 1  1  1  1
 1  1 -1 -1
 1  1 -1 -1
 1 -1  1 -1
 1 -1  1 -1
 1 -1 -1  1
 1 -1 -1  1
 -1  1  1 -1
 -1  1  1 -1
 -1  1 -1  1
 -1  1 -1  1
 -1 -1  1  1
 -1 -1  1  1
```

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```
-1 -1 -1 -1  
-1 -1 -1 -1
```

2.4 Enumerate orthogonal arrays

The Orthogonal Array package can completely enumerate all orthogonal arrays of a specified class. In this notebook, we enumerate specific classes of three-level orthogonal arrays and mixel-level orthogonal arrays.

First, we specify the class of three-level orthogonal arrays to enumerate. For example, we consider three-level orthogonal arrays of strength 2 with 27 runs and 8 factors.

```
[1]: import oapackage  
run_size = 27  
strength=2  
number_of_factors=8  
factor_levels = 3  
arrayclass=oapackage.arraydata_t(factor_levels, run_size, strength, number_of_factors)  
print(arrayclass)  
  
arrayclass: N 27, k 8, strength 2, s {3,3,3,3,3,3,3,3}, order 0
```

Second, we create the root array as the starting point of our enumeration.

```
[2]: l12=[arrayclass.create_root()]  
l12[0].showarraycompact()  
  
00  
00  
00  
01  
01  
01  
02  
02  
02  
10  
10  
10  
10  
11  
11  
11  
12  
12  
12  
20  
20  
20  
21  
21  
21  
22
```

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```
22
22
```

Third, extend the root array. It is also possible to extend a list of arrays.

```
[3]: list3columns = oapackage.extend_arraylist(l12, arrayclass)
print('extended to %d arrays with 3 columns' % len(list3columns))
list4columns = oapackage.extend_arraylist(list3columns, arrayclass)
print('extended to %d arrays with 4 columns' % len(list4columns))

extended to 9 arrays with 3 columns
extended to 711 arrays with 4 columns
```

It is also possible to extend selected arrays from a list.

```
[4]: l1 = oapackage.extend_arraylist(list4columns[0:8], arrayclass)
print('extended first 2 arrays to %d arrays with 5 columns' % len(l1))

extended first 2 arrays to 189 arrays with 5 columns
```

By adding one column at a time we can enumerate all three-level orthogonal arrays of strength 2 with 27 runs and 8 factors. The total computation time for this would be a couple of hours.

2.4.1 Mixed-level orthogonal arrays

The package can also enumerate mixed-level orthogonal arrays. For instance, consider enumerating all 16-run strength-2 orthogonal arrays with one four-level factor and nine two-level factors.

```
[9]: run_size = 16
strength=2
number_of_factors = 10
factor_levels=[4,2,2,2,2,2,2,2,2]
arrayclass=oapackage.arraydata_t(factor_levels, run_size, strength, number_of_factors)
print(arrayclass)

arrayclass: N 16, k 10, strength 2, s {4,2,2,2,2,2,2,2,2}, order 0
```

Create the root array as the starting point of our enumeration.

```
[10]: al=arrayclass.create_root()
al.showarraycompact()

00
00
01
01
10
10
11
11
20
20
21
21
```

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```
30
30
31
31
```

For these arrays, we can extend a single array or lists of arrays.

```
[14]: array_list=[arrayclass.create_root()]
array_list_3columns=oapackage.extend_arraylist(array_list, arrayclass)
array_list_4columns=oapackage.extend_arraylist(array_list_3columns, arrayclass)
print('extended to %d arrays with 3 columns' % len(array_list_3columns))
print('extended to %d arrays with 4 columns' % len(array_list_4columns))

extended to 3 arrays with 3 columns
extended to 10 arrays with 4 columns
```

Finally, enumerate all 16-run strength-2 orthogonal arrays with one four-level factor and nine two-level factors.

```
[15]: arrays = array_list_4columns
for extension_column in range(5, number_of_factors+1):
    extensions=oapackage.extend_arraylist(arrays, arrayclass)
    print('extended to %d arrays with %d columns' % (len(extensions), extension_column))
    arrays=extensions

extended to 28 arrays with 5 columns
extended to 65 arrays with 6 columns
extended to 110 arrays with 7 columns
extended to 123 arrays with 8 columns
extended to 110 arrays with 9 columns
extended to 72 arrays with 10 columns
```

2.4.2 Notes

- The numbers of isomorphism classes for various types of classes can be found at the webpage series of orthogonal arrays.
- For larger number of arrays the command line tools are more convenient and more memory efficient.

2.5 Generate orthogonal arrays with high D-efficiency

This notebook contains example code from the article Two-level designs to estimate all main effects and two-factor interactions by Eendebak, P. T. and Schoen, E. D. This example shows how to generate orthogonal arrays with a high D -efficiency in a reasonable amount of time (< 1 minute). For more results and details, see the paper.

Generate a D-optimal orthogonal array of strength 2 with 32 runs and 7 factors.

```
[12]: import numpy as np
import matplotlib.pyplot as plt
import oapackage
%matplotlib inline
```

```
[2]: run_size = 32
number_of_factors=7
factor_levels=2
strength=2
nkeep=24 # Number of designs to keep at each stage

arrayclass=oapackage.arraydata_t(factor_levels, run_size, strength, number_of_factors)
print('In this example we generate orthogonal arrays in the class: %s' % arrayclass)

In this example we generate orthogonal arrays in the class: arrayclass: N 32, k 7, ↴
→ strength 2, s {2,2,2,2,2,2}, order 0
```

First, generate orthogonal arrays with the function `extend_arraylist`. Next, keep the arrays with the best D -efficiency.

```
[7]: arraylist=[arrayclass.create_root()]

#% Extend arrays and filter based on D-efficiency
options=oapackage.OAextend()
options.setAlgorithmAuto(arrayclass)

for extension_column in range(strength+1, number_of_factors+1):
    print('extend %d arrays with %d columns with a single column' % (len(arraylist), ↴
→arraylist[0].n_columns) )
    arraylist_extensions = oapackage.extend_arraylist(arraylist, arrayclass, options)

    # Select the best arrays based on the D-efficiency
    dd = np.array([a.Defficiency() for a in arraylist_extensions])
    ind = np.argsort(dd)[::-1][0:nkeep]
    selection = [ arraylist_extensions[ii] for ii in ind]
    dd=dd[ind]
    print(' generated %d arrays, selected %d arrays with D-efficiency %.4f to %.4f' %_
→(len(arraylist_extensions), len(ind), dd.min(), dd.max() ) )

    arraylist = selection

extend 1 arrays with 2 columns with a single column
generated 5 arrays, selected 5 arrays with D-efficiency 0.0000 to 1.0000
extend 5 arrays with 3 columns with a single column
generated 19 arrays, selected 19 arrays with D-efficiency 0.0000 to 1.0000
extend 19 arrays with 4 columns with a single column
generated 491 arrays, selected 24 arrays with D-efficiency 0.9183 to 1.0000
extend 24 arrays with 5 columns with a single column
generated 2475 arrays, selected 24 arrays with D-efficiency 0.9196 to 1.0000
extend 24 arrays with 6 columns with a single column
generated 94 arrays, selected 24 arrays with D-efficiency 0.7844 to 0.8360
```

Show the best array from the list of D-optimal orthogonal arrays.

```
[20]: selected_array = selection[0]
print('Generated a design in OA(%d, %d, 2^%d) with D-efficiency %.4f' % (selected_array.
→n_rows, arrayclass.strength, selected_array.n_columns, dd[0] ) )
print('The array is (in transposed form):\n')
selected_array.transposed().showarraycompact()
```

```
Generated a design in OA(32, 2, 2^7) with D-efficiency 0.8360
The array is (in transposed form):
```

```
00000000000000001111111111111111
0000000011111110000000011111111
000001100011110001111100000111
00011001011001110110011100011001
0010101010101011010101100101010
01001011010110011101000101101001
01110010001101010111001010100011
```

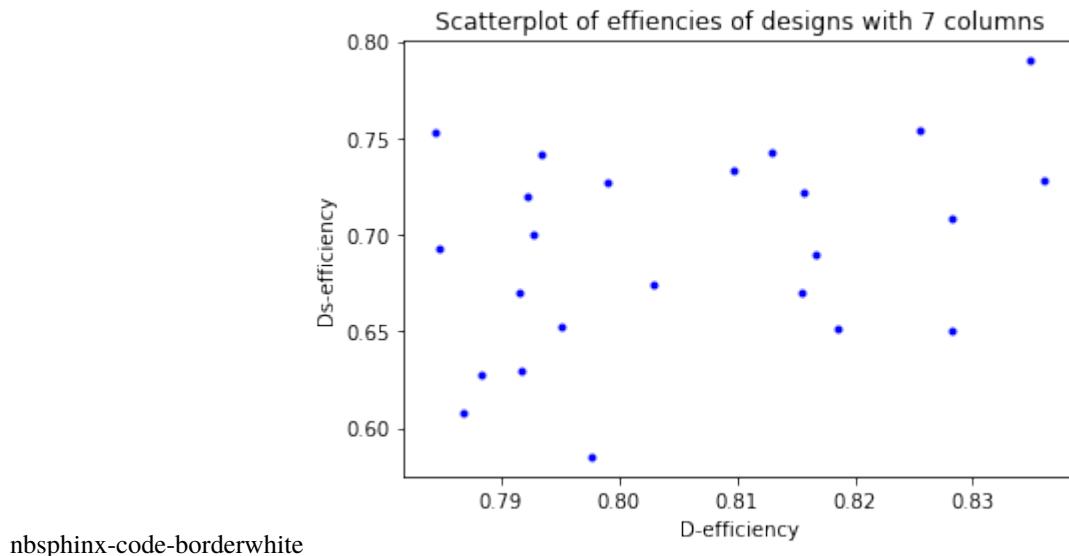
We calculate the D -, D_s - and D_1 -efficiencies.

```
[21]: efficiencies = np.array([array.Defficiencies() for array in arraylist])
print(efficiencies)
```

```
[[0.8360354  0.72763273 1.          ]
 [0.83481532 0.78995185 1.          ]
 [0.82829522 0.70849985 1.          ]
 [0.82829522 0.65037401 1.          ]
 [0.82545286 0.75411444 1.          ]
 [0.8185915  0.65157148 1.          ]
 [0.81676643 0.68965719 1.          ]
 [0.81559279 0.72218391 1.          ]
 [0.81557799 0.66966068 1.          ]
 [0.81302642 0.74299714 1.          ]
 [0.80973102 0.73354611 1.          ]
 [0.80286424 0.67455544 1.          ]
 [0.79907785 0.72697978 1.          ]
 [0.79762174 0.58515515 1.          ]
 [0.79514152 0.65199837 1.          ]
 [0.79348419 0.74167976 1.          ]
 [0.7928208  0.70038649 1.          ]
 [0.79225237 0.71961467 1.          ]
 [0.79171981 0.62994172 1.          ]
 [0.79160277 0.66978711 1.          ]
 [0.7883109  0.62733236 1.          ]
 [0.78683679 0.60799604 1.          ]
 [0.78477264 0.69310129 1.          ]
 [0.7843891  0.7533355  1.         ]]
```

Visualize the D -efficiencies using a scatter plot.

```
[19]: plt.plot(efficiencies[:,0], efficiencies[:,1], '.b')
plt.title('Scatterplot of efficiencies of designs with %d columns' % arraylist[0].n_
          _columns)
plt.xlabel('D-efficiency')
plt.ylabel('Ds-efficiency')
```



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2.6 Generate D-efficient designs

This notebook contains example code from the article [Two-level designs to estimate all main effects and two-factor interactions](#) by Eendebak, P. T. and Schoen, E. D. This example shows how to generate D-efficient designs with a user-specified optimization function.

```
[1]: import numpy as np
import oapackage
import oapackage.Doptim

%matplotlib inline
```

Define the class of designs to generate.

```
[2]: run_size = 40
number_of_factors = 7
factor_levels = 2
strength = 0
arrayclass = oapackage.arraydata_t(factor_levels, run_size, strength, number_of_factors)
print("We generate D-efficient designs with %d rows and %d columns\n" % (run_size, number_of_factors))

We generate D-efficient designs with 40 rows and 7 columns
```

Generate a single D-efficient design using $\alpha = (1, 2, 0)$ as the parameters for the optimization function. For details on this parameter and its corresponding optimization function, see [Two-Level Designs to Estimate All Main Effects and Two-Factor Interactions](#).

```
[3]: alpha = [1, 2, 0]
scores, design_efficiencies, designs, ngenerated = oapackage.Doptim.Doptimize(
    arrayclass, nrestarts=30, optimfunc=alpha, selectpareto=True
)
```

```
Doptim: optimization class 40.2-2-2-2-2-2-2  
Doptimize: iteration 0/30  
Doptimize: iteration 29/30  
Doptim: done (11 arrays, 0.4 [s])
```

```
[4]: print("\nGenerated %d designs, the efficiencies for these designs are:" % len(designs))  
for ii, d in enumerate(designs):  
    dd = d.Defficiencies()  
    print("array %d: D-efficiency %.4f, Ds-efficiency %.4f" % (ii, dd[0], dd[1]))  
  
D = [d.Defficiency() for d in designs]  
best = np.argmax(D)  
print("\nThe design with the highest D-efficiency (%.4f) is:\n" % D[best])  
  
designs[best].transposed().showarraycompact()
```

```
Generated 11 designs, the efficiencies for these designs are:  
array 0: D-efficiency 0.8815, Ds-efficiency 0.9807  
array 1: D-efficiency 0.9076, Ds-efficiency 0.9628  
array 2: D-efficiency 0.8670, Ds-efficiency 0.9827  
array 3: D-efficiency 0.8945, Ds-efficiency 0.9669  
array 4: D-efficiency 0.9027, Ds-efficiency 0.9540  
array 5: D-efficiency 0.8851, Ds-efficiency 0.9549  
array 6: D-efficiency 0.8737, Ds-efficiency 0.9581  
array 7: D-efficiency 0.9036, Ds-efficiency 0.9400  
array 8: D-efficiency 0.8614, Ds-efficiency 0.9595  
array 9: D-efficiency 0.8897, Ds-efficiency 0.9418  
array 10: D-efficiency 0.9046, Ds-efficiency 0.9203
```

The design with the highest D-efficiency (0.9076) is:

```
0010011001011001010101011101101100011101  
0011010111100101111100010111001100100010  
1011011111001010100010111001000010011010  
0101100001100111110011010001001100111110  
0011100010001101001011101101110100010001  
0011110000011011101001110011101010101000  
1000110011101000101110001001101111001101
```

Optimizing with a different optimization target leads to different D-efficient designs. Below we compare the sets of designs generated with optimization target [1,0,0] and [1,2,0].

```
[5]: scores0, design_efficiencies0, designs0, _ = oapackage.Doptim.Doptimize(  
    arrayclass, nrestarts=30, optimfunc=[1, 0, 0], selectpareto=True  
)  
  
Doptim: optimization class 40.2-2-2-2-2-2-2  
Doptimize: iteration 0/30  
Doptimize: iteration 29/30  
Doptim: done (13 arrays, 0.4 [s])
```

```
[7]: def combineEfficiencyData(lst):
```

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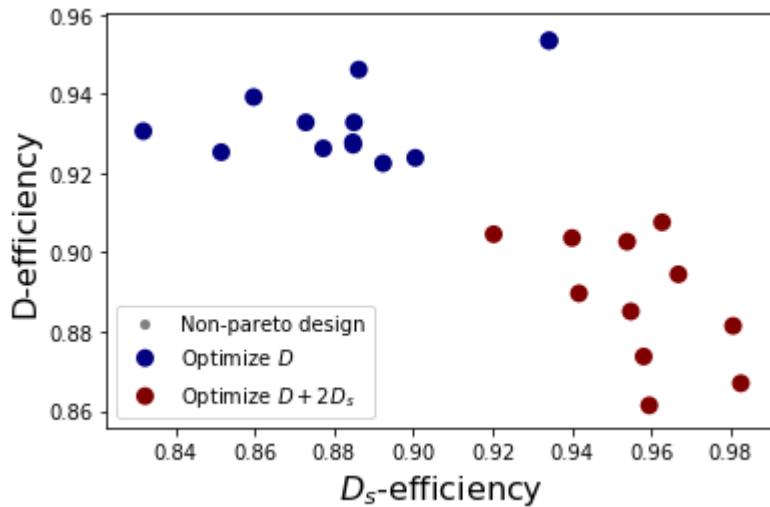
```

data = np.zeros((0, 4))

for jj, dds in enumerate(lst):
    dds_index = np.hstack((dds, jj * np.ones((len(dds), 1))))
    data = np.vstack((data, dds_index))
return data

design_efficiencies_combined = combineEfficiencyData([design_efficiencies0, design_
    ↪efficiencies])
plot_handles = oapackage.generateDscatter(
    design_efficiencies_combined, ndata=3, lbls=["Optimize $D$", "Optimize $D+2D_s$"], ↪
    ↪verbose=0
)
Pareto: 23 optimal values, 24 objects

```



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<Figure size 432x288 with 0 Axes>

[]:

2.7 Example script to use Nauty from Python

Nauty can be used to reduce any graph into a normal form. In this notebook, we show how to use the Nauty functionality from Python.

```
[1]: import numpy as np
import oapackage
```

Define a function to invert a permutation.

```
[2]: def inverse_permutation(perm):
    inverse = [0] * len(perm)
    for i, p in enumerate(perm):
```

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```
    inverse[p] = i
return inverse
```

We define a graph with 5 nodes. The graph is defined by the incidence matrix of size 5×5 and a coloring with two colors.

```
[3]: graph = np.zeros((5, 5), dtype=int)
graph[0, 1] = graph[0, 2] = graph[0, 3] = graph[1, 3] = 1
graph = np.maximum(graph, graph.T) # make array symmetric
colors = [0, 0, 0, 1, 1]
```

Reduce the graph to normal form using Nauty.

```
[4]: help(oapackage.reduceGraphNauty)
```

Help on function reduceGraphNauty in module oalib:

```
reduceGraphNauty(G, colors=None, verbose=1)
    Return vertex transformation reducing array to normal form
```

The reduction is calculated using `Nauty <<http://users.cecs.anu.edu.au/~bdm/nauty/>>`_

Args:

```
G (numpy array or array_link) : the graph in incidence matrix form
colors (list or None): an optional vertex coloring
```

Returns:

```
v: relabelling of the vertices
```

```
[4]: def reduce(graph, colors):
    tr = oapackage.reduceGraphNauty(graph, colors=colors, verbose=0)
    tri = inverse_permutation(tr)
```

```
graph_reduced = oapackage.transformGraphMatrix(graph, tri)
colors_reduced = [colors[idx] for idx in tr]
return graph_reduced, colors_reduced, tri
```

```
graph_reduced, colors_reduced, tr = reduce(graph, colors)
```

```
print("input graph: ")
print(graph)
```

```
print("normal form reduction: %s" % (tr,))
print("reduced graph: ")
print(graph_reduced)
print("colors reduced: %s" % (colors_reduced,))
```

```
input graph:
[[0 1 1 1 0]
 [1 0 0 1 0]
 [1 0 0 0 0]
 [1 1 0 0 0]]
```

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```
[0 0 0 0 0]
normal form reduction: (1, 2, 0, 4, 3)
reduced graph:
[[0 0 1 0 1]
 [0 0 1 0 0]
 [1 1 0 0 1]
 [0 0 0 0 0]
 [1 0 1 0 0]]
colors reduced: [0, 0, 0, 1, 1]
```

Apply a random permutation to the graph and reduce the graph again.

```
[5]: perm = np.random.permutation(5)
iperm = inverse_permutation(perm)
print("random permutation: %s" % (perm,))
graph2 = graph[perm, :][:, perm]
colors2 = [colors[idx] for idx in perm]
random permutation: [3 2 0 4 1]
```

Show the transformed matrix and color vector.

```
[8]: print(graph2)
print(colors2)

[[0 0 0 0 0]
 [0 0 0 1 1]
 [0 0 0 0 1]
 [0 1 0 0 1]
 [0 1 1 1 0]]
[1, 1, 0, 0, 0]
```

```
[6]: graph2_reduced, colors2_reduced, tr2 = reduce(graph2, colors2)

print("input graph: ")
print(graph2)

print("tr2: %s" % (tr2,))
print("reduced graph: ")
print(graph2_reduced)

print("colors2_reduced: %s" % (colors2_reduced,))

input graph:
[[0 0 1 0 1]
 [0 0 1 0 0]
 [1 1 0 0 1]
 [0 0 0 0 0]
 [1 0 1 0 0]]
tr2: (4, 1, 2, 3, 0)
reduced graph:
[[0 0 1 0 1]
 [0 0 1 0 0]
 [1 1 0 0 1]]
```

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```
[0 0 0 0 0]  
[1 0 1 0 0]]  
colors2_reduced: [0, 0, 0, 1, 1]
```

Check that the two reduced graphs are equal.

```
[9]: if np.all(graph_reduced == graph2_reduced):
        print("reduced arrays are equal!")
if np.all(colors_reduced == colors2_reduced):
        print("reduced colors are equal!")

reduced arrays are equal!
reduced colors are equal!
```

2.8 Analyse isomorphisms of a set of orthogonal arrays with N=56

In this example, we show how to identify isomorphic arrays from a list of two-level strength-2 orthogonal arrays with 56 runs and 28 factors.

```
[1]: import numpy as np
      import oapackage
      import oapackage.graphtools
      from oapackage.graphtools import selectIsomorphismClasses
```

Read the arrays from a file and determine their class.

Determine the unique isomorphism classes using Nauty.

```
[3]: b,mm=selectIsomorphismClasses(sols, verbose=0)

print('from %d arrays selected %d unique isomorphism classes' % (len(mm),np.unique(b).size))
print('indices: %s' % str(b) )

from 9 arrays selected 6 unique isomorphism classes
indices: [0 4 5 3 1 5 3 2 4]
```

Verify that the first two arrays are indeed non-isomorphic:

```
[4]: jj=np.abs(sols[0].Jcharacteristics(4))
n0, _=np.histogram(jj, [0,8,16,24])
print(n0)
jj=np.abs(sols[1].Jcharacteristics(4))
```

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```
n1, _=np.histogram(jj, [0,8,16,24])
print(n1)

[ 0 18018 2457]
[ 0 18032 2436]
```

Since the first two arrays have different J -characteristics (see the section [Statistical properties of orthogonal arrays](#) for details), they are non-isomorphic. For the isomorphic arrays, it is possible to obtain the array transformation to make the arrays identical using the function `reduceConferenceTransformation`.

2.9 Generation and analysis of conference designs

In this notebook, we show how to generate conference designs and calculate properties of these designs. For details on conference designs and their properties, see [Properties of conference designs](#) and [A Classification Criterion for Definitive Screening Designs](#), Schoen et al., 2018 and [Enumeration and Classification of Definitive Screening Designs] (in preparation).

Load required libraries and define the class of conference designs to enumerate.

```
[3]: import oapackage
conference_class=oapackage.conference_t(12, 6, 0)
print(conference_class)

conference class: number of rows 12, number of columns 6
```

Define the root array and extend the lists of conference designs.

```
[4]: conference_designs=[[conference_class.create_root_three_columns()]]  
  
for ii, ncols in enumerate(range(4, 8)):  
    arrays = oapackage.extend_conference (conference_designs[ii], conference_class,  
    ↴verbose=0)  
    conference_designs.append(arrays)  
    print('extension resulted in %d designs with %d columns' % (len(arrays), ncols))  
  
extension resulted in 9 designs with 4 columns  
extension resulted in 42 designs with 5 columns  
extension resulted in 123 designs with 6 columns  
extension resulted in 184 designs with 7 columns
```

2.9.1 Calculate properties of conference designs

Here, we show how to calculate relevant properties of conference designs. Select a 12-run 7-factor conference design generated previously.

```
[5]: design = conference_designs[4][0]
design.showarray()  
  
array:  
 0  1  1  1  1  1  1  
 1  0 -1 -1 -1 -1 -1  
 1  1  0 -1 -1  1  1
```

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1	1	1	0	1	-1	-1
1	1	1	-1	0	-1	1
1	1	-1	1	1	0	-1
1	1	-1	1	-1	1	0
1	-1	1	1	-1	1	-1
1	-1	1	1	-1	-1	1
1	-1	1	-1	1	1	-1
1	-1	-1	1	1	-1	1
1	-1	-1	-1	1	1	1

A sensible criterion to evaluate conference designs is the so-called F_4 -vector (Schoen et al., 2019). We can compute the F_4 -vector of a conference design as follows.

```
[6]: design.FvaluesConference(4)
```

```
[6]: (0, 25, 10)
```

Schoen et al., 2019 showed that conference designs are good building blocks for definitive screening designs (Xiao et al. 2012). The Orthogonal Array package can construct a definitive screening design from a conference design.

```
[9]: dsd = oapackage.conference2DSD(design)
dsd.showarray()
```

array:
0 1 1 1 1 1 1
1 0 -1 -1 -1 -1 -1
1 1 0 -1 -1 1 1
1 1 1 0 1 -1 -1
1 1 1 -1 0 -1 1
1 1 -1 1 1 0 -1
1 1 -1 1 -1 1 0
1 -1 1 1 -1 1 -1
1 -1 1 1 -1 -1 1
1 -1 1 -1 1 -1 -1
1 -1 -1 1 1 -1 1
1 -1 -1 1 1 -1 -1
1 -1 -1 -1 1 1 1
0 -1 -1 -1 -1 -1 -1
-1 0 1 1 1 1 1
-1 -1 0 1 1 -1 -1
-1 -1 -1 0 -1 1 1
-1 -1 -1 1 0 1 -1
-1 -1 1 -1 -1 0 1
-1 -1 1 -1 1 -1 0
-1 1 -1 -1 1 -1 1
-1 1 -1 -1 1 1 -1
-1 1 1 -1 -1 1 -1
-1 1 1 1 -1 1 -1
0 0 0 0 0 0 0

For the resulting definitive screening design, the Orthogonal Array package can compute some statistical properties based on projections into a smaller number of factors.

```
[7]: PEC4, PIC4, PPC4 = oapackage.conference.conferenceProjectionStatistics(design,
   ↪ncolumns=4, verbose=1)

conferenceProjectionStatistics: projection to 4 columns: PEC 0.286 PIC 3.111 PPC 0.458
```

2.10 Example code for delete-one-factor projections

Any orthogonal array can be reduced to delete-one-factor projection form using `reduceDOPform`. The method is described in the article [A canonical form for non-regular arrays based on generalized wordlength pattern values of delete-one-factor projections](#) by Eendebak, P. T. In this notebook, we reduce an example array to its delete-one-factor projection form.

Load required libraries and select an example orthogonal array with 16 runs and 7 factors.

```
[4]: import oapackage
```

```
al = oapackage.exampleArray(4)
al = oapackage.reduceDOPform(al)
al.showarray()
```

array:

0	0	0	0	0	0	0
0	0	0	0	0	0	1
0	0	0	1	1	1	0
0	0	0	1	1	1	1
0	1	1	0	0	1	0
0	1	1	0	0	1	1
0	1	1	1	1	0	0
0	1	1	1	1	0	1
1	0	1	0	1	0	0
1	0	1	0	1	1	1
1	0	1	1	0	0	0
1	0	1	1	0	1	1
1	1	0	0	1	0	1
1	1	0	0	1	1	0
1	1	0	1	0	0	1
1	1	0	1	0	1	0

A key property of the delete-of-factor projection form is that the generalized word length patterns (GWLPs) of the projections are ordered. For details on the GWLP, see [Statistical properties of orthogonal arrays](#).

```
[5]: print("GWLP %s" % str(al.GWLP()))
for ii in range(0, al.n_columns):
    bl = al.deleteColumn(ii)
    print("Delete column %d: GWLP %s" % (ii, str(bl.GWLP())))

GWLP (1.0, 0.0, 0.0, 3.5, 2.5, 0.5, 0.5, 0.0)
Delete column 0: GWLP (1.0, 0.0, 0.0, 1.5, 1.0, 0.5, 0.0)
Delete column 1: GWLP (1.0, 0.0, 0.0, 1.75, 0.75, 0.25, 0.25)
Delete column 2: GWLP (1.0, 0.0, 0.0, 1.75, 0.75, 0.25, 0.25)
Delete column 3: GWLP (1.0, 0.0, 0.0, 2.0, 1.0, 0.0, 0.0)
Delete column 4: GWLP (1.0, 0.0, 0.0, 2.0, 1.0, 0.0, 0.0)
```

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```
Delete column 5: GWLP (1.0, 0.0, 0.0, 2.0, 1.0, 0.0, 0.0)
Delete column 6: GWLP (1.0, 0.0, 0.0, 3.0, 2.0, 0.0, 0.0)
```

The symmetry group of the projection GWLPs can be calculated. This symmetry group determines how fast an array can be reduced to normal form.

```
[6]: dof_values = oapackage.projectionDOFvalues(al)
sg = oapackage.symmetry_group(dof_values, False)
sg.show(1)

symmetry group: 7 elements, 4 subgroups: 1 2 3 1
```

It is also possible to reduce mixed-level arrays to their delete-of-factor projection forms. We now show an example involving an orthogonal array with 24 runs, one four-level factor, one three-level factor and three two-level factors.

```
[8]: al = oapackage.exampleArray(5)
al.showarray()
dopgwlps = oapackage.projectionGWLPs(al)
print("delete-one-factor GWLP values %s" % ([x.raw_values() for x in dopgwlps,]))

array:
 0  0  0  0  0
 0  0  0  0  0
 0  1  0  0  0
 0  1  1  1  1
 0  2  1  1  1
 0  2  1  1  1
 1  0  0  1  1
 1  0  0  1  1
 1  1  0  0  1
 1  1  1  1  0
 1  2  1  0  0
 1  2  1  0  0
 2  0  1  0  1
 2  0  1  0  1
 2  1  0  1  0
 2  1  1  0  1
 2  2  0  1  0
 2  2  0  1  0
 3  0  1  1  0
 3  0  1  1  0
 3  1  0  1  1
 3  1  1  0  0
 3  2  0  0  1
 3  2  0  0  1

delete-one-factor GWLP values [(1.0, 0.0, 0.0, 0.0, 0.6666666666666666), (1.0, 0.0, 0.0, 0.0, 2.111111111111111, 0.0), (1.0, 0.0, 0.0, 1.8888888888888888, 0.4444444444444444), (1.0, 0.0, 0.0, 2.3333333333333335, 0.0), (1.0, 0.0, 0.0, 1.8888888888888888, 0.4444444444444444)]
```

The delete-of-factor values for mixel-level arrays consists of the factor level of the deleted column and the GWLP of the projection.

```
[9]: oapackage.projectionGWLPs
dopgwp = oapackage.projectionGWLPs(al)
arrayclass = oapackage.arraylink2arraydata(al)
dofvalues = oapackage.projectionDOFvalues(al)
factor_levels = arrayclass.factor_levels()

for column, dof_value in enumerate(dofvalues):
    print("column %d: factor level %s" % (column, factor_levels[column]))
    print("  delete-of-factor value: %s" % (list(dof_value.raw_values()),))

column 0: factor level 4
  delete-of-factor value: [-4.0, 1.0, 0.0, 0.0, 0.0, 0.6666666666666666]
column 1: factor level 3
  delete-of-factor value: [-3.0, 1.0, 0.0, 0.0, 2.111111111111111, 0.0]
column 2: factor level 2
  delete-of-factor value: [-2.0, 1.0, 0.0, 0.0, 1.888888888888888, 0.4444444444444444]
column 3: factor level 2
  delete-of-factor value: [-2.0, 1.0, 0.0, 0.0, 2.3333333333333335, 0.0]
column 4: factor level 2
  delete-of-factor value: [-2.0, 1.0, 0.0, 0.0, 1.888888888888888, 0.4444444444444444]
```

Show the reduced array.

```
[10]: reduced_array = al.reduceDOP()
al.showarray()
```

```
array:
 0  0  0  0  0
 0  0  0  0  0
 0  1  0  0  0
 0  1  1  1  1
 0  2  1  1  1
 0  2  1  1  1
 1  0  0  1  1
 1  0  0  1  1
 1  1  0  0  1
 1  1  1  1  0
 1  2  1  0  0
 1  2  1  0  0
 2  0  1  0  1
 2  0  1  0  1
 2  1  0  1  0
 2  1  1  0  1
 2  2  0  1  0
 2  2  0  1  0
 3  0  1  1  0
 3  0  1  1  0
 3  1  0  1  1
 3  1  1  0  0
 3  2  0  0  1
 3  2  0  0  1
```

2.11 Minimal number of runs for an orthogonal array

In this example we calculate the minimum number of runs required for an orthogonal array. For more details, see Schoen et al.

```
[6]: import itertools
import numpy as np

def minimum_number_of_runs(factor_levels, strength):
    """Calculate the minimum number of runs for an orthogonal array

    The minimum number of runs is based on the strength conditions. Whether a design
    actually exists
    Args:
        factor_levels: Factor levels of the design
        strength: Strength of the array
    Returns:
        Minimum number of runs

    """
    runs = [np.prod(tt) for tt in itertools.combinations(factor_levels, strength)]
    N = np.lcm.reduce(runs)
    return N
```

We run the method on several examples.

```
[7]: strength = 3
factor_levels = [2, 3, 3, 4, 5]
N = minimum_number_of_runs(factor_levels, strength)

print(f"for a design of strength {strength} and factor levels {factor_levels} we require
      (a multiple of) {N} runs")
for a design of strength 3 and factor levels [2, 3, 3, 4, 5] we require (a multiple of)
      360 runs
```

```
[12]: strength = 2
factor_levels = [3, 2, 2, 2, 2]
N = minimum_number_of_runs(factor_levels, strength)

print(f"for a design of strength {strength} and factor levels {factor_levels} we require
      (a multiple of) {N} runs")
for a design of strength 2 and factor levels [3, 2, 2, 2, 2] we require (a multiple of)
      12 runs
```

```
[ ]:
```

2.12 Example of GWLP calculation for mixed-level designs

This notebook contains example code to compute the type-specific generalized word-length pattern (GWLP) for mixed-level designs, more specifically for regular four-and-two-level designs.

In four-and-two-level designs, the four-level factors are constructed us the grouping scheme of [Wu & Zhang \(1989\)](#) where the levels of a four-level factor A are based on the levels of three two-level factors a_1, a_2 and a_3 , called the pseudo-factors, where $I = a_1a_2a_3$:

a_1	a_2	a_3	\rightarrow	A
1	1	0	\rightarrow	0
1	0	1	\rightarrow	1
0	1	1	\rightarrow	2
0	0	0	\rightarrow	3

The two-level factors can either be main factors or be entirely aliased with a combination of the main factors. Such aliased factors are called added factors. If one of the main factors, used in an added factor, is also used as pseudo-factor in a four-level factor, then the added factor has type I . If it is used as pseudo-factor in two distinct four-level factor, it has type II , etc . . .

```
[1]: import numpy as np
import oapackage
```

Create a $4^{12}7$ four-and-two-level regular design in 32 runs with 1 four-level factor and 7 two-level factors.

```
[2]: array = oapackage.exampleArray(56, 1)
array = array.selectFirstColumns(7)
arrayclass = oapackage.arraylink2arraydata(array)
array.showarraycompact()

exampleArray 56: design in OA(32, 42^{18})
0000000
0100110
0101010
0001100
0110011
0010101
0011001
0111111
1010100
1110010
1111110
1011000
1100111
1000001
1001101
1101011
2101101
2001011
2000111
2100001
2011110
2111000
2110100
```

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```
2010010
3111001
3011111
3010011
3110101
3001010
3101100
3100000
3000110
```

The GWLP for mixed-level designs is computed using the adapted forms of equations (7) and (8) in Xu and Wu (2001).

2.12.1 Distance distribution

First, the distance distribution is first computed for all combinations of (i, j) with $i \in \{0, 1\}$ and $j = 0, \dots, 7$ and $i \neq j$. In this example with a $4^1 2^7$ design, that is a 2×8 matrix B , where $B_{i,j}$ is the number of rows that have $(1 - i)$ different elements if their four-level parts and $(7 - j)$ different elements in their two-level parts, divided by the number of runs.

```
[3]: Dm = oapackage.distance_distribution_mixed(array, 0)
D = np.array(Dm).astype(int)
print(f"distance distribution for mixed-level design\n{D}")

distance distribution for mixed-level design
[[1 0 1 4 1 0 1]
 [0 2 6 8 6 2 0]]
```

This is verified since the sum of the matrix is 32 which is equal to $\binom{32}{2} 32^{-1}$.

2.12.2 McWilliams Transforms

Now, the second step in the computation of the GWLP, is to use the McWilliams Transforms to obtain the GWLP from the distance distribution matrix. The McWilliams Transform will create another 2×8 matrix B' , obtained using the following formula

$$B'_{j_1, j_2} = N^{-1} \sum_{i_1=0}^m \sum_{i_2=0}^n B_{i_1, i_2} P_{j_1}(i_1; 1, 4) P_{j_2}(i_2; 7, 2)$$

where $P_j(x, n, s)$ is the Krawtchouck polynomials for a total of n factors with s levels.

```
[4]: N = array.n_rows
factor_levels_for_groups = arrayclass.factor_levels_column_groups()
Bprime = oapackage.macwilliams_transform_mixed(Dm, N, factor_levels_for_groups,
                                              verbose=0)
print(f"MacWilliams transform:")
print(np.array(Bprime).astype(int))

MacWilliams transform:
[[1. 0. 0. 0. 1. 0. 0.]
 [0. 0. 2. 0. 4. 0. 0.]]
```

This matrix is equivalent to the type specific generalized word-length pattern, where the row index indicates the type of words (0 to 1) and the column index indicates the length of the words (0 to 7).

The generalized word-length pattern (A) can be obtained by summing the rows of the B' matrix anti-diagonally. That is:

$$A_j(D) = \sum_{i'+j'=j} B'_{i',j'}$$

```
[4]: gwlp_mixed = oapackage.GWLPmixed(array, 0)
print(f"GWLP: {gwlp_mixed}")

GWLP: (1.0, 0.0, 0.0, 2.0, 1.0, 4.0, 0.0, 0.0)
```

2.13 Calculate a Pareto optimal set

Pareto optimality (or multi-objective optimization) allows one to search for optimal solutions for an optimization problem with multiple objectives. The Pareto class in the Orthogonal Array package allows one to calculate the Pareto optimal elements (called the Pareto frontier).

```
[1]: import numpy as np
import matplotlib.pyplot as plt
%matplotlib inline

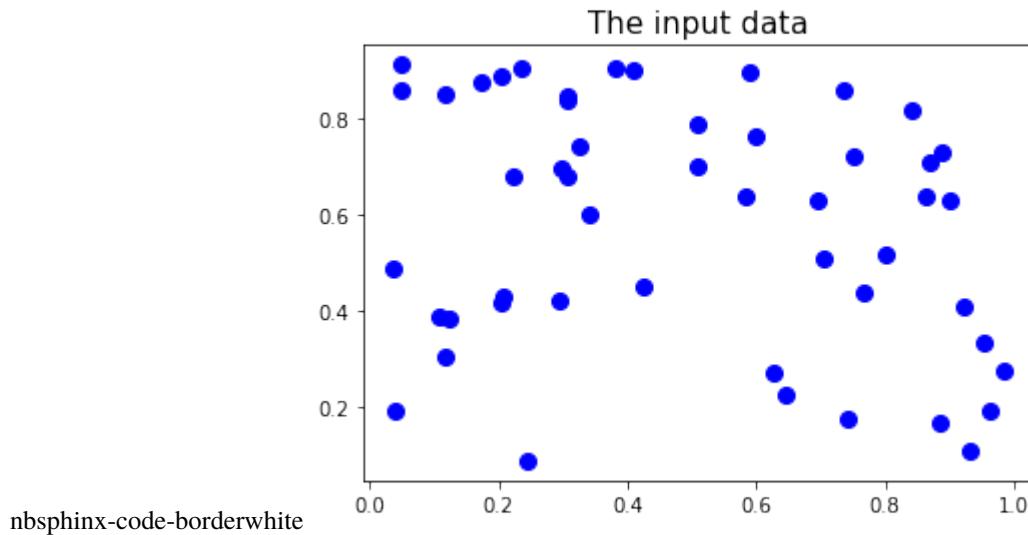
import oapackage
```

First, define a dataset of 50 random vectors. The vectors have length 2, so there are 2 objectives to be optimized.

```
[2]: datapoints=np.random.rand(2, 50)

for ii in range(0, datapoints.shape[1]):
    w=datapoints[:,ii]
    fac=.6+.4*np.linalg.norm(w)
    datapoints[:,ii]=(1/fac)*w

h=plt.plot(datapoints[0,:], datapoints[1,:], '.b', markersize=16, label='Non Pareto-optimal')
plt.title('The input data', fontsize=15)
plt.xlabel('Objective 1', fontsize=16)
plt.ylabel('Objective 2', fontsize=16)
```



Create a structure (ParetoDoubleLong) to keep track of the data.

```
[3]: pareto=oapackage.ParetoDoubleLong()

for ii in range(0, datapoints.shape[1]):
    w=oapackage.doubleVector( (datapoints[0,ii], datapoints[1,ii]))
    pareto.addvalue(w, ii)

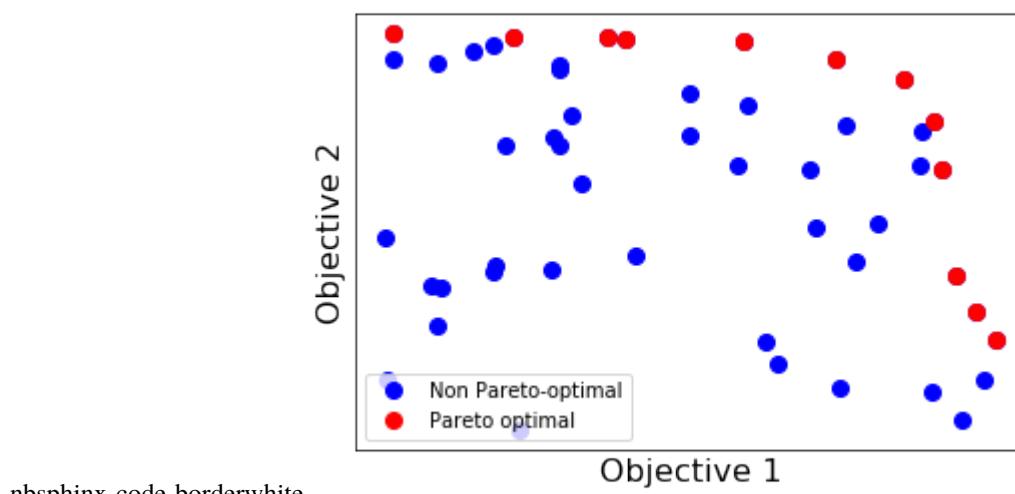
pareto.show(verbose=1)
Pareto: 12 optimal values, 12 objects
```

Plot the results.

```
[4]: lst=pareto.allindices() # the indices of the Pareto optimal designs

optimal_datapoints=datapoints[:,lst]

h=plt.plot(datapoints[0,:], datapoints[1,:], '.b', markersize=16, label='Non Pareto-optimal')
hp=plt.plot(optimal_datapoints[0,:], optimal_datapoints[1,:], '.r', markersize=16, label='Pareto optimal')
plt.xlabel('Objective 1', fontsize=16)
plt.ylabel('Objective 2', fontsize=16)
plt.xticks([])
plt.yticks([])
_=plt.legend(loc=3, numpoints=1)
```



2.14 Isomorphism reduction for conference designs

In this example, we show how to test if two conference designs are isomorphic. We consider conference designs with 10 runs and 3 factors, and calculate a reduction to their normal form. Using the reduction, we determine if the two designs are isomorphic.

```
[1]: import oapackage
import numpy as np

A = np.array([
    [0, 1, 1, 1, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, -1, 1, 1, -1, 1, -1, 1, 1, -1, 1, 1, -1, -1, 1, 1, -1],
    [-1, 1, -1, -1]
]).reshape(10, 3)
B = np.array([
    [0, 1, 1, 1, 0, -1, 1, 1, 1, 1, 1, 1, 1, 1, -1, 1, 1, -1, 1, -1, 1, 0, 1, -1, 1, 1, -1, -1, 1, 1, -1],
    [-1, 1, -1, -1]
]).reshape(10, 3)
array1 = oapackage.makearraylink(A)
array2 = oapackage.makearraylink(B)

array1.showarray()
array2.showarray()

array:
  0   1   1
  1   0   1
  1   1   0
  1   1   1
  1   1  -1
  1   1  -1
  1  -1   1
  1  -1   1
  1  -1  -1
  1  -1  -1
array:
```

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```

0  1  1
1  0 -1
1  1  1
1  1  1
1  1 -1
1  1 -1
1 -1  0
1 -1  1
1 -1  1
1 -1 -1

```

We calculate the normal forms of the conference designs using the function `reduceConference` or `reduceConferenceTransformation`. The result of the former is the reduced design, while the result of the latter is an object describing the transformation to normal form. The normal form is calculated using Nauty.

[2]: `help(oapackage.reduceConference)`

Help on function `reduceConference` in module `oalib`:

```

reduceConference(arg1, verbose=0)
    reduceConference(array_link arg1, int verbose=0) -> array_link
    reduceConference(array_link arg1) -> array_link

```

Reduce conference matrix to normal form using Nauty

See also: `reduceConferenceTransformation`

[3]: `T1 = oapackage.reduceConferenceTransformation(array1, verbose=1)`

`T2 = oapackage.reduceConferenceTransformation(array2, verbose=1)`

`T1.show()`

`reduceConferenceTransformation: reduce design with 10 rows, 3 columns`

`reduceConferenceTransformation: reduce design with 10 rows, 3 columns`

`row permutation: {2,0,1,9,7,8,5,6,3,4}`

`row flips: {1,1,-1,1,1,1,1,1,1,1}`

`column permutation: {0,1,2}`

`col flips: {1,-1,-1}`

We can check whether the designs are isomorphic by comparing the normal forms.

[4]: `design_equal = T1.apply(array1) == T2.apply(array2)`

`print("designs isomorphic? %s" % design_equal)`

`designs isomorphic? 1`

The designs are isomorphic. So, it is possible to calculate a reduction of the second design into the first design.

[5]: `TT = T1.inverse() * T2`

`TT.show()`

```

row permutation: {0,1,8,9,6,7,2,4,5,3}
  row flips: {-1,1,1,1,1,1,1,1,1,1}
column permutation: {0,1,2}
  col flips: {1,-1,-1}

```

[6]:

```
r1 = T1.apply(array1)
r1.showarray()
r2 = T2.apply(array2)
r2.showarray()
```

```

array:
1  0  -1
1  -1  0
0  1  1
1  1  1
1  1  1
1  1  -1
1  1  -1
1  -1  1
1  -1  1
1  -1  -1

```

```

array:
1  0  -1
1  -1  0
0  1  1
1  1  1
1  1  1
1  1  -1
1  1  -1
1  -1  1
1  -1  1
1  -1  -1

```

Calculate some properties of a conference design; see the section [Properties of conference designs](#) for details.

[7]:

```
print("array 1: is_conference() %d" % array1.is_conference())
print("array 1: J2-characteristics %s" % (oapackage.Jcharacteristics_conference(array1,
    number_of_columns=2),))
array 1: is_conference() 1
array 1: J2-characteristics (0, 0, 0)
```

[8]:

```
help(oapackage.Jcharacteristics_conference)
```

Help on function Jcharacteristics_conference in module oalib:

```
Jcharacteristics_conference(array, number_of_columns, verbose=0)
  Jcharacteristics_conference(array_link array, int number_of_columns, int verbose=0) -
-> intVector
  Jcharacteristics_conference(array_link array, int number_of_columns) -> intVector
```


DATA REPRESENTATION

All designs handled by the OApackage are integer valued. The designs (whether these are orthogonal arrays, optimal designs or conference designs) are stored in an `array_link()` object. The definitions of orthogonal arrays, optimal designs and conference designs are included in the section *Definitions of arrays and designs*.

3.1 Data structures

The package contains several data structures. Here, we describe the main structures and their use.

`array_link()`

The structure containing an orthogonal array is called the `array_link()` structure. Lists of arrays are stored in the `arraylist_t()` object, which is implemented as a `std::deque` container.

`arrayfile_t()`

This object allows for reading and writing of arrays to disk.

`arraydata_t()`

The structure describing a certain class of orthogonal arrays or optimal designs.

`conference_t()`

The structure describing a certain class of conference designs.

`array_transformation_t()`

The structure describing a transformation of an orthogonal array, which includes row and column permutations, as well as permutations to the symbols in one or more columns.

`conference_transformation_t()`

The structure describing a transformation of conference design or double conference design, which includes row and column permutations, as well as sign switches to the elements in one or more rows and columns.

3.2 Representing arrays

The structure containing an orthogonal array is called the `array_link` structure. It consists of a specified number of rows and columns, the data (integer valued) and an index. In the Python interface, the `array_link()` object can be indexed just as normal arrays.

It is also possible to convert to a Numpy array. The `array_link` object implements the Python array interface, so most operations from packages such as Numpy work on the `array_link()` object.

Array representation and indexing in Python

```
>>> import oapackage; import numpy as np
>>> al=oapackage.exampleArray(0)
>>> al.showarray()
array:
 0  0
 0  0
 0  1
 0  1
 1  0
 1  0
 1  1
 1  1

>>> al[2,1]
1
>>> X=np.array(al)
>>> X
array([[0,  0],
       [0,  0],
       [0,  1],
       [0,  1],
       [1,  0],
       [1,  0],
       [1,  1],
       [1,  1]], dtype=int16)
```

The C++ class is *array_link*.

3.3 Classes of arrays

The *arraydata_t* object represents data about a class of orthogonal arrays, e.g. the class OA($N; t; s^k$); see *Definitions of arrays and designs*. The *conference_t* object represents data about a class of conference designs.

3.4 Array transformations

Transformations of (orthogonal) arrays consist of row, column and level permutations. A transformation is represented by the *array_transformation_t* object.

For a given transformation, the column permutations are applied first, then the level permutations and finally the row permutations. The level and column permutations are not commutative.

The conference design transformations also allow for row sign switches and are described by the class *conference_transformation_t*.

3.5 Reading and writing arrays

Reading and writing arrays to disk can be done with the `arrayfile_t` class.

Write an array or a list of arrays to disk

```
>>> import oapackage
>>> list_of_arrays = [oapackage.exampleArray(24), oapackage.exampleArray(25)]
>>> _ = oapackage.writearrayfile('test.oa', list_of_arrays)
>>> oapackage.oainfo('test.oa')
file test.oa: 64 rows, 16 columns, 2 arrays, mode text, nbits 0
>>> al=oapackage.exampleArray()
>>> af=oapackage.arrayfile_t('test.oa', al.n_rows, al.n_columns)
>>> af.append_array(al)
>>> print(af)
file test.oa: 8 rows, 2 columns, 1 arrays, mode text, nbits 8
>>> af.closefile()
```

The arrays can be written in text or binary format. For more details on the file format, see the section [File formats](#).

The Python interface is `oalib.arrayfile_t()` and the C++ interface is `arrayfile_t`.

3.6 File formats

The Orthogonal Array package stores arrays in a custom file format. There is a text format which is easily readable by humans and a binary format which is faster to process and memory efficient.

3.6.1 Plain text array files

Arrays are stored in plain text files with extension `.oa`. The first line contains the number of columns, the number of rows and the number of arrays (or -1 if the number of arrays is not specified). Then, for each array, a single line with the index of the array, followed by N lines containing the array.

A typical example of a text file is the following:

```
5 8 1
1
0 0 0 0 0
0 0 0 1 1
0 1 1 0 0
0 1 1 1 1
1 0 1 0 1
1 0 1 1 0
1 1 0 0 1
1 1 0 1 0
-1
```

This file contains exactly 1 array with 8 rows and 5 columns.

3.6.2 Binary array files

Every binary file starts with a header, which has the following format:

```
[INT32] 65 (magic identifier)
[INT32] b: Format: number of bits per number. Currently supported are 1 and 8
[INT32] N: number of rows
[INT32] k: kumber of columns
[INT32] Number of arrays (can be -1 if unknown)
[INT32] Binary format number: 1001: normal, 1002: binary diff, 1003: binary diff zero
[INT32] Reserved integer
[INT32] Reserved integer
```

The format of the remainder of the binary file depends on the binary format specified. For the normal binary format, the format is as follows. For each array, the number is specified in the header:

```
[INT32] Index
[Nxk elements] The elements contain b bits
```

If the number of bits per number is 1 (e.g. a 2-level array), then the data is padded with zeros to a multiple of 64 bits. The data of the array is stored in column-major order. The binary file format allows for random access reading and writing. The **binary diff** and **binary diff zero** formats are special formats.

A binary array file can be compressed using gzip. Most tools in the Orthogonal Array package can read these compressed files transparently. Writing to compressed array files is not supported at the moment.

3.6.3 Data files

The analysis tool (`oaanalyse`) writes data to disk in binary format. The format consists of a binary header:

```
[FLOAT64] Magic number 30397995;
[FLOAT64] Magic number 12224883;
[FLOAT64] nc: Number of rows
[FLOAT64] nr: Number of columns
```

After the header there follow $nc \times nr$ [FLOAT64] values.

3.6.4 MD5 sums

To check data integrity on disk, the packages includes functions to generate MD5 sums of designs.

Calculate md5 sum of a design

```
>>> import oapackage; a1=oapackage.exampleArray(0)
>>> a1.md5()
'6454c492239a8e01e3c01a864583abf2'
```

The C++ functions are `array_link::md5()` and `md5()`.

3.7 Command line interface

Several command line tools are included in the Orthogonal Array package. For each tool, help can be obtained from the command line by using the switch -h. The tools include the following:

oainfo

This program reads Orthogonal Array package data files and reports the contents of the files. For example:

```
$ oainfo result-8.2-2-2-2.oa
Orthogonal Array package 1.8.7
oainfo: reading 1 file(s)
file result-8.2-2-2-2.oa: 8 rows, 3 columns, 2 arrays, mode text, nbits 0
$
```

oacat

Shows the contents of a file with orthogonal arrays for a data file.

oacheck

Checks or reduces an array to canonical form.

oaextendsingle

Extends a set of arrays in LMC form with one or more columns.

oacat

Shows the contents of an array file or data file.

Usage: oacat [OPTIONS] [FILES]

oajoin

Reads one or more files from disk and join all the array files into a single list.

oasplit

Takes a single array file as input and splits the arrays into a specified number of output files.

oapareto

Calculates the set of Pareto optimal arrays in a file with arrays.

oaanalyse

Calculates various statistical properties of arrays in a file. The properties are described in section [Properties of designs](#).

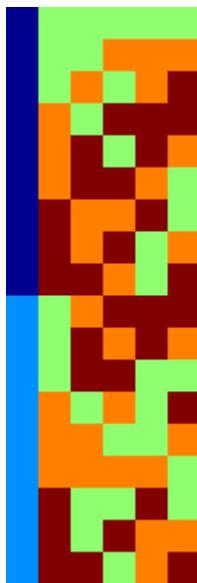


Fig. 1: Orthogonal array in $\text{OA}(18, 23^a, 2)$.

GENERATION OF DESIGNS

The Orthogonal Array package can be used to generate several classes of arrays and designs. A collection of arrays and designs generated by the package is available on the website <http://www.pieterendebak.nl/oapackage/index.html>.

4.1 Generation of orthogonal arrays

A list of arrays in LMC form (i.e., lexicographically minimum in columns) can be extended to a list of arrays in LMC form with one additional column. Details about the algorithm are described in [SEN10].

The main function for array extension is the function `extend_arraylist()`. The arguments for this function are the list of arrays to extend, a specification of the class of arrays in `arraydata_t` and the options `OAextend` for the algorithm.

An example of a session that extends an array is:

```
>>> import oapackage
>>> nrows=8; ncols=3;
>>> arrayclass=oapackage.arraydata_t(2, nrows, 2, ncols)
>>> root_array=arrayclass.create_root()
>>> root_array.showarraycompact()
00
00
01
01
10
10
11
11
>>> array_list=oapackage.extend_array(root_array, arrayclass)
>>> print('found %d extensions of the root array' % len(array_list))
found 2 extensions of the root array
```

A more detailed example is included in *Enumerate orthogonal arrays*.

4.2 Conference designs

A conference design is an $N \times k$ matrix with entries 0, -1, +1 such that i) in each column the symbol 0 occurs exactly one time and ii) all columns are orthogonal to each other. For details on conference designs, see the section [Properties of conference designs](#) and [SEG19]. An example of a session to generate conference designs is the following:

Generate conference designs with 8 rows

```
>>> import oapackage
>>> conference_class=oapackage.conference_t(8, 6, 0)
>>> array = conference_class.create_root_three_columns()
>>> array.showarray()
array:
 0   1   1
 1   0  -1
 1   1   0
 1   1   1
 1   1  -1
 1  -1   1
 1  -1   1
 1  -1  -1
>>> l4=oapackage.extend_conference ([array], conference_class, verbose=0)
>>> l5=oapackage.extend_conference ( l4, conference_class, verbose=0)
>>> l6=oapackage.extend_conference ( l5, conference_class, verbose=0)
>>> print('number of non-isomorphic conference designs with 6 columns: %d' % len(l6) )
number of non-isomorphic conference designs with 6 columns: 11
```

An example notebook with more functionality is included in [Generation and analysis of conference designs](#). The full interface for conference designs is available in the [Interface for conference designs](#).

The main functions to extend conference and double conference designs are `extend_conference()` and `extend_double_conference()`, respectively. The low-level functions for generating candidate extension columns of conference and double conference designs are `generateConferenceExtensions()` and `generateDoubleConferenceExtensions()`, respectively.

The conference designs are generated in `LMO` form.

4.3 Calculation of D-efficient designs

D-efficient designs (sometimes called D-optimal designs) can be calculated with the function `oapackage.Doptim.Doptimize()`. This function uses a coordinate-exchange algorithm to generate designs with good properties for the D -efficiency. With the coordinate-exchange algorithm, the following target function T is optimized:

$$T = \alpha_1 D_{\text{eff}} + \alpha_2 D_{s,\text{eff}} + \alpha_3 D_{1,\text{eff}}$$

Here, α is a weight vector specified by the user. Details on the D_{eff} , $D_{s,\text{eff}}$ and $D_{1,\text{eff}}$ can be found in the section [Optimality criteria for D-efficient designs](#).

A Python script to generate D-efficient designs with 40 runs and 7 factors is shown below.

Example of Doptimize usage

```

>>> N=40; s=2; k=7;
>>> arrayclass=oapackage.arraydata_t(s, N, 0, k)
>>> print('We generate optimal designs with: %s' % arrayclass)
We generate optimal designs with: arrayclass: N 40, k 7, strength 0, s {2,2,2,2,2,2,2}, order 0
>>> alpha=[1,2,0]
>>> scores, dds, designs, ngenerated = oapackage.Doptimize(arrayclass, nrestarts=40,
   optimfunc=alpha, selectpareto=True, verbose=0)
Doptimize: iteration 0/40
Doptimize: iteration 39/40
>>> print('Generated %d designs, the best D-efficiency is %.4f' % (len(designs), dds[:, 0].max() ))
Generated 10 designs, the best D-efficiency is 0.9198

```

The parameters of the `Doptimize()` function are documented in the code.

To calculate the D -, D_s - and D_1 -efficiencies of the designs, we can use the method `Deficiencies()`. For details on these efficiencies, see the section *Optimality criteria for D-efficient designs* and [ES17].

In [ES17], it is shown that one can optimize a linear combination of the D -efficiency and D_s -efficiency to generate a rich set of good compromise designs. From the generated designs, the optimal ones according to Pareto optimality can be selected.

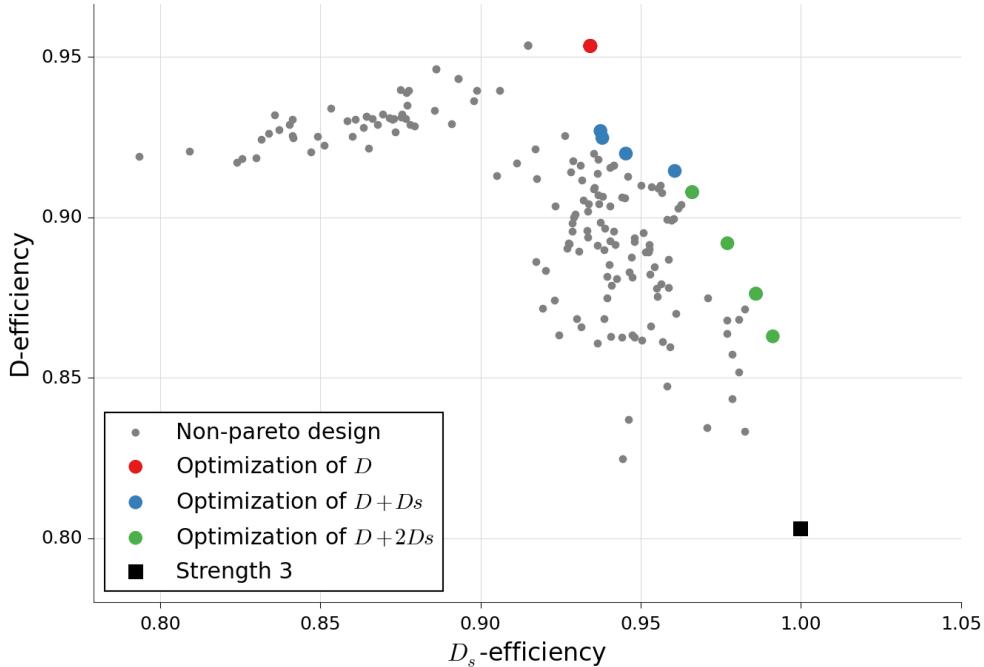


Fig. 1: Scatterplot for the D -efficiency and D_s -efficiency for generated designs in OA(40; 2; 2⁷). The Pareto optimal designs are colored, while the non-Pareto optimal designs are grey. For reference the strength-3 orthogonal array with highest D-efficiency is also included in the plot.

4.4 Even-odd arrays

The even-odd arrays are a special class of orthogonal arrays with at least one of the odd J_k -characteristics unequal to zero. More information on this class of designs will appear later.

NORMAL FORM OF ARRAYS

The Orthogonal Array package contains functions to reduce arrays and designs to canonical form with respect to some ordering. The default ordering for orthogonal arrays is the lexicographic ordering in columns [SEN10]. The default ordering for conference designs is the LMC0 ordering [SEG19]. Alternative orderings include the delete-one-factor projection ordering introduced in [Een13] or the even-odd ordering. For a given ordering of a set of arrays, the minimal element of all arrays in an isomorphism class defines a unique representative of that isomorphism class.

Specialized packages such as Nauty [McK81], [MP13] can also reduce arrays to their canonical form using state-of-the-art, graph-isomorphism methods. However, these methods do not take into account the special structure of the arrays and so, they cannot be tailored to create normal forms of a specific form.

5.1 Reduction to LMC normal form

The Orthogonal Array package implements theory and methods from the article [Complete enumeration of pure-level and mixed-level orthogonal arrays](#), Schoen et al. to reduce orthogonal arrays to their LMC normal form. The C++ function to perform the reduction is `reduceLMCform()`. An example on how to use this function is shown below.

```
>>> import oapackage
>>> oapackage.set_srand(1)
>>> array = oapackage.exampleArray(1, 0).selectFirstColumns(3)
>>> array = array.randomperm()
>>> print('input array:');
>>> array.transposed().showarraycompact()
input array:
1100010111010001
0101100110100011
0000001111101101
>>> reduced_array = oapackage.reduceLMCform(array)
>>> print('reduced array:');
>>> reduced_array.transposed().showarraycompact()
reduced array:
0000000011111111
0000111100001111
0001011101110001
```

It is also possible to check whether an array is in normal form with the `LMCcheck()` method:

```
>>> import oapackage
>>> array = oapackage.exampleArray(1)
>>> lmc_type = oapackage.LMCcheck(array)
>>> if lmc_type == oapackage.LMC_MORE:
...     print('array is in minimal form')
```

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```
... elif lmc_type == oapackage.LMC_LESS:  
...     print('array is not in minimal form')  
array is in minimal form
```

5.2 Reduction to delete-one-factor projection form

The article [A canonical form for non-regular arrays based on generalized word length pattern values of delete-one-factor projections](#) [Een13] describes a canonical form of an orthogonal array based on delete-one-factor projections. The C++ interface to delete-one-factor projection form is `reduceDOPform()`. The reduction method works well for large arrays with a large variation in the projection values.

An example on how to use this reduction is shown in [Example code for delete-one-factor projections](#), which can be found in the example notebooks section.

5.3 Reduction using graph isomorphisms

The function `reduceOAnauty()` reduces an orthogonal array to Nauty canonical form. To reduce general graphs to Nauty canonical form, the Orthogonal Array package includes the function `reduceGraphNauty()`.

Reduce a design to normal form using Nauty

```
>>> oapackage.set_srand(1)  
>>> al = oapackage.exampleArray(0).randomperm()  
>>> al.showarray()  
array:  
 0  0  
 0  1  
 1  1  
 0  1  
 1  0  
 0  0  
 1  0  
 1  1  
>>> transformation=oapackage.reduceOAnauty(al, 0)  
>>> transformation.show()  
array transformation: N 8  
column permutation: {0,1}  
level perms:  
{0,1}  
{0,1}  
row permutation: {0,5,1,3,4,6,2,7}  
>>> alr=transformation.apply(al)  
>>> alr.showarray()  
array:  
 0  0  
 0  0  
 0  1  
 0  1
```

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1	0
1	0
1	1
1	1

5.4 Normal forms for conference designs

For conference designs, a convenient normal form is the LMC0 ordering (sometimes also called L0 ordering) [SEG19].

LMC0 ordering

The LMC0 ordering for conference designs is defined in three steps:

Definition LMC0 i: Order of elements

The LMC0 order of the factor levels -1, 0 and +1 is $0 < +1 < -1$.

Definition LMC0 ii: Order of columns

A column a is smaller than a column b according to LMC0 ordering, notated as $a < b$, if either of the following conditions hold:

1. If we replace the values -1 by +1 in both columns, then the first element where the columns differ is smaller in a than in b according to Definition 1.
2. The zeros in column a are in the same position as the zeros in column b, and the first element where the columns differ is smaller in a than in b according to Definition i.

Definition LMC0 iii: Order of designs

Conference design A is smaller than conference design B according to LMC0 ordering, notated as $A < B$, if the first column where the designs differ is smaller in A than in B.

The definition implies that the ordering of designs is column-by-column and that the position of zeros in the columns is dominant over the values +1, -1. To check whether a design is in LMC0 form, we can use `LMC0check()`:

Conference design in normal form

```
>>> array = oapackage.exampleArray(53, 1)
exampleArray 53: third array in C(12,4)
>>> array.showarray()
array:
 0   1   1   1
 1   0  -1   1
 1   1   0  -1
 1   1   1  -1
 1   1   1  -1
 1   1  -1   1
 1   1  -1   1
 1  -1   1   0
 1  -1   1   1
 1  -1  -1   1
 1  -1  -1  -1
```

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```
1 -1 -1 -1
>>> oapackage.LMC0check(array) == oapackage.LMC_LESS
True
```

PROPERTIES OF DESIGNS

This section shows the structural and statistical properties of the orthogonal arrays, conference designs and D-efficient designs generated by the Orthogonal Array package. The properties of the arrays and designs are calculated using the `array_link` object or functions from the package.

6.1 Definitions of arrays and designs

Before introducing the structural and statistical properties, we define orthogonal arrays, conference designs and D-efficient designs:

An orthogonal array (OA) of strength t , N runs and n factors at s levels is an $N \times n$ array of symbols $0, \dots, (s - 1)$, such that for every subset of t columns, every t -tuple occurs equally often [Rao47]. The set of all strength- t OAs with N runs and n factors at s levels is denoted by $\text{OA}(N; t; s^n)$. If $s = 2$, the OA is called a two-level OA and the set of all strength- t two-level OAs with N runs and n factors is denoted as $\text{OA}(N; t; 2^n)$.

For N even, a conference design [SEG19] C is an $N \times n$ array which satisfies $C^T C = (n - 1)I_n$, with $C_{ii} = 0$ and $C_{ij} \in \{-1, 1\}$, for $i \neq j$ and $i, j = 1, \dots, n$. A $N \times N$ conference design E such that $EE^T = (n - 1)I_n$ is called a conference matrix; see [EN95], [CD06] and [XLB12].

A D-optimal design [DAT07] (X) is an $N \times n$ array which maximizes the D -efficiency, defined as $(\det(X_M^T X_M)^{1/p})/N$, for a given $N \times p$ model matrix X_M (for details see *Model matrices*). The Orthogonal Array package uses a coordinate-exchange algorithm to generate designs that optimize the D -efficiency. Since there is no guarantee that the resulting designs have the largest possible D -efficiency, we refer to them as D-efficient designs in this documentation. An orthogonal array is called D-optimal orthogonal array if it provides the largest D -efficiency among all comparable orthogonal arrays.

6.2 Structural properties of an array

The OApackage can calculate the rank of an array, defined as the maximum number of linearly independent column or row vectors in the array. The rank of an array is useful for several other functions in the package. For two-level arrays, the OApackage can also check if the arrays are foldover arrays. A two-level array is called a foldover array if half of its runs are mirror images of the other half, in the sense that the factor levels are changed from 0 to 1 and from 1 to 0.

For example, to calculate the rank of a two-level orthogonal array and determine whether the array is a foldover array, one can use the methods `array_link::rank()` and `array_link::foldover()`:

Calculate rank of array and test for foldover

```
>>> array = oapackage.exampleArray(1) # Select an example two-level orthogonal array
>>> array.showarray() # Show the two-level orthogonal array
array:
 0  0  0  0  0
 0  0  0  0  0
 0  0  0  1  1
 0  0  1  0  1
 0  1  0  1  0
 0  1  1  0  0
 0  1  1  1  1
 0  1  1  1  1
 1  0  0  1  1
 1  0  1  0  1
 1  0  1  1  0
 1  0  1  1  0
 1  1  0  0  1
 1  1  0  0  1
 1  1  0  1  0
 1  1  1  0  0
```

```
>>> print(array.rank()) # Calculate the rank of the array
5
>>> print(array.foldover()) # Determine if the array is foldover
False
```

Other structural properties such as whether an array involves two levels or is symmetric can be found in the documentation of [array_link](#), which shows the full set of methods available.

6.3 Model matrices

For orthogonal arrays and conference designs, the OApackage can calculate different model matrices. The model matrices available depend on the type of array and design.

Model matrices for two-level orthogonal arrays

For two-level orthogonal arrays, the levels of the array are first coded according to the map $0 \rightarrow -1$ and $1 \rightarrow +1$. The coded matrix is referred to as the design matrix. The main effect contrast vectors are given by the columns in the design matrix. The contrast vectors associated to the two-factor interactions are calculated by taking products between two different columns in the design matrix. The model matrix consists of the intercept column (i.e. a column of ones) and the contrast vectors associated to the main effects and, optionally, the two-factor interactions.

Model matrices for conference designs

The model matrix for a conference design consists of the intercept column (i.e. a column of ones) and the contrast vectors associated to the main effects and, optionally, the second-order effects (two-factor interactions and quadratic effects). The main effect contrast vectors are given by the columns in the conference design. The contrast vectors associated to the second-order effects are calculated by taking products between two columns in the conference design.

Model matrices for mixed-level orthogonal arrays

For mixed-level orthogonal arrays, the main effect contrast vectors are defined by the Helmert contrasts. The contrast vectors associated to the two-factor interactions are calculated by taking products between two different columns in the matrix containing the Helmert contrasts of the array; see Model matrices for mixed-level orthogonal arrays for details. The model matrix consists of the intercept column (i.e. a columns of ones) and the contrast vectors associated to the main effects and, optionally, the two-factor interactions.

An example on how to generate an interaction model matrix for a two-level orthogonal array is shown below.

Calculate interaction effects model matrix

```
>>> array=oapackage.exampleArray(0,1)
exampleArray 0: array in OA(8,2, 2^2)
>>> array.showarray()
array:
 0  0
 0  0
 0  1
 0  1
 1  0
 1  0
 1  1
 1  1
>>> M=oapackage.array2modelmatrix(array, 'i')
>>> print(M)
[[ 1. -1. -1.  1.]
 [ 1. -1. -1.  1.]
 [ 1. -1.  1. -1.]
 [ 1. -1.  1. -1.]
 [ 1.  1. -1. -1.]
 [ 1.  1. -1. -1.]
 [ 1.  1.  1.  1.]
 [ 1.  1.  1.  1.]]
```

6.4 Statistical properties of orthogonal arrays

Orthogonal arrays are commonly evaluated in terms of their generalized wordlength pattern [XW01] (GWLP). Two-level OAs are also commonly evaluated in terms of their J_k -characteristics and F -vectors [DT99]. The OApakcage can calculate all these statistical criteria: `array_link::GWLP()`, `array_link::Fvalues()`, `array_link::Jcharacteristics()`.

The following example shows how to calculate the GWLP, F_k -values and J_k -characteristics from an `array_link` object:

Calculate GWLP and F-values

```

>>> al=oapackage.exampleArray(1,1) # Select an example array
exampleArray 1: array 3 in OA(16, 2, 2^5)
>>> gwlp = al.GWLP() # Calculate its generalized word length pattern
>>> print('GWLP: %s' % str(gwlp) )
GWLP: (1.0, 0.0, 0.0, 1.0, 1.0, 0.0)
>>> print('F3-value: %s' % str(al.Fvalues(3))) # Calculate the F_3 values
F3-value: (4, 6)
>>> print('F4-value: %s' % str(al.Fvalues(4))) # Calculate the F_3 values
F4-value: (1, 4)
>>> print('J3-characteristics: %s' % str(al.Jcharacteristics(3))) # Calculate the J_3-
    ↵characteristics
J3-characteristics: (-8, -8, 0, 0, 0, -8, 0, -8, 0, 0)
    
```

We now briefly mention some technical details of the J_k -characteristics, the F_k -values and the GWLP.

J_k -characteristics

To calculate J_k -characteristics of a two-level OA, the OApakage codes the levels of the array as -1 and $+1$. To this end, the package uses the mapping $0 \rightarrow -1$ and $1 \rightarrow +1$. Let D be an $N \times n$ with coded levels -1 and $+1$. For $S = \{l_1, \dots, l_k\}$, a subset of k different factors of $D = (d_{il})$, define

$$j_k(S; D) = \sum_{i=1}^N d_{il_1} \cdots d_{il_k}.$$

The $|j_k(S; D)|$ values are called the J_k -characteristics, which necessarily equal $N - 4q$ [DT02], where $q \leq N/4$ is a non-negative integer.

F_k -values

The F_k -vector collects the frequencies of all the J_k -characteristics. More specifically, the vector $F_k = (f_{k1}, \dots, f_{kv})$, where $v = N/4$ and f_{ku} denotes the frequency of the J_k -characteristics which are equal to $4(v + 1 - u)$. When calculating an F_k -vector, the OApakage shows only the vector (f_{k1}, \dots, f_{kv}) , whose elements are referred to as the F_k -values.

Generalized word length pattern

Consider an OA, D , of strength t with N runs and n factors at s levels. Let X_0 be a column of ones, X_1 the matrix involving the contrast vectors associated with the main effects, and X_j the matrix involving the contrast vectors associated with the j -factor interactions, $j \geq 2$. We assume that the column vectors in X_1 are normalized so that they have the same length \sqrt{N} . For $j = 0, \dots, n$, let

$$A_j(D) = N^{-2} 1_N^T X_j X_j^T 1_N,$$

where 1_N denotes the $N \times 1$ column of ones. The value of $A_j(D)$ is invariant to the choice of the orthonormal contrasts used; see [XW01] for details. The vector $(A_0(D), \dots, A_n(D))$ is called the generalized word length pattern (GWLP). To increase the speed of the computations for the GWLP, the OApakage uses the distance distribution and the MacWilliams identities as in [XW01] and [Xu09].

6.5 Optimality criteria for D-efficient designs

In [ES17], D-efficient designs for the model including the intercept, all main effects and all two-factor interactions are generated. The OApakage provides functionality to compute the optimality criteria used to generate the D-efficient designs in [ES17]. Moreover, the package can calculate the well-known A - and E -optimality criteria from the literature on Optimal Experimental Design [DAT07]. The functions to perform the calulations are `array_link::Defficiency()`, `array_link::DsEfficiency()`, `array_link::Aefficiency()`, `array_link::Eefficiency()`.

The following example shows how to calculate the D -, D_s -, A - and E -efficiency for a design that permits the estimation of the interaction model.

Calculate optimality criteria for D-efficient designs

```
# Select an array that can estimate the interaction model
>>> al = oapackage.exampleArray(11, 1)
exampleArray 11: D-optimal array in OA(44, 2^8)
>>> print('D-efficiency: %.4f' % al.Defficiency())
D-efficiency: 0.8879
>>> print('Ds-efficiency (Eendebak and Schoen, 2017): %.4f' % al.DsEfficiency())
Ds-efficiency (Eendebak and Schoen, 2017): 0.8059
>>> print('A-efficiency for the interaction model: %.4f' % al.Aefficiency())
A-efficiency for the interaction model: 0.7906
>>> print('E-efficiency for the interaction model: %.4f' % al.Eefficiency())
E-efficiency for the interaction model: 0.3602
```

Calculation of D -, A - and E -efficiency

Let X be again the $N \times p$ interaction model matrix (see section [Model matrices](#)) consisting of a column of ones and the contrast vectors associated to the main and two-factor interactions of n factors, where $p = 1 + n + (n)(n - 1)/2$. The D -, A - and E -efficiency are calculated using the eigenvalues of the singular-value decomposition (SVD) of X . To calculate the rank of a matrix, the lower-upper (LU) decomposition, as implemented in the Eigen package [GJ+10], is used.

Let $\lambda_1, \dots, \lambda_p$ be the eigenvalues of the SVD of X . The OApakage calculates the D -, A - and E -efficiency of a design D as follows:

$$\begin{aligned} D_{\text{eff}}(D) &= (\prod_j \lambda_j)^{1/p} / N, \\ A_{\text{eff}}(D) &= N(\sum_j \lambda_j^{-1}) / m, \\ E_{\text{eff}}(D) &= \min_j \lambda_j. \end{aligned}$$

D_s -efficiency and D_1 -efficiency

In [ES17], the D_s -efficiency is used to assess the joint precision of the main effects in the interaction model. Let the interaction model matrix X be split into X_1 , containing the contrast vectors associated with the main effects only, and X_{02} , containing the intercept column and the contrast vectors

associated to the two-factor interactions. The D_s -criterion of a design D is defined as

$$D_{s,\text{crit}}(D) = \det(X^T X) / \det(X_{02}^T X_{02}),$$

where X_{02} is necessarily of full rank. Similar to the calculations of the D -efficiency, the OApackage calculates the D_s -criterion using the eigenvalues of the SVD of the matrices X and X_{01} . Finally, the package calculates the D_s -efficiency of D as $D_{s,\text{eff}}(A) = D_{s,\text{crit}}(A)^{1/m}$, where m is the number of factors.

In a similar way the D_1 -efficiency of a design A with n factors and model matrix of intercept and main effects X_{01} , is defined as

$$D_{1,\text{eff}}(A) = (\det((X_{01})^T (X_{01})))^{1/(n+1)}$$

6.6 Projection capacities

Other relevant statistical criteria to evaluate a two-level design with N runs and k factors include the so-called projection estimation capacity (PEC) and projection information capacity (PIC) [LST07]. These criteria focus on the projections of the two-level design onto a smaller number of factors. More specifically, the PEC and PIC summarize the performance of all the N -run subdesigns with $l \leq k$ factors in terms of the capacity to estimate the interaction model and the D -efficiency for this model, respectively.

The PEC and PIC are based on the so-called PEC and PIC sequences, which are formally defined as follows. Let PEC_l denote the proportion of N -run l -factor subdesigns that permit the estimation of the interaction model in l factors, that is, the model including the intercept, all l main effects and all $l(l - 1)/2$ two-factor interactions. The PEC sequence is the vector $(PEC_1, PEC_2, \dots, PEC_k)$. Now, let PIC_l denote the average D -efficiency for the interaction model in l factors across all N -run l -factor subdesigns. The PIC sequence is the vector $(PIC_1, PIC_2, \dots, PIC_k)$. The OApackage can calculate the PEC and PIC sequences of two-level designs with `PECsequence()` and `PICsequence()`, respectively.

The following example shows how to compute the PEC and PIC sequences of a two-level orthogonal array using the OApackage.

Calculate the PEC and PIC sequences

```
>>> al=oapackage.exampleArray(1,1)
exampleArray 1: array 3 in OA(16, 2, 2^5)
>>> PEC = al.PECsequence()
>>> print('PEC sequence: %s'% ','.join(['%.2f' % x for x in PEC]) )
PEC sequence: 1.00,1.00,1.00,0.80,0.00
>>> PIC = al.PICsequence()
>>> print('PIC sequence: %s'% ','.join(['%.2f' % x for x in PIC]) )
PIC sequence: 1.00,1.00,0.95,0.66,0.00
```

6.7 Properties of conference designs

In [SEG19], it is shown that the F_4 vector is useful for classifying definitive screening designs [XLB12] that are generated by folding over a conference design. To calculate the F_4 vector, we first need to compute the J_4 -characteristics of the conference design. The calculations for the J_k -characteristics of conference designs are similar as for orthogonal arrays; see *Statistical properties of orthogonal arrays*. Consider a definitive screening design constructed from an N -run conference design with at least four factors. The F_4 vector of this design collects the frequencies of the J_4 -characteristics of $2N8\lambda$ for $\lambda = 1, \dots, N/4$ when N is a multiple of 4, or $\lambda = 1, \dots, (N^2)/4$ when N is an odd multiple of 2.

Note: the J_4 -values of a definitive screening design generated by folding over a conference design are twice the value of the J_4 -values of the conference design. The F_4 vector of a conference design and the corresponding definitive screening design are equal.

Calculate the F4 vector for a conference design

```
>>> import oapackage
>>> array=oapackage.exampleArray(47, 1)
exampleArray 47: third conference design in C(20,8)
>>> F4=array.FvaluesConference(4)
>>> print(F4)
(0, 2, 4, 51, 13)
>>> definitive_screening_design = oapackage.conference2DSD(array)
```

The individual J_k -characteristics can be calculated with the method `Jcharacteristics_conference()`. For conference designs, we can calculate the projection statistics using `conferenceProjectionStatistics()`.

Calculate projection statistics for conference designs

```
>>> array = oapackage.exampleArray(46, 1)
exampleArray 46: second conference design in C(20,8)
>>> pec, pic, ppc = oapackage.conference.conferenceProjectionStatistics(array)
>>> print('Projection estimation capacity for 4 columns: %.3f' % pec)
Projection estimation capacity for 4 columns: 0.986
>>> J3 = oapackage.Jcharacteristics_conference(array, number_of_columns = 3)
```


C++ LIBRARY

The full documentation for the C++ library can be build from the source code using [doxygen](#). For convenience we provide links the main functions on this page.

7.1 Interface for D-optimal designs

Contains functions to generate optimal designs.

For more information see “Two-Level Designs to Estimate All Main Effects and Two-Factor Interactions”, P.T. Eendebak and E.D. Schoen, 2017

Enums

enum **coordinate_exchange_method_t**

Different methods for the optimization. The default method DOPTIM_SWAP is a coordinate-exchange algorithms.

Values:

enumerator **DOPTIM_UPDATE**

replace a random element with a random value

enumerator **DOPTIM_SWAP**

swap two elements at random

enumerator **DOPTIM_FLIP**

randomly flip an element between 0 and 1

enumerator **DOPTIM_AUTOMATIC**

automatically select one of the methods

enumerator **DOPTIM_NONE**

perform no optimization

Functions

`double scoreD(const std::vector<double> efficiencies, const std::vector<double> weights)`

Calculate score from a set of efficiencies

The score is the weighted sum of the efficiencies.

Parameters

- **efficiencies** – Vector with calculated efficiencies
- **weights** – Weights for the efficiencies

Returns

Weighted sum of the efficiencies

DoptimReturn `Doptimize`(const *arraydata_t* &*arrayclass*, int *nrestarts*, const std::vector<double> *alpha*, int *verbose*,
coordinate_exchange_method_t *method* = DOPTIM_AUTOMATIC, int *niter* = 300000,
double *maxtime* = 100000, int *nabort* = 5000)

Generates optimal designs for the specified class of designs

The method uses a coordinate-exchange algorithm to optimize a target function defined by the optimization parameters. The optimization is performed multiple times to prevent finding a design in a local minimum of the target function.

The method is described in more detail in “Two-Level Designs to Estimate All Main Effects and Two-Factor Interactions”, Eendebak et al., 2015, Technometrics, <https://doi.org/10.1080/00401706.2016.1142903>.

Parameters

- **arrayclass** – Class of designs to optimize
- **nrestarts** – Number of restarts to perform
- **alpha** – Optimization parameters. The target function is alpha_1 D + alpha_2 D_s + alpha_D_1
- **verbose** – Verbosity level
- **method** – Method for optimization algorithm
- **niter** – Maximum number of iterations for each restart
- **maxtime** – Maximum calculation time. If this time is exceeded, the function is aborted
- **nabort** – Maximum number of iterations when no improvement is found

Returns

A structure with the generated optimal designs

DoptimReturn `DoptimizeMixed`(const *arraylist_t* &*sols*, const *arraydata_t* &*arrayclass*, const std::vector<double> *alpha*, int *verbose* = 1, int *nabort* = -1)

Function to generate optimal designs with mixed optimization approach

This function is beta code. See Doptimize for details of the parameters.

array_link `optimDef`(const *array_link* &*array*, const *arraydata_t* &*arrayclass*, std::vector<double> *alpha*, int *verbose* = 1, *coordinate_exchange_method_t* *optimmethod* = DOPTIM_AUTOMATIC, int *niter* = 100000, int *nabort* = 0)

Optimize a design according to the optimization function specified.

Arguments:

Parameters

- **array** – Array to be optimized
- **arrayclass** – Structure describing the design class
- **alpha** – 3x1 array with optimization parameters
- **verbose** – Verbosity level
- **optimmethod** – Optimization method to use
- **niter** – Number of iterations
- **nabort** – Number of iterations after which to abort when no improvements are found

Returns

Optimized designs

struct **DoptimReturn**

#include <Deff.h> Structure containing results of the Doptimize function

Public Members

std::vector<std::vector<double>> **dds**

calculated efficiencies for the generated designs

arraylist_t **designs**

designs generated

int **nrestarts**

number of restarts performed

int **_nimproved**

7.2 Interface for array properties

Contains functions to calculate properties of arrays.

Author: Pieter Eendebak pieter.eendebak@gmail.com Copyright: See LICENSE.txt file that comes with this distribution

Defines

GWLValue

TypeDefs

typedef mvalue_t<double> **DOFvalue**
delete-one-factor projection value

Enums

enum **model_matrix_t**

Values:

enumerator **MODEL_CONSTANT**

only the intercept

enumerator **MODEL_MAIN**

intercept and main effects

enumerator **MODEL_INTERACTION**

intercept, main effects and second order interactions

enumerator **MODEL_SECONDORDER**

intercept, main effects and second order effects(interactions and quadratic effects)

enumerator **MODEL_INVALID**

invalid model

enum **paretomethod_t**

Values:

enumerator **PARETOFUNCTION_DEFAULT**

enumerator **PARETOFUNCTION_J5**

Functions

void **DAEfficiencyWithSVD**(const Eigen::MatrixXd &secondorder_interaction_matrix, double &Deff, double
&vif, double &Eeff, int &rank, int verbose)

Calculate D-efficiency and VIF-efficiency and E-efficiency values using SVD.

int **array2rank_Deff_Beff**(const *array_link* &al, std::vector<double> *ret = 0, int verbose = 0)

Calculate the rank of the second order interaction matrix of an orthogonal array

The model is the intercept, main effects and interaction effects The rank, D-efficiency, VIF-efficiency and E-efficiency are appended to the second argument

The return vector is filled with the rank, Defficiency, VIF efficiency and Eefficiency

`double Defficiency(const array_link &orthogonal_array, int verbose = 0)`

Calculate D-efficiency for a 2-level array using symmetric eigenvalue decomposition.

`std::vector<double> Deficiencies(const array_link &array, const arraydata_t &arrayclass, int verbose = 0, int addDs0 = 0)`

Calculate efficiencies for an array

Parameters

- **array** – Array to use in calculation
- **arrayclass** – Specification of the array class
- **verbose** – Verbosity level
- **addDs0** – If True, then add the Ds0-efficiency to the output

Returns

Vector with the calculate D-efficiency, the main effect robustness (or Ds-optimality) and D1-efficiency for an orthogonal array

`double VIFefficiency(const array_link &orthogonal_array, int verbose = 0)`

Calculate VIF-efficiency of matrix.

`double Aefficiency(const array_link &orthogonal_array, int verbose = 0)`

Calculate A-efficiency of matrix.

`double Eefficiency(const array_link &orthogonal_array, int verbose = 0)`

Calculate E-efficiency of matrix (1 over the VIF-efficiency)

`std::vector<double> Aefficiencies(const array_link &orthogonal_array, int verbose = 0)`

calculate various A-efficiencies

`std::vector<double> projDeff(const array_link &array, int number_of_factors, int verbose = 0)`

Calculate D-efficiencies for all projection designs

Parameters

- **array** – Design to calculate D-efficiencies for
- **number_of_factors** – Number of factors into which to project
- **verbose** – Verbosity level

Returns

Vector with calculated D-efficiencies

`std::vector<double> PECsequence(const array_link &array, int verbose = 0)`

Calculate the projection estimation capacity sequence for a design

The PECK of a design is the fraction of estimable second-order models in k factors. The vector (PEC1, PEC2, ...,) is called the projection estimation capacity sequence. See “Ranking Non-regular Designs”, J.L. Loeppky, 2004.

Parameters

- **array** – Input array
- **verbose** – Verbosity level

Returns

Vector with the caculated PEC sequence

```
std::vector<double> PICsequence(const array_link &array, int verbose = 0)
```

Calculate the projection information capacity sequence for a design.

The PIC_k of a design is the average D-efficiency of estimable second-order models in k factors. The vector (PIC₁, PIC₂, ...,) is called the PIC sequence.

Parameters

- **array** – Input array
- **verbose** – Verbosity level

Returns

Vector with the caculated PIC sequence

```
ndarray<double> macwilliams_transform_mixed(const ndarray<double> &B, int N, const std::vector<int> &factor_levels_for_groups, int verbose = 0)
```

Calculate MacWilliams transform.

Calculate MacWilliams transform for mixed level data.

Parameters

- **B** – Input array
- **N** –
- **verbose** – Verbosity level
- **factor_levels_for_groups** – Factor levels for the groups
- **B** – Input array
- **N** – Number of runs
- **factor_levels_for_groups** – Factor levels
- **verbose** – Verbosity level

Returns

MacWilliams transform of the input array

Returns

Transform if the input array

```
std::vector<double> distance_distribution(const array_link &array)
```

Return the distance distribution of a design

The distance distribution is described in “Generalized minimum aberration for asymmetrical fractional factorial designs”, Wu and Xu, 2001

Parameters

a1 – Array for which to calculate the distribution

Returns

Distance distribution

```
std::vector<int> distance_distribution_shape(const arraydata_t arrayclass)
```

Return shape of distance distribution for mixed level design

Parameters

arrayclass – Specification of the array class

Returns

Shape of the distance distribution

```
ndarray<double> distance_distribution_mixed(const array_link &array, int verbose = 0)
```

Return the distance distribution of a mixed-level design

The distance distribution is described in “Generalized minimum aberration for asymmetrical fractional factorial designs”, Wu and Xu, 2001. For mixed-level designs more details can be found in “A canonical form for non-regular arrays based on generalized wordlength pattern values of delete-one-factor projections”, Eendebak, 2014.

Parameters

- **al** – Array for which to calculate the distribution
- **verbose** – Verbosity level

Returns

Distance distribution

```
void distance_distribution_mixed_inplace(const array_link &al, ndarray<double> &B, int verbose = 0)
```

template<class **Type**>

```
std::vector<double> macwilliams_transform(std::vector<Type> B, int N, int s)
```

Calculate MacWilliams transform.

```
std::vector<int> Jcharacteristics(const array_link &array, int number_of_columns = 4, int verbose = 0)
```

Calculate Jk-characteristics of a matrix

The calculated Jk-values are signed.

Parameters

- **array** – Array to calculate Jk-characteristics for
- **number_of_columns** – Number of columns
- **verbose** – Verbosity level

Returns

Vector with calculated Jk-characteristics

```
std::vector<double> GWLP(const array_link &array, int verbose = 0, int truncate = 1)
```

Calculate GWLP (generalized wordlength pattern)

The method used for calculation is from Xu and Wu (2001), “Generalized minimum aberration for asymmetrical fractional factorial desings”. For non-symmetric arrays see “Algorithmic Construction of Efficient Fractional Factorial Designs With Large Run

Sizes”, Xu, Technometrics, 2009.

A more detailed description of the generalized wordlength pattern can also be found in the documentation at <https://oapackage.readthedocs.io/>.

Parameters

- **array** – Array to calculate the GWLP value for
- **verbose** – Verbosity level
- **truncate** – If True then round values near zero to solve double precision errors

Returns

Vector with calculated generalized wordlength pattern

`std::vector<double> GWLPmixed(const array_link &array, int verbose = 0, int truncate = 1)`

Calculate GWLP (generalized wordlength pattern) for mixed-level arrays.

The method used for calculation is from “Algorithmic Construction of Efficient Fractional Factorial Designs With Large Run Sizes”, Xu, Technometrics, 2009.

Parameters

- **array** – Array to calculate the GWLP value for
- **verbose** – Verbosity level
- **truncate** – If True then round values near zero to solve double precision errors

Returns

Vector with calculated generalized wordlength pattern

`std::vector<GWLPvalue> projectionGWLPs(const array_link &al)`

calculate delete-one-factor GWLP (generalized wordlength pattern) projections

`std::vector<GWLPvalue> sortGWLP(std::vector<GWLPvalue>)`

sort a list of GWLP values and return the sorted list

`double CL2discrepancy(const array_link &array)`

Calculate centered L2-discrepancy of a design

The method is from “A connection between uniformity and aberration in regular fractions of two-level factorials”, Fang and Mukerjee, 2000

`array_link array2secondorder(const array_link &array)`

Calculate second order interaction model for 2-level array

Parameters

array – Array to calculate second order interaction model from

Returns

Array interaction effects

`array_link array2xf(const array_link &array)`

calculate second order interaction model for 2-level array

Parameters

array – Array to calculate second order interaction model from

Returns

Array with intercept, main effects and interaction effects

`array_link conference_design2modelmatrix(const array_link &conference_design, const char *mode, int verbose = 0)`

Calculate model matrix for a conference design

Parameters

- **conference_design** – Conference design
- **mode** – Can be ‘m’ for main effects, ‘i’ for interaction effects or ‘q’ for quadratic effects

- **verbose** – Verbosity level

Returns

Calculated model matrix

Eigen::MatrixXd **array2modelmatrix**(const *array_link* &array, const char *mode, int verbose = 0)

Convert orthogonal array or conference design to model matrix

The model matrix consists of the intercept, main effects and (optionally) the interaction effects and quadratic effects. The order in the interaction effects is (c1, c2)=(0,0), (1,0), (2,0), (2,1), ... with c2<c1 for columns c1, c2. The size of the model matrix calculated by this function is given by *array2modelmatrix_sizes*.

For conference designs the method *conference_design2modelmatrix* is used. For orthogonal array the calculated is performed with *array2eigenModelMatrixMixed*.

Parameters

- **array** – Orthogonal array or conference design
- **mode** – Type of model matrix to calculate. Can be ‘m’ for main effects, ‘i’ for interaction effects or ‘q’ for quadratic effects
- **verbose** – Verbosity level

Returns

Calculated model matrix

std::vector<int> **array2modelmatrix_sizes**(const *array_link* &array)

Return the sizes of the model matrices calculated

Parameters

array – Orthogonal array or conference designs

Returns

List with the sizes of the model matrix for: only intercept; intercept, main; intercept, main, and interaction terms, intercept, main and full second order

Eigen::MatrixXd **array2xfeigen**(const *array_link* &array)

calculate second order interaction model for 2-level array

Parameters

array – Array to calculate second order interaction model from

Returns

Array with intercept, main effects and interaction effects

int **arrayrankFullPivQR**(const *array_link* &al, double threshold = -1)

return rank of an array based on Eigen::FullPivHouseholderQR

int **arrayrankColPivQR**(const *array_link* &al, double threshold = -1)

return rank of an array based on Eigen::ColPivHouseholderQR

int **arrayrankFullPivLU**(const *array_link* &al, double threshold = -1)

return rank of an array based on Eigen::FullPivLU

int **arrayrankSVD**(const *array_link* &al, double threshold = -1)

return rank of an array based on Eigen::JacobiSVD

int **arrayrank**(const *array_link* &array)

calculate the rank of an array

```
int arrayrankInfo(const Eigen::MatrixXd&, int verbose = 1)
    Return rank of an array. Information about the different methods for rank calculation is printed to stdout.

int arrayrankInfo(const array_link &array, int verbose = 1)
    Return rank of an array. Information about the different methods for rank calculation is printed to stdout.

Eigen::MatrixXd arraylink2eigen(const array_link &array)
    convert array_link to Eigen matrix

double conditionNumber(const array_link &matrix)
    Return the condition number of a matrix.

void calculateParetoEvenOdd(const std::vector<std::string> infiles, const char *outfile, int verbose = 1,
                            arrayfilemode_t afmode = ABINARY, int nrows = -1, int ncols = -1,
                            paretomethod_t paretomethod = PARETOFUNCTION_DEFAULT)
    Calculate the Pareto optimal arrays from a list of array files

    Pareto optimality is calculated according to (rank; A3,A4; F4)

Pareto<mvalue_t<long>, long> parsePareto(const arraylist_t &arraylist, int verbose, paretomethod_t
                                             paretomethod = PARETOFUNCTION_DEFAULT)

mvalue_t<long> A3A4(const array_link &al)
    calculate A3 and A4 value for array

Parameters
    a1 – Array for which to calculate A3 and A4

Returns
    Object with A3 and A4

inline mvalue_t<long> F4(const array_link &al, int verbose = 1)
    calculate F4 value for 2-level array

template<class IndexType>
Pareto<mvalue_t<long>, IndexType>::pValue calculateArrayParetoRankFA(const array_link &array, int
                                                                     verbose)
    Calculate properties of an array and create a Pareto element

    The values calculated are:
        1) Rank (higher is better) 2) A3, A4 (lower is better) 3) F4 (lower is better, sum of elements is constant)

    Valid for 2-level arrays of strength at least 3

template<class IndexType>
void addJmax(const array_link &al, typename Pareto<mvalue_t<long>, IndexType>::pValue &p, int verbose = 1)
    add Jmax criterium to Pareto set

template<class IndexType>
Pareto<mvalue_t<long>, IndexType>::pValue calculateArrayParetoJ5(const array_link &al, int verbose)
    Calculate Pareto element with J5 criterium.

template<class IndexType>
inline void parseArrayPareto(const array_link &array, IndexType i, Pareto<mvalue_t<long>, IndexType> &pset,
                           int verbose)
    Add array to list of Pareto optimal arrays

    The values to be optimized are:
        1) Rank (higher is better) 2) A3, A4 (lower is better) 3) F4 (lower is better, sum of elements is constant)
```

```
inline double Cvalue2Dvalue(double Cvalue, int number_of_columns)
    convert C value to D-efficiency value
inline double Dvalue2Cvalue(double Defficiency, int number_of_columns)
    convert D-efficiency value to C value
template<class Type>
class ndarray
    #include <arrayproperties.h> Class representing an n-dimensional array
    The data is stored in a flat array. The dimensions are stored in a vector dims.
```

Public Functions

```
inline ndarray(const std::vector<int> dims)
    Class represensing an n-dimensional array.

Parameters
dims – Dimension of the array

inline ndarray(const ndarray<Type> &rhs)
    Copy constructor Copies the internal data

inline ~ndarray()

inline void initialize(const Type value)
    Initialize array with specified value.

inline int sizeof_type() const
    Return size of ndarray template type.

inline bool type_is_floating_point() const
    Return True is the data type is of floating point type.

inline void info() const

inline std::string idxstring(int linear_idx) const
    Convert linear index to string representing the index.

inline long totalsize() const
    size of the array (product of all dimensions)

inline void show() const
    print the array to stdout

inline void linear2idx(int ndx, int *nidx = 0) const
    convert a linear index to normal indices

inline void linear2idx(int ndx, std::vector<int> &nidx) const
    convert a linear index to normal indices

inline int getlinearidx(int *idx) const
    From an n-dimensional index return the linear index in the data.

inline void *data_pointer() const
    Return pointer to data.
```

```
inline void setconstant(Type val)
    set all values of the array to specified value

inline void set(int *idx, Type val)
    set value at position

inline void setlinear(int idx, Type val)
    set value using linear index

inline Type getlinear(int idx) const
    get value using linear index

inline Type get(int *idx) const
    get value using n-dimensional index
```

Public Members

Type ***data**

std::vector<int> **dims**

int **k**

dimensions of the array

int **n**

std::vector<int> **cumdims**

std::vector<int> **cumprod**

Private Functions

inline void **initialize_internal_structures**(const std::vector<int> dimsx)

 Initialize internal structures

 Data pointer is created, but not set with data

Parameters

dimsx – Dimensions of the array

class **rankStructure**

#include <arrayproperties.h> Structure to efficiently calculate the rank of the second order interaction matrix of many arrays

The efficiency is obtained if the arrays share a common subarray. The theory is described in “Efficient rank calculation for matrices with a common submatrix”, Eendebak, 2016

Public Types

typedef Eigen::FullPivHouseholderQR<Eigen::MatrixXd> **EigenDecomp**

Public Functions

```
inline rankStructure(const array_link &al, int nsub = 3, int verbose = 0)
    constructor

inline rankStructure(int nsub = 3, int id = -1)
    constructor

void info() const
    print information about the rank structure

void updateStructure(const array_link &al)
    update the structure cache with a new array

int rankdirect(const Eigen::MatrixXd &array) const
    calculate the rank of an array directly, uses special threshold

int rankxfdirect(const array_link &array) const
    calculate the rank of the second order interaction matrix of an array directly

int rankxf(const array_link &array)
    calculate the rank of the second order interaction matrix of an array using the cache system
```

Public Members

array_link **absub**

int **r**

int **verbose**

verbosity level

int **ks**

number of columns of subarray in cache

int **nsub**

number of columns to subtract from array when updating cache

int **id**

used for debugging

Private Members

EigenDecomp **decomp**
decomposition of subarray

Eigen::MatrixXd **Qi**

long **ncalc**
internal structure

long **nupdate**

7.3 Interface for array tools

Contains the *array_link* class and related classes.

This file contains method and classes to work with (orthogonal) arrays.

Author: Pieter Eendebak pieter.eendebak@gmail.com Copyright: See LICENSE.txt file that comes with this distribution

Defines

MPI_ARRAY_T

Typedefs

typedef Eigen::MatrixXd **MatrixFloat**

typedef Eigen::ArrayXd **ArrayFloat**

typedef Eigen::VectorXd **VectorFloat**

typedef double **eigenFloat**

typedef short int **array_t**
data type for elements of orthogonal arrays

typedef const short int **carray_t**
constant version of array_t

typedef short int **rowindex_t**

```
typedef int colindex_t
    type used for row indexing

typedef const int const_colindex_t
    type used for column indexing

typedef array_t *array_p
    pointer to array
    constant version of type used for column indexing

typedef carray_t *carray_p
    pointer to constant array

typedef rowindex_t *rowperm_t

typedef colindex_t *colperm_t
    type of row permutation

typedef array_t *levelperm_t
    type of column permutation

typedef int vindex_t
    type of level permutation

typedef signed char conf_t
    data type for elements of conference designs

typedef std::vector<conf_t> conference_column
    data type for column of a conference design

typedef std::vector<conference_column> conference_column_list
    list of columns of conference designs

typedef std::deque<array_link> arraylist_t
    container with arrays
```

Enums

```
enum ordering_t
    Values:

        enumerator ORDER_LEX
            lexicograph minimal by columns ordering
```

enumerator **ORDER_J5**

J5 based ordering.

Functions

void **throw_runtime_exception**(const std::string exception_message)

void **eigenInfo**(const *MatrixFloat* m, const char *str = "eigen", int verbose = 1)

Print information about an Eigen matrix

Parameters

- **m** – Matrix about which to print information
- **str** – String to prepend in output
- **verbose** – Verbosity level

void **print_eigen_matrix**(const *MatrixFloat* matrix)

Print Eigen matrix to stdout

void **eigen2numpyHelper**(double *pmat1, int n, const *MatrixFloat* &m)

int **sizeof_array_t**()

return size in bytes of array_t type

int **sizeof_double**()

return size in bytes of double type

inline std::vector<int> **possible_F_values**(int N, int strength)

possible values for J-values of 2-level design

bool **file_exists**(const std::string filename)

return true if the specified file exists

bool **file_exists**(const char *filename)

return true if the specified file exists

bool **oa_file_exists**(const char *filename)

return true if the specified oa file exists

bool **oa_file_exists**(const std::string filename)

return true if the specified oa file exists

arraydata_t ***readConfigFile**(const char *file)

Read array configuration from file.

inline void **copy_array**(const *array_t* *src, *array_t* *const dst, const int nrows, const int ncols)

Make a copy of an array.

inline int **destroy_array**(*array_t* *array)

Delete an array.

Parameters

array –

Returns

static inline `array_t` ***create_array**(const int nrows, const int ncols)

Create an array.

Parameters

- **nrows** – Number of rows
- **ncols** – Number of columns

Returns

inline `array_t` ***create_array**(const `arraydata_t` *ad)

Create an array from an `arraydata_t` structure.

inline `array_t` ***clone_array**(const `array_t` *const array, const `rowindex_t` nrows, const `colindex_t` ncols)

Clone an array.

int **compareLMC**(const `array_link` &lhs, const `array_link` &rhs)

Return -1 if the first array is smaller in LMC ordering than the second array, 0 if equal and 1 otherwise

`array_link` **exampleArray**(int idx = 0, int verbose = 0)

Return example array

Parameters

- **idx** – Index of example array to return
- **verbose** – If True, then print information about the array to stdout

std::vector<int> **Jcharacteristics_conference**(const `array_link` &array, int number_of_columns, int verbose = 0)

Calculate Jk-characteristics for a conference design

Parameters

- **array** – Conference design
- **number_of_columns** – Specifies the number of columns to use
- **verbose** – Verbosity level

Returns

A vector of calculated inner products between all combinations of k columns.

`array_link` **hstack**(const `array_link` &array1, const `array_link` &array2)

concatenate 2 arrays in vertical direction

concatenate 2 arrays in horizontal direction

`array_link` **hstack**(const `array_link` &array, const `conference_column` &column)

concatenate array and conference_column

`array_link` **hstacklastcol**(const `array_link` &A, const `array_link` &B)

concatenate the last column of array B to array A

`conference_column` **vstack**(const `conference_column` &column_top, const `conference_column` &column_bottom)

concatenate two columns

void **perform_column_permutation**(const `array_link` source, `array_link` &target, const std::vector<int> perm)

perform column permutation for an array

void **perform_row_permutation**(const `array_link` source, `array_link` &target, const std::vector<int> perm)

perform row permutation for an array

`arraydata_t arraylink2arraydata(const array_link &array, int extracols = 0, int strength = 2)`

create `arraydata_t` structure from array

Parameters

- **array** – Array to use as input specification for array class
- **extracols** – Number of extra columns to add to the number of columns of the array
- **strength** – Strength to set in the array class. If -1, then use the strength of the array

`arraylist_t addConstant(const arraylist_t &lst, int value)`

add a constant value to all arrays in a list

`std::vector<int> getJcounts(arraylist_t *arraylist, int N, int k, int verbose = 1)`

Return number of arrays with $j_{\{2n+1\}}=0$ for $\text{number_of_arrays} < m$

`void create_root(array_t *array, const arraydata_t *arrayclass)`

set first columns of an array to root form

`void create_root(const arraydata_t *arrayclass, arraylist_t &solutions)`

Creates the root of an orthogonal array. The root is appended to the list of arrays.

`int array_diff(caray_p A, caray_p B, const rowindex_t r, const colindex_t c, rowindex_t &rpos, colindex_t &cpos)`

Compare 2 arrays and return position of first difference.

`inline void fastJupdate(const array_t *array, rowindex_t N, const int J, const colindex_t *column_indices, array_t *tmp)`

helper function to calculate J-values

`int jvalue(const array_link &array, const int J, const int *column_indices)`

Calculate J-value for a 2-level array

`int jvaluefast(const array_t *array, rowindex_t N, const int J, const colindex_t *column_indices)`

Calculate J-value for a column combination of a 2-level array

We assume the array has values 0 and 1. No boundary checks are performed.

`std::vector<jstruct_t> analyseArrays(const arraylist_t &arraylist, const int verbose, const int jj = 4)`

Analyse a list of arrays.

`void showArrayList(const arraylist_t &lst)`

print a list of arrays to stdout

`long nArrays(const char *fname)`

return number of arrays in an array file

`void arrayfileinfo(const char *filename, int &number_of_arrays, int &number_of_rows, int &number_of_columns)`

return information about file with arrays

Parameters

- **filename** – Filename of array file
- **number_of_arrays** – Variable is set with number of arrays
- **number_of_rows** – Variable is set with number of rows
- **number_of_columns** – Variable is set with number of columns

`arraylist_t readarrayfile`(const char *fname, int verbose = 1, int *setcols = 0)

Read all arrays in a file

Parameters

- **fname** – Filename to read from
- **verbose** – Verbosity level
- **setcols** – Pointer to return number of columns from array file

Returns

List of arrays

`int readarrayfile`(const char *filename, `arraylist_t` *arraylist, int verbose = 1, int *setcols = 0, int *setrows = 0, int *setbits = 0)

Read all arrays in a file and append them to an array list

Parameters

- **filename** – Filename to read from
- **arraylist** – Pointer to list of arrays
- **verbose** – Verbosity level
- **setcols** – Reference that is set with the number of columns from the file
- **setrows** – Reference that is set with the number of rows from the file
- **setbits** – Reference that is set with the number of bits from the file

Returns

`int writearrayfile`(const char *filename, const `arraylist_t` &arraylist, `arrayfile::arrayfilemode_t` mode = `arrayfile::ATEXT`, int nrows = `NRAUTO`, int ncols = `NRAUTO`)

Write a list of arrays to file on disk

Parameters

- **filename** – Filename to use
- **arraylist** – List of arrays to write
- **mode** – Mode for the file with designs
- **nrows** – If the list of arrays is empty, use this number of rows for the design file
- **ncols** – If the list of arrays is empty, use this number of rows for the design file

Returns

Value zero if successful

`int writearrayfile`(const char *filename, const `array_link` &array, `arrayfile::arrayfilemode_t` mode = `arrayfile::ATEXT`)

Write a single array to file.

`int append_arrayfile`(const char *filename, const `array_link` array)

Append a single array to an array file. creates a new file if no file exists.

`void selectArrays`(const std::string filename, std::vector<int> &idx, `arraylist_t` &fl, int verbose = 0)

Make a selection of arrays from binary array file, append to list.

```
array_link selectArrays(std::string filename, int index)
    Select a single array from a file.

arraylist_t selectArrays(const arraylist_t &input_list, std::vector<int> &idx)
    Make a selection of arrays.

arraylist_t selectArrays(const arraylist_t &input_list, std::vector<long> &idx)
    Make a selection of arrays.

void selectArrays(const arraylist_t &input_list, std::vector<int> &idx, arraylist_t &output_list)
    Make a selection of arrays, append to list.

void selectArrays(const arraylist_t &input_list, std::vector<long> &idx, arraylist_t &output_list)
    Make a selection of arrays, append to list.

template<class Container, class IntType>
void keepElements(Container &al, std::vector<IntType> &idx)
    From a container keep all elements with specified indices.

template<class Container, class IntType>
void removeElements(Container &al, std::vector<IntType> &idx)
    From a container remove all elements with specified indices.

template<class MType>
void selectArraysMask(const arraylist_t &al, std::vector<MType> &mask, arraylist_t &rl)
    Make a selection of arrays from a list, append to list.

template<class IndexType>
void appendArrays(const arraylist_t &al, const typename std::vector<IndexType> &idx, arraylist_t &lst)
    Append selection of arrays to existing list.

void appendArrays(const arraylist_t &arrays_to_append, arraylist_t &dst)
    Append set of arrays to existing list.

template<class atype>
void write_array_format(const atype *array, const int nrows, const int ncols, int width = 3)
    Write a formatted array

template<class atype>
void write_array_format(FILE *fid, const atype *array, const int nrows, const int ncols)
    Write an array to a file pointer.

template<class atype>
void write_array_latex(std::ostream &ss, const atype *array, const int nrows, const int ncols)
    write an array in latex style

void convert_array_file(std::string input_filename, std::string output_filename, arrayfile::arrayfilemode_t
                        output_format, int verbose = 0)
    Convert a file with arrays to a different format

bool readbinheader(FILE *fid, int &nr, int &nc)
    Read header for binary data file. Return true if valid header file

    The header consists of 4 integers: 2 magic numbers, then the number of rows and columns

void writebinheader(FILE *fid, int number_rows, int number_columns)
    Write header for binary data file.

template<class Type>
```

`void vector2doublebinfile(const std::string fname, std::vector<Type> vals, int writeheader = 1)`

Write a vector of numeric elements to binary file as double values.

`void vectorvector2binfile(const std::string fname, const std::vector<std::vector<double>> vals, int writeheader, int na)`

Write a vector of vector elements to binary file.

`MatrixFloat array2eigenX1(const array_link &array, int intercept = 1)`

Convert 2-level array to main effects in Eigen format

Parameters

- **array** – Array to convert
- **intercept** – If True, then include the intercept

Returns

The main effects model

`MatrixFloat array2eigenX2(const array_link &array)`

Convert 2-level array to second order interaction matrix in Eigen format

The intercept and main effects are not included.

Parameters

array – Array to convert

Returns

The second order interaction model

`MatrixFloat array2eigenModelMatrix(const array_link &array)`

Convert 2-level array to second order interaction model matrix (intercept, main effects, interaction effects)

Parameters

array – Design of which to calculate the model matrix

Returns

Eigen matrix with the model matrix

`std::pair<MatrixFloat, MatrixFloat> array2eigenModelMatrixMixed(const array_link &array, int verbose = 1)`

Create first and second order model matrix for mixed-level orthogonal array

For 2-level arrays a direct calculation is used. For mixel-level arrays Helmert contrasts are used.

Parameters

- **array** – Input array
- **verbose** – Verbosity level

Returns

Pair with main effects and two-factor interaction model

`std::vector<int> numberModelParams(const array_link &array, int order = -1)`

Calculate number of parameters in the model matrix

A list of integers is returned, with the number of columns in:

- The intercept (always 1)
- The main effects

- The interaction effects (second order interaction terms without quadratics)
- The quadratic effects

Parameters

- **array** – Orthogonal array or conference design
- **order** – Not used any more

Returns

List of sizes

```
int arrayInFile(const array_link &array, const char *array_file, int verbose = 1)
```

return index of specified array in a file. returns -1 if array is not found

Parameters

- **array** – Array to find
- **array_file** – Location of file with arrays
- **verbose** – Verbosity level

Returns

Position of array in list

```
int arrayInList(const array_link &array, const arraylist_t &arrays, int verbose = 1)
```

return index of specified array in a list. returns -1 if array is not found

Parameters

- **array** – Array to find
- **arrays** – List of arrays
- **verbose** – Verbosity level

Returns

Position of array in list

Variables

```
const int NRAUTO = 0
```

```
struct arraydata_t
```

#include <arraytools.h> Specifies a class of arrays.

The specification includes the number of rows, number of columns, factor levels and strength.

Public Functions

arraydata_t()

Specifies a class of orthogonal arrays

The specification includes the number of rows, number of columns, factor levels and strength.

An orthogonal array of strength t, N runs, k factors (columns) and factor levels s[i] is an N times k array with symbols 0, 1, ..., s[i]-1 in column i such that for every t columns every t-tuple of elements occurs equally often.

arraydata_t(*array_t* s, *rowindex_t* N, *colindex_t* strength, *colindex_t* ncols)

Specifies a class of orthogonal arrays

The specification includes the number of rows, number of columns, factor levels and strength.

An orthogonal array of strength t, N runs, k factors (columns) and factor levels s[i] is an N times k array with symbols 0, 1, ..., s[i]-1 in column i such that for every t columns every t-tuple of elements occurs equally often.

Parameters

- **s** – Factor levels
- **N** – Number of rows
- **strength** – Strength for class
- **ncols** – Number of columns for the class

arraydata_t(const std::vector<int> s, *rowindex_t* N, *colindex_t* strength, *colindex_t* ncols)

Specifies a class of orthogonal arrays

The specification includes the number of rows, number of columns, factor levels and strength.

An orthogonal array of strength t, N runs, k factors (columns) and factor levels s[i] is an N times k array with symbols 0, 1, ..., s[i]-1 in column i such that for every t columns every t-tuple of elements occurs equally often.

Parameters

- **s** – Factor levels
- **N** – Number of rows
- **strength** – Strength for class
- **ncols** – Number of columns for the class

arraydata_t(const *array_t s_, *rowindex_t* N, *colindex_t* strength, *colindex_t* ncols)**

Specifies a class of orthogonal arrays

The specification includes the number of rows, number of columns, factor levels and strength.

An orthogonal array of strength t, N runs, k factors (columns) and factor levels s[i] is an N times k array with symbols 0, 1, ..., s[i]-1 in column i such that for every t columns every t-tuple of elements occurs equally often.

arraydata_t(const *arraydata_t* &adp)

Specifies a class of orthogonal arrays

The specification includes the number of rows, number of columns, factor levels and strength.

An orthogonal array of strength t, N runs, k factors (columns) and factor levels s[i] is an N times k array with symbols 0, 1, ..., s[i]-1 in column i such that for every t columns every t-tuple of elements occurs equally often.

arraydata_t(const *arraydata_t* *adp, *colindex_t* newncols)

Specifies a class of orthogonal arrays

The specification includes the number of rows, number of columns, factor levels and strength.

An orthogonal array of strength t, N runs, k factors (columns) and factor levels s[i] is an N times k array with symbols 0, 1, ..., s[i]-1 in column i such that for every t columns every t-tuple of elements occurs equally often.

~arraydata_t()

arraydata_t &**operator=**=(const *arraydata_t* &ad2)

int **operator==**=(const *arraydata_t* &ad2)

bool **ismixed**() const

return true if the class represents mixed-level arrays

bool **is2level**() const

return true if the class represents a 2-level array

array_link **randomarray**(int strength = 0, int ncols = -1) const

return random array from the class. this operation is only valid for strength 0 or 1

void **writeConfigFile**(const char *filename) const

Write file with specification of orthogonal array class.

Parameters

filename – Filename to write to

std::string **idstr**() const

return string with class representation

std::string **idstrseriesfull**() const

return string with class representation. series of level is expended

std::string **fullidstr**(int series = 0) const

return string with class representation

std::string **latexstr**(int cmd = 0, int series = 0) const

return latex string describing the class

inline *arraydata_t* **reduceColumns**(int k)

std::string **showstr**() const

Return string used for displaying the class.

void **show**(int verbose = 1) const

void **complete_arraydata**()

Calculate derived data such as the index and column groups from a design.

void **lmc_overflow_check**() const

check whether the LMC calculation will overflow

void **complete_arraydata_fixlast**()

```

void complete_arraydata_splitn(int ns)

void set_colgroups(const std::vector<int> splits)

void set_colgroups(const symmetry_group &sg)
    set column group equal to that of a symmetry group

std::vector<int> get_column_groups_sizes() const
    return sizes of the column groups

void show_colgroups() const
    show column groups in the array class

void calculate_oa_index(colindex_t strength)
    calculate the index of the orthogonal arrays in this class

array_link create_root(int n_columns = -1, int fill_value = 0) const
    return the root array for the class

int getfactorlevel(int idx) const
    return the factor level for the specified column return -1 if the column index is invalid

inline std::vector<int> getS() const
    return factor levels

std::vector<int> factor_levels() const
    return factor levels

std::vector<int> factor_levels_column_groups() const
    return factor levels for the column groups

void reset_strength(colindex_t strength)
    Reset strength of arraydata.

```

Parameters**strength** – The strength to reset the structure to*colindex_t* **get_col_group**(const *colindex_t* col) const

Return index of the column group for a column.

bool **is_factor_levels_sorted**() const

Return True if the factor levels are sorted from large to small.

Public Members*rowindex_t* **N**

number of runs

colindex_t **ncols**

total number of columns (factors) in the design

colindex_t **strength**

strength of the design

`array_t *s`

pointer to factor levels of the array

`ordering_t order`

Ordering used for arrays.

`colindex_t ncolgroups`

number of groups of columns with the same number of levels

`colindex_t *colgroupindex`

specifies for each column the index of the column group

`colindex_t *colgroupsize`

specifies for each column the size of the column group

`int oaindex`

index of the array

struct `array_link`

`#include <arraytools.h>`

Public Functions

`array_link()`

A class representing an integer valued array

`array_link(rowIndex_t nrows, colindex_t ncols, int index)`

A class representing an integer valued array

The array is initialized with zeros.

Parameters

- `nrows` – Number of rows
- `ncols` – Number of columns
- `index` – Number to keep track of lists of designs

`array_link(rowIndex_t nrows, colindex_t ncols, int index, carray_t *data)`

A class representing an integer valued array

Initialize with data from a pointer.

`array_link(const array_link&)`

A class representing an integer valued array

Initialize with data from another `array_link` object.

`array_link(Eigen::MatrixXd &eigen_matrix)`

A class representing an integer valued array

Initialize with data from an Eigen matrix.

array_link(const *array_link* &array, const std::vector<int> &column_permutation)

A class representing an integer valued array

The array is initialized by permuting the columns of another array

Parameters

- **array** – Source to copy from
- **column_permutation** – The permutation to apply

array_link(const *array_t* *array, *rowindex_t* nrows, *colindex_t* ncols, int index = 0)

A class representing an integer valued array

array_link(const *array_t* *array, *rowindex_t* nrows, *colindex_t* ncolsorig, *colindex_t* ncols, int index)

A class representing an integer valued array

array_link(const std::vector<int> &values, *rowindex_t* nrows, *colindex_t* ncols, int index = 0)

A class representing an integer valued array

The array is initialized by copying the values from a vector.

~array_link()

array_link **clone**() const

void showarray() const

print array to stdout

std::string **showarrayString()** const

print array to string

void showarraycompact() const

print array to stdout in compact format (no whitespace between elements)

void showproperties() const

print array properties to stdout

bool is2level() const

return true if the array is a 2-level array (e.g. only contains values 0 and 1)

bool is_mixed_level() const

return true if the array is a mixed-level array

bool is_orthogonal_array() const

return true if the array is array with values in 0, 1, ..., for each column

bool is_conference() const

return true if the array is a +1, 0, -1 valued array

bool is_conference(int number_of_zeros) const

return true if the array is a +1, 0, -1 valued array, with specified number of zeros in each column

bool isSymmetric() const

return true if the array is symmetric

void makeSymmetric()

make the array symmetric by copying the upper-right to the lower-left

```
array_link deleteColumn(int index) const
    return array with selected column removed

array_link selectFirstRows(int nrows) const
    return array with first number_of_arrays rows

array_link selectFirstColumns(int ncolumns) const
    return array with first number_of_arrays columns selected

array_link selectLastColumns(int ncolumns) const
    return array with last number_of_arrays columns selected

array_link selectColumns(const std::vector<int> c) const
    select columns from an array

array_link selectColumns(int c) const
    select single column from an array

inline void setColumn(int c, const std::vector<int> v)
    set a column of the array to the given vector

inline void setColumn(int c, const std::vector<signed char> v)
    set a column of the array to the given vector

array_link transposed() const
    return transposed array

double Defficiency() const
    calculate D-efficiency

double DsEfficiency(int verbose = 0) const
    calculate main effect robustness (or Ds-optimality)

std::vector<double> Deficiencies(int verbose = 0, int addDs0 = 0) const
    calculate D-efficiency, calculate main effect robustness (or Ds-optimality) and D1-efficiency for an orthogonal array

double VIFefficiency() const

double Aefficiency() const
    calculate A-efficiency

double Eefficiency() const
    calculate E-efficiency

std::vector<int> Fvalues(int number_of_columns) const
    Calculate F-values of a 2-level matrix.

    This assumes the strength is at least 3. Otherwise use the jstruct_t object

std::vector<int> FvaluesConference(int number_of_columns) const
    Calculate F-values of a conference design

Parameters
    number_of_columns – Number of columns to use

Returns
    The Fk vector with k the number of columns specified
```

`std::vector<int> Jcharacteristics(int jj = 4) const`
Calculate the Jk-characteristics of the matrix (the values are signed)

Parameters`jj` – Number of columns to use**Returns**

Vector with calculated Jk values

`std::vector<double> PECsequence(int verbose = 0) const`

Calculate the projective estimation capacity sequence.

`std::vector<double> PICsequence(int verbose = 0) const`

Calculate the projective information capacity sequence.

`int rank() const`

calculate rank of array

`std::vector<double> GWLP(int truncate = 1, int verbose = 0) const`

Calculate generalized wordlength pattern

See also:`GWLP`

`int strength() const`

calculate strength of an array

`bool foldover() const`

return true if the array is a foldover array

`array_t min() const`

`array_t max() const`

`double CL2discrepancy() const`

Calculate centered L2 discrepancy

The method is from “A connection between uniformity and aberration in regular fractions of two-level factorials”, Fang and Mukerjee, 2000

`array_link randomperm() const`

apply a random permutation of rows, columns and levels of an orthogonal array

`array_link randomcolperm() const`

apply a random permutation of columns of an orthogonal array

`array_link randomrowperm() const`

apply a random permutation of rows of an orthogonal array

`MatrixFloat getModelMatrix(int order, int intercept = 1, int verbose = 0) const`

Calculate model matrix of an orthogonal array

This function uses `array2eigenModelMatrixMixed` for the calculation.

Parameters

- **order** – For 0 return only the intercept; for 1 return intercept and main effects; for 2 return intercept, main effects and interaction effects.
- **intercept** – If 1, then include the intercept in the output.
- **verbose** – Verbosity level

Returns

Calculated model matrix

`array_link &operator=(const array_link &rhs)`

`array_link &deepcopy(const array_link &rhs)`

`array_link &shallowcopy(const array_link &rhs)`

`int operator==(const array_link &rhs) const`

Return True if both arrays are equal.

Parameters

`rhs` – Array to compare to

Returns

1 if arrays are equal. 0 otherwise. Returns 0 if arrays have different sizes

`int operator!=(const array_link &rhs) const`

`int operator<(const array_link &rhs) const`

`int operator>(const array_link &rhs) const`

`int equalsize(const array_link &rhs) const`

return true of two array have the same dimensions

`array_link operator+(const array_link&) const`

elementwise addition

`array_link operator+(array_t value) const`

elementwise addition

`array_link operator-(const array_link&) const`

`array_link operator-(array_t value) const`

`array_link operator*(const array_link &rhs) const`

elementwise multiplication

`array_link operator*(array_t value) const`

`array_link operator*=(array_t value)`

`array_link operator+=(array_t value)`

`array_link operator-=(array_t value)`

`inline const array_t &atfast(const rowindex_t r, const colindex_t c) const`

get element from array, no error checking, inline version

`inline array_t &atfast(const rowindex_t r, const colindex_t c)`

get element from array, no error checking, inline version

```

array_t _at(const rowindex_t, const colindex_t) const
    get element at specified position, no bounds checking

array_t _at(const int index) const
    get element at specified position, no bounds checking

array_t at(const rowindex_t, const colindex_t) const
    get element at specified position

array_t at(const int index) const
    get element at specified position

array_t &at(const rowindex_t, const colindex_t)
    get element at specified position

void setconstant(array_t value)
    set all elements in the array to a value

void setvalue(int row, int col, int value)
    set value of an array

void setvalue(int row, int col, double value)
    set value of an array

void _setvalue(int row, int col, int value)
    set value of an array, no bounds checking!

void negateRow(rowindex_t row)
    multiply a row by -1

void show() const
    print information about array

std::string showstr() const
    return string describing the array

std::string md5() const
    return md5 sum of array representation (as represented with 32bit int datatype in memory)

bool columnEqual(int column_index, const array_link &rhs, int column_index_rhs) const
    return true if two columns are equal

int firstColumnDifference(const array_link &A) const
    return index of first different column

bool firstDiff(const array_link &A, int &r, int &c, int verbose = 1) const
    Calculate row and column index of first difference between two arrays

    The difference is according to the column-major ordering.

void create_root(const arraydata_t &arrayclass, int fill_value = 0)
    create root in arraylink

double nonzero_fraction() const
    return fraction of nonzero elements in array

void clear()
    fill array with zeros

```

```
inline void getarraydata(int *pymat1, int n)

template<class numtype>
inline void setarraydata(const numtype *tmp, int n)
    internal function

template<class numtype>
inline void setarraydata_transposed(const numtype *input_data, int n)
    internal function

inline void setarraydata(std::vector<int> tmp, int n)
    special method for SWIG interface

template<class numtype>
inline void setarraydata(std::vector<numtype> tmp, int n)
    internal function

void setcolumn(int target_column, const array_link &source_array, int source_column = 0) const
    set column to values

void init(rowindex_t r, colindex_t c)

symmetry_group row_symmetry_group() const
    return the row_symmetry group of an array

array_link reduceLMC() const
    return the LMC form of the array

array_link reduceDOP() const
    return the delete-one-factor-projection form of the array

MatrixFloat getEigenMatrix() const
    return the array as an Eigen matrix

int columnGreater(int c1, const array_link &rhs, int rhs_column) const
    return true if specified column is smaller than column in another array

void debug() const
```

Public Members

rowindex_t **n_rows**

Number of rows in array.

colindex_t **n_columns**

Number of columns in array.

int **index**

Index number.

array_t ***array**

Pointer to array data.

Public Static Attributes

```
static const int INDEX_NONE = 0
```

```
static const int INDEX_ERROR = -1
```

```
static const int INDEX_DEFAULT = 0
```

Private Functions

```
bool equal_size(const array_link &array) const
    return true if both arrays have the same size
bool _valid_index(const rowindex_t r, const colindex_t c) const
bool _valid_index(int index) const
```

Friends

```
friend std::ostream &operator<<(std::ostream&, const array_link &A)
    print an array to output stream
```

```
class jstructbase_t
    #include <arraytools.h> struct to hold data of an array, e.g. J-characteristic. Abstract base class
    Subclassed by jstructconference_t
```

Public Functions

```
int maxJ() const
    calculate maximum J value
inline std::vector<int> Jvalues() const
    calculate possible values in F vector
std::vector<int> calculateF() const
    Calculate histogram of J values
```

```
\return Histogram of J values
```

The histogram bins are given by the values of @ref Jvalues.

```
virtual void calc(const array_link &array) = 0
```

Calculate the J-values for a given array.

```
void show()
```

Show contents of structure.

```
void showdata(int verbose = 1)
```

```
std::string showstr()  
inline int allzero()  
    return 1 if all vals are zero
```

Public Members

```
std::vector<int> values  
    calculated J-characteristics  
  
std::vector<int> jvalues  
  
std::map<int, int> jvalue2index  
    map from Jk-value to index in the jvalues variable  
  
int jj  
    number of columns
```

```
struct symmdata  
#include <arraytools.h> structure containing data related to symmetries of arrays
```

Public Functions

```
symmdata(const array_link &al, int minlen = 1)  
inline void show(int verbose = 1) const  
inline std::vector<int> checkIdx(int col = -1) const  
    list with indices set to check for symmetry reductions
```

Public Members

```
array_link rowvalue  
array_link orig  
array_link ft
```

```
class jstruct_t  
#include <arraytools.h> struct to hold data of an array, e.g. J-characteristic, rank  
See papers: Minimum G2-aberration properties of two-level foldover designs, Butler, 2004 Design Selection and  
Classification for Hadamard Matrices Using Generalized Minimum Aberration Criteria, Deng and Tang
```

Public Functions

jstruct_t()

Create an object to calculate J-characteristics.

jstruct_t(const array_link &al, int jj = 4)

Create an object to calculate J-characteristics.

jstruct_t(const int N, const int K, const int jj = 4)

Create an object to calculate J-characteristics.

jstruct_t(const jstruct_t &js)

Create an object to calculate J-characteristics.

~jstruct_t()

jstruct_t &operator=(const jstruct_t &rhs)

int maxJ() const

calculate maximum J value

int number_J_values(int strength) const

Calculate the number of possible J values that can occur for the given strength.

std::vector<int> Fval(int strength = 3) const

Calculate possible values in F vector

Parameters

strength – Strength to use

Returns

Vector with possible Jk values (ordered from high to low)

std::vector<int> calculateF(int strength = 3) const

calculate histogram of J values for a 2-level array

void calculateAberration()

Calculate aberration value

This is equal to the sum of the squares of all Jk values, divided by the number of rows squared.

The calculated aberration is stored in the variable aberration.

void show() const

Show contents of structure.

void showdata()

std::string showstr()

int allzero() const

return 1 if all J values are zero, otherwise return 0

void calcj5(const array_link &al)

calculate J-characteristics of a 2-level array, special function for jj=5

Public Members

int N

number of rows in array

int k

number of columns in array

int jj

J-characteristic that is calculated.

int nc

number of column combinations possible

std::vector<int> values

contains calculated J-values

double aberration

calculated abberation

Private Functions

void init(int N, int k, int jj)

init data structures

void calc(const array_link &al)

calculate J-characteristics of a 2-level array

void calcj4(const array_link &al)

calculate J-characteristics of a 2-level array, special function for jj=4

class jstructconference_t : public jstructbase_t

#include <arraytools.h> Calculate J-characteristics of conference designs

Public Functions

inline jstructconference_t(int N, int jj = 4)

Create structure to calculate J-characteristics of conference designs

Parameters

- **N** – Number of rows
- **jj** – Number of columns to use for the Jk-characteristics

inline jstructconference_t(const array_link &array, int jj = 4)

Calculate J-characteristics of a conference design

Parameters

- **array** – Array to calculate the J-characteristics for

- **jj** – Number of columns to use for the Jk-characteristics

Private Functions

```
void calcJvalues(int N, int jj)
virtual void calc(const array_link &al)
Calculate the J-values for a given array.
```

class array_transformation_t

#include <arraytools.h> Contains a transformation of an array.

Contains an array transformation. The transformation consists of column, row and level permutations. The level and column permutations are not commutative (since the level permutations are tied to a particular column). We apply the column permutations first.

Public Functions

```
array_transformation_t(const arraydata_t *arrayclass)
array_transformation_t(const arraydata_t &arrayclass)
array_transformation_t()
array_transformation_t(const array_transformation_t &transformation)
copy constructor
array_transformation_t &operator=(const array_transformation_t &at)
assignment operator
~array_transformation_t()

void show() const
show the array transformation

bool isIdentity() const
return true if the transformation is equal to the identity

array_transformation_t inverse() const
return the inverse transformation

void reset()
return the transformation to the identity transformation

void randomize()
initialize to a random transformation

void randomizecolperm()
initialize with a random column permutation

void randomizerowperm()
initialize with a random row permutation

array_link apply(const array_link &array) const
apply transformation to an array_link object
```

```
int operator==(const array_transformation_t &t2) const
    Comparison operator.

array_transformation_t operator*(const array_transformation_t b) const
    composition operator. the transformations are applied from the left

void apply(array_t *source,target) const
    apply transformation to an array (inplace)

void apply(const array_t *source, array_t *target) const
    apply transformation to an array

void print_transformed(array_t *source) const
    apply transformation and show resulting array

void show(std::ostream &out) const

std::vector<int> rowperm() const
    return the row permutation of the transformation

std::vector<int> colperm() const
    return the column permutation of the transformation

std::vector<int> lvlperm(int c) const
    return the level permutations of the transformation

void setrowperm(std::vector<int> row_permutation)
    set the row permutation of the transformation

void setcolperm(std::vector<int> column_permutation)
    set the column permutation of the transformation

void setlevelperm(int column_index, std::vector<int> lvl_permutation)
    set the level permutation of the transformation
```

Public Members

rowperm_t **rperm**

row permutation

colperm_t **cperm**

column permutation

levelperm_t ***lperms**

level permutations

const *arraydata_t* ***ad**

type of array

Private Functions

```
void allocate_data_structures()
    initialize permutation structures

void free_data_structures()
    free permutation structures and arraydata_t structure
```

class **conference_transformation_t**

#include <arraytools.h> Contains a transformation of a conference matrix.

Contains an array transformation. The transformation consists of column permutations, row permutations and sign switches for both the rows and columns.

The sign switches and the permutations are not commutative. We apply the permutations first and then the sign flips.

Public Functions

```
conference_transformation_t()

conference_transformation_t(int nrows, int ncols)
    default constructor

conference_transformation_t(const array_link &al)

conference_transformation_t(const conference_transformation_t &T)

void show(int verbose = 1) const
    show the array transformation

bool isIdentity() const
    return true if the transformation is equal to the identity

conference_transformation_t inverse() const
    return the inverse transformation

void reset()
    return the transformation to the identity transformation

void randomize()
    initialize to a random transformation

void randomizecolperm()
    initialize with a random column permutation

void randomizerowperm()
    initialize with a random row permutation

void randomizecolflips()
    initialize with random col switches

void randomizerowflips()
    initialize with random row switches

array_link apply(const array_link &al) const
    apply transformation to an array_link object
```

```
int operator==(const conference_transformation_t &rhs) const  
conference_transformation_t operator*(const conference_transformation_t &rhs) const  
composition operator. the transformations are applied from the left  
E.g. (T1*T2)(x) = T1(T2(x))  
inline void setrowperm(std::vector<int> rp)  
inline void setcolperm(std::vector<int> cp)
```

Public Members

```
std::vector<int> rperm  
row permutation of the transformation  
  
std::vector<int> cperm  
column permutation of the transformation  
  
std::vector<int> cswitch  
sign flips for the columns  
  
std::vector<int> rswitch  
sign flips for the rows  
  
int nrows  
number of rows  
  
int ncols  
number of columns
```

Private Functions

```
void init(int nr, int nc)
```

```
struct arraywriter_t  
#include <arraytools.h> structure to write arrays to disk, thread safe
```

Public Functions

```
inline arraywriter_t()  
inline ~arraywriter_t()  
inline void flush()  
flush all output files  
inline void writeArray(const array_link &A)  
write a single array to disk
```

```
inline void writeArray(const arraylist_t &lst)
    write a list of arrays to disk

inline void initArrayFiles(const arraydata_t &ad, int kstart, const std::string prefix, arrayfilemode_t mode
    = ABINARY_DIFF)
    initialize the result files

inline int nArraysWritten() const
    return the total number arrays written to disk

inline void closeafies()
```

Public Members

std::vector<arrayfile_t*> **afiles**

Pointers to different data files.

Since depth_extend is a depth first approach we need to store arrays with a different number of columns

bool **writearrays**

only write arrays if this variable is true

int **nwritten**

number of arrays written to disk

int **verbose**

verbosity level

namespace **arrayfile**

Enums

enum **arrayfilemode_t**

file format mode

Values:

enumerator **ATEXT**

text based format

enumerator **ALATEX**

write arrays to a text file in a format that can be parsed by LaTeX

enumerator **ABINARY**

binary format

enumerator **ABINARY_DIFF**

binary format storing differences of arrays

enumerator **ABINARY_DIFFZERO**

binary format storing differences of arrays and zero offsets

enumerator **AERROR**

enumerator **A_AUTOMATIC**

automatically determine the format

enumerator **A_AUTOMATIC_BINARY**

automatically determine the format (but binary)

enum **afilerw_t**

file mode for array file

Values:

enumerator **READ**

enumerator **WRITE**

enumerator **READWRITE**

struct **arrayfile_t**

#include <arraytools.h> Structure for reading or writing a file with arrays.

The format of the file is determined by the **arrayfilemode_t**. The format described in detail in the documentation of the OApackage <https://oapackage.readthedocs.io/en/latest/>.

Public Functions

arrayfile_t()

Structure for reading or writing a file with arrays

arrayfile_t(const std::string filename, int verbose = 1)

Structure for reading or writing a file with arrays

Parameters

- **filename** – File to open for reading
- **verbose** – Verbosity level

arrayfile_t(const std::string filename, int nrows, int ncols, int narrays = -1, arrayfilemode_t mode = ATEXT, int number_of_bits = 8)

Structure for reading or writing a file with arrays

Open new array file for writing

Parameters

- **filename** – File to open
- **nrows** – Number of rows
- **ncols** – Number of columns
- **narrays** – Specify a number of arrays, or -1 to add dynamically
- **mode** – File mode

- **number_of_bits** – Number of bits to use for storage. For 2-level arrays only 1 bit is needed

~arrayfile_t()
 destructor function, closes all filehandles

void createfile(const std::string filename, int nrows, int ncols, int narrays = -1, arrayfilemode_t m = ATEXT, int number_of_bits = 8)
 Open a new file for writing and (if opened) close the current file.

void closefile()
 close the array file

int isopen() const
 return true if file is open

int seek(int pos)
 seek to specified array position

int read_array(array_link &a)
 read array and return index

array_link readnext()
 read next array from the file

arraylist_t readarrays(int nmax = NARRAYS_MAX, int verbose = 1)
 read set of array from the file

void flush()
 flush any open file pointer

bool isbinary() const
 return true if the file has binary format

int append_arrays(const arraylist_t &arrays, int startidx = -1)
 append list of arrays to the file

void append_array(const array_link &a, int specialindex = -1)
 append a single array to the file

void add_comment(const std::string &comment)
 Add a comment to an array file (only available in text mode)

int swigcheck() const
 return True if code is wrapped by SWIG

std::string showstr() const
 return string describing the object

inline size_t pos() const
 return current position in file

inline bool hasrandomaccess() const
 return true if the file format has random access mode

void updatenumbers()

int read_array(array_t *array, const int nrows, const int ncols)
 read array and return index

```
void finisharrayfile()
void setVerbose(int v)
    set verbosity level
int getnbits()
```

Public Members

std::string **filename**

location of file on disk

int **iscompressed**

True if the file is compressed with gzip.

int **nrows**

number of rows of the arrays

int **ncols**

number of columns of the arrays

int **nbits**

number of bits used when storing an array

arrayfilemode_t mode

file mode, can be ATEXT or ABINARY, ABINARY_DIFF, ABINARY_DIFFZERO

afilerw_t rwmode

file opened for reading or writing

int **narrays**

number of arrays in the file

int **narraycounter**

FILE ***nfid**

int **gzfid**

pointer to compressed file

int **verbose**

verbosity level

Public Static Functions

```
static arrayfile::arrayfilemode_t parseModeString(const std::string format)
    parse string to determine the file mode

static inline int arrayNbits(const arraydata_t &ad)
    return number of bits necessary to store an array

static inline int arrayNbits(const array_link &A)
    return number of bits necessary to store an array
```

Public Static Attributes

```
static const int NARRAYS_MAX = 2 * 1000 * 1000 * 1000
    maximum number of arrays in structure
```

Protected Functions

```
void writeheader()

void read_array_binary(array_t *array, const int nrows, const int ncols)
    Read a binary array from a file.
```

Private Functions

```
int headersize() const
    return header size for binary format array

int barraysize() const
    return size of bit array

size_t afwrite(void *ptr, size_t t, size_t n)
    wrapper function for fwrite or gzwrite

size_t afread(void *ptr, size_t sz, size_t cnt)
    wrapper function for fread or gzread

int read_array_binary_zero(array_link &a)

void write_array_binary(array_t *array, const int nrows, const int ncols)

void write_array_binary(const array_link &A)

void write_array_binary_diff(const array_link &A)
    Write an array in binary diff mode to a file

    We only write the section of columns of the array that differs from the previous array.

void write_array_binary_diffzero(const array_link &A)
    Write an array in binary diffzero mode
```

Private Members

array_link **diffarray**

7.4 Interface for conference designs

Contains functionality to generate and analyse conference designs. For more information see:

- https://en.wikipedia.org/wiki/Conference_matrix
- "A Classification Criterion for Definitive Screening Designs", Schoen et al., The Annals of Statistics, 2019

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Typedefs

typedef *CandidateGenerator* **CandidateGenerator**

Functions

void **print_column**(const *conference_column* &column, const char *msg = 0)

 print a candidate extension

void **showCandidates**(const std::vector<*conference_column*> &column_candidates)

 Show a list of candidate extensions

Parameters

column_candidates – List of candidates to show

array_link **conference2DSD**(const *array_link* &conference_design, bool add_zeros = 1)

 Convert conference design to definitive screening design

 The DSD is created by appending the negated design to the conference design and then appending a row of zeros.

Parameters

- **conference_design** – Array with the conference design
- **add_zeros** – If True, then append a row of zeros

Returns

 The DSD generated from the conference design

array_link **reduceConference**(const *array_link*&, int verbose = 0)

 Reduce conference matrix to normal form using Nauty

See also:

reduceConferenceTransformation

`conference_transformation_t` **reduceConferenceTransformation**(const `array_link` &conference_design, int verbose)

Reduce conference matrix to normal form using Nauty

The design is converted to a graph representation. The graph is then reduced using Nauty to normal form and the resulting graph translated back to a conference design.

Parameters

- **conference_design** – Design to be reduced to normal form
- **verbose** – Verbosity level

Returns

A transformation that converts the input design to normal form

`conference_extend_t` **extend_conference_matrix**(const `array_link` &design, const `conference_t` &conference_type, int extcol, int verbose = 1, int maxzpos = -1)

Extend a single conference design with candidate columns

Parameters

- **design** – Conference design
- **conference_type** – Type specification for the conference designs
- **extcol** – Index of column to generate extensions for
- **verbose** – Verbosity level
- **maxzpos** – Maximum position of zero in specified design

Returns

Structure with information about the possible extensions

`arraylist_t` **extend_conference**(const `arraylist_t` &lst, const `conference_t` conference_type, int verbose, int select_isomorphism_classes = 0)

Extend a list of conference designs with a single column.

The list of conference designs is extended by adding to each design the candidate extention generated by *CandidateGenerator*.

The extension algorithm tries to generate designs in LMC0 normal form and prunes any designs that are not in LMC0 form.

Parameters

- **lst** – List of conference designs
- **conference_type** – Type specification for the conference designs
- **verbose** – Verbosity level
- **select_isomorphism_classes** – If True then select only a single design for each isomorphism class specified by the conference type.

Returns

List of generated conference designs

```
arraylist_t extend_conference_plain(const arraylist_t &lst, const conference_t conference_type, int verbose, int select_isomorphism_classes = 0)
```

Extend a list of conference designs with a single column, plain version without caching

Research function.

```
arraylist_t extend_conference_restricted(const arraylist_t &lst, const conference_t conference_type, int verbose)
```

Extend a list of conference designs with a single column

Research function.

```
arraylist_t extend_double_conference(const arraylist_t &lst, const conference_t conference_type, int verbose)
```

Extend a list of double conference matrices with an additional column

The list of designs is extended by adding each design with the candidate extention generated by *CandidateGeneratorDouble*.

Parameters

- **lst** – List of double conference designs
- **conference_type** – Type specification for the double conference designs
- **verbose** – Verbosity level

Returns

List of generated double conference designs

```
arraylist_t selectConferenceIsomorpismClasses(const arraylist_t &list, int verbose, matrix_isomorphism_t itype = CONFERENCE_ISOMORPHISM)
```

Select representatives for the isomorphism classes of a list of conference arrays

The method uses Nauty for reduction to normal form and selection of isomorphism classes.

Parameters

- **list** – List of designs
- **verbose** – Verbosity level
- **itype** – Specification of the type of isomorphism to use

Returns

Selected isomorphism classes

```
std::vector<int> selectConferenceIsomorpismIndices(const arraylist_t &lst, int verbose, matrix_isomorphism_t itype = CONFERENCE_ISOMORPHISM)
```

select representatives for the isomorphism classes of a list of conference arrays, return indices of classes

```
arraylist_t selectLMC0doubleconference(const arraylist_t &list, int verbose, const conference_t &ctype)
```

Select double conference designs in LMC0 form

Parameters

- **list** – List of double conference designs
- **verbose** – Verbosity level
- **ctype** – Specification of the class of designs

Returns

List with only the designs in the input list that are in LMC0 normal form.

`arraylist_t selectLMC0(const arraylist_t &list, int verbose, const conference_t &ctype)`

Select conference designs in LMC0 form

Parameters

- **list** – List of conference designs
- **verbose** – Verbosity level
- **ctype** – Specification of the class of designs

Returns

List with only the designs in the input list that are in LMC0 normal form.

```
std::vector<conference_column> generateConferenceExtensions(const array_link &array, const conference_t &conference_type, int zero_index, int verbose = 1, int filter_symmetry = 1, int filterj2 = 1)
```

Generate candidate extensions for a conference design

Parameters

- **array** – Design to be extended
- **conference_type** – Class of conference designs
- **zero_index** – Index of zero in candidate column
- **verbose** – Verbosity level
- **filter_symmetry** – If True, filter based on symmetry
- **filterj2** – If True, filter based on J2 values

Returns

List of generated extensions

```
std::vector<conference_column> generateConferenceRestrictedExtensions(const array_link &array, const conference_t &conference_type, int zero_index, int verbose = 1, int filter_symmetry = 1, int filterip = 1)
```

Generate candidate extensions for restricted isomorphism classes

```
std::vector<conference_column> generateDoubleConferenceExtensions(const array_link &array, const conference_t &conference_type, int verbose = 1, int filter_symmetry = 1, int filterip = 1, int filterJ3 = 0, int filter_symmetry_inline = 1)
```

generate extensions for double conference matrices in LMC0 form

```
std::vector<conference_column> generateSingleConferenceExtensions(const array_link &array, const conference_t &conference_type, int zero_index, int verbose, int filter_symmetry, int filterj2, int filterj3, int filter_symmetry_inline = 0)
```

generate extensions for conference matrices in LMC0 form

The the method assumes that the input array is in LMC0 format. In particular, the element at row 0 and column 0 of the design should be a zero.

Parameters

- **array** – Design to generate extensions for
- **conference_type** – Specification of the type of designs
- **zero_index** – Passed to checkZeroPosition to determine whether a zero in the extension column is in a valid position
- **verbose** – Verbosity level
- **filter_symmetry** – If True than reject extensions which are not minimal according to the row symmetry group of the specified design
- **filterj2** – If True than reject extensions which do not satisfy the J2 criterea
- **filterj3** – If True than reject extensions which do not satisfy the J3 criterea
- **filter_symmetry_inline** – Quick rejection of extensions which do not satisfy the symmetry criterion.

Returns

List of extensions of the design

int **maxz**(const *array_link* &al, int column_index = -1)

return max position of zero in array, returns -1 if no zero is found

The parameter k specifies the column to search in. For k=-1 all columns are searched.

bool **compareLMC0**(const *array_link* &array_first, const *array_link* &array_second)

Return true if the first array is smaller in LMC-0 ordering than the second array

arraylist_t **sortLMC0**(const *arraylist_t* &arrays)

sort list of conference designs according to LMC0 ordering

lmc_t **LMC0checkDC**(const *array_link* &al, int verbose = 0)

lmc_t **LMC0check**(const *array_link* &array, int verbose = 0)

bool **isConferenceFoldover**(const *array_link* &array, int verbose = 0)

return true if the design is a foldover array

std::vector<int> **double_conference_foldover_permutation**(const *array_link* &double_conference)

For a double conference design return a row permutation to a single conference design

If the design is not a foldover design then the first element of the returned permutation is -1.

Parameters

double_conference – A double conference design

Returns

Permutation such that the top block of the resulting design forms a single conference design

int **minz**(const *array_link* &al, int column_index)

return minimal position of zero in specified column of a design

class **conference_t**

#include <conference.h> Structure representing the type of conference designs.

Public Types

enum **conference_type**

Type of conference design.

Values:

enumerator **CONFERENCE_NORMAL**

normal conference design

enumerator **CONFERENCE_DIAGONAL**

conference design with zeros only on diagonal

enumerator **DCONFERENCE**

double conference design

Public Functions

conference_t()

Structure representing the type of conference designs

conference_t(int N, int k, int j1zero)

Structure representing the type of conference designs

Parameters

- **N** – Number of rows
- **k** – Number of columns
- **j1zero** – If True then require the J1-characteristics to be zero

conference_t(const conference_t &rhs)

Structure representing the type of conference designs

std::string **idstr() const**

array_link create_root() const

create the unique representative of the 2 column conference design in LMC0 form

array_link create_root_three_columns() const

create the unique representative of the 3 column conference design in LMC0 form

arraylist_t createDoubleConferenceRootArrays() const

create the root arrays with 1 column for the double conference matrices

arraylist_t createRootArrays() const

return the list of root arrays for the class of conference designs

inline std::string **__repr__() const**

return string representation of the object

Public Members

rowindex_t **N**

number of runs

colindex_t **ncols**

total number of columns (factors) in the design

conference_type **ctype**

defines the type of designs

matrix_isomorphism_t **itype**

defines the isomorphism type

bool **j1zero**

if true then J1 values should be zero

bool **j3zero**

if true then J3 values should be zero

class **CandidateGeneratorBase**

#include <conference.h> Class to generate candidate extensions with caching

We assume that the designs to be extended are run ordered, so that the caching has maximal effect.

The key idea used is that any valid extension of a design A with k columns is a permutation of a valid extension of the design B obtained by taking the first $l < k$ columns of A. The permutations that are allowed are called the symmetry inflations. All the j2 checks performed for the extension of B do not have to be repeated for the permutations of this extension.

Subclassed by *CandidateGeneratorConference*, *CandidateGeneratorDouble*

Public Functions

CandidateGeneratorBase(const *array_link* &al, const *conference_t* &ct)

void **showCandidates**(int verbose = 1) const

Show the candidate extensions for each column

conference_column_list **candidates**(int k)

return all candidates for the kth column

Public Members

`conference_t ct`
type of designs to generate

`int verbose`
verbosity level

`mutable array_link al`
last array analyzed

`mutable int last_valid`
index of last valid column

Protected Functions

`inline int startColumn(const array_link &alx, int verbose = 0) const`
Find the starting column for the extension of a design

The static variable START_COL is the number of columns for which is the starting point if the cache is empty. Therefore for a design with initial columns the same, START_COL+1 is the first number of columns with valid entries.

For startcol k the elements in candidate_list[k] are valid, e.g. we can start with extensions valid for index k-1

Protected Attributes

`mutable std::vector<conference_column_list> candidate_list`
list of candidate extensions. the elements of candidate_list[k] correspond to columns with index k-1

Protected Static Attributes

`static const int START_COL = 2`

```
class CandidateGeneratorConference : public CandidateGeneratorBase
#include <conference.h> Class to generate conference candidate extensions.
```

Public Functions

```
CandidateGeneratorConference(const array_link &al, const conference_t &ct)
const std::vector<conference_column> &generateCandidates(const array_link &al) const
    Generate a list of candidate extensions for the specified design.

std::vector<conference_column> generateCandidatesZero(const array_link &al, int kz) const
    generate all candidate extensions with a zero at the specified position
```

class **CandidateGeneratorDouble** : public *CandidateGeneratorBase*

```
#include <conference.h> Class to generate double conference candidate extensions with caching.
```

Public Functions

```
CandidateGeneratorDouble(const array_link &al, const conference_t &ct)
const std::vector<conference_column> &generateCandidates(const array_link &al) const
    Generate a list of candidate extensions for the specified design

This method uses symmetry inflation, assumes j1=0 and j2=0. Optimal performance is achieved when the
arrays to be extended have identical first columns.
```

struct **conference_extend_t**

```
#include <conference.h> Helper structure containing extensions of conference designs
```

Public Functions

```
inline conference_column combine(int i, int j) const
    list of candidate extensions

inline size_t nExtensions() const

inline arraylist_t getarrays(const array_link al) const
    return the set of extension arrays
```

Public Members

std::vector<conference_column> **first**

std::vector<conference_column> **second**
list of first block candidate extensions

std::vector<conference_column> **extensions**
list of first block candidate extensions

class **DconferenceFilter**

```
#include <conference.h> class to filter single or double conference designs
```

Public Functions

```
DconferenceFilter(const array_link &_als, int filter_symmetry, int filterj2_, int filterj3_ = 1)
void show() const
    print object to stdout

std::vector<conference_column> filterList(const std::vector<conference_column> &lst, int verbose = 0)
    const
        filter a list of columns using the filter method

std::vector<conference_column> filterListJ2last(const std::vector<conference_column> &column_list)
    const

std::vector<conference_column> filterListZero(const std::vector<conference_column> &lst) const
    filter a list of cperms using the filterZero method

bool filter(const conference_column &c) const
    return True if the extension satisfies all checks

bool filterJpartial(const conference_column &column, int maxrow) const
    Filter on partial column (only last col)

Parameters

- column – Extension column
- maxrow – the number of rows that are valid



bool filterJ(const conference_column &column, int j2start = 0) const
    return True if the extension satisfies all J-characteristic checks

bool filterJlast(const conference_column &c, int j2start = 0) const
    return True if the extension satisfies all J-characteristic checks for the last columns

bool filterReason(const conference_column &column) const
    return True if the extension satisfies all checks. prints the reason for returning True or False to stdout

bool filterJ3(const conference_column &column) const
    return True if the candidate satisfies the J3 check

bool filterJ3s(const conference_column &column, int idxstart) const
    return True if the candidate satisfies the J3 check for specified pairs

bool filterJ3inline(const conference_column &column) const
    return True if the candidate satisfies the J3 check

bool filterSymmetry(const conference_column &column) const
    return True if the candidate satisfies the symmetry check

bool filterJ2(const conference_column &c) const
    return True if the candidate extension satisfies the J2 check

bool filterJ2last(const conference_column &c) const
    return True if the candidate extension satisfies the J2 check for the last column of the array checked against

bool filterZero(const conference_column &c) const
    return True if the candidate extension satisfies the zero check

    This means that the first entries of the extension do not contain a zero.
```

Public Members

array_link **als**

int **filtersymm**

filter based on symmetry

int **filterj2**

filter based on j2 value

int **filterj3**

filter based on j3 value

int **filterfirst**

filter only columns with first value ≥ 0

int **filterzero**

filter based on first occurrence of zero in a column

mutable long **ngood**

int **inline_row**

row at which infile filtering is performed

symmdata **sd**

Private Members

array_link **dtable**

table of J2 vectors for J3 filter

array_link **inline_dtable**

table of J2 vectors for inline J3 filter

std::vector<int> **check_indices**

indices to check for symmetry check

int **minzvalue**

used for filtering based on zero

7.5 Interface for even-odd designs

Contains functions to generate even-odd designs.

The generation is done by defining a special ordering in the set of designs. The primary ordering is based in the J5 value of 5-column designs, the secondary ordering is the regular LMC ordering.

TypeDefs

```
typedef Pareto<mvalue_t<long>, array_link>::pValue (*pareto_cb)(const array_link&, int)
callback function for Pareto calculations
```

```
typedef Pareto<mvalue_t<long>, array_link>::pValue (*pareto_cb_cache)(const array_link&, int, rankStructure &rs)
callback function for Pareto calculations with cache
```

Enums

```
enum depth_alg_t
```

Values:

enumerator DEPTH_DIRECT

enumerator DEPTH_EXTENSIONS

Functions

```
void processDepth(const arraylist_t &goodarrays, depth_alg_t depthalg, depth_extend_t &dextend,
                  depth_extend_sub_t &dextendsublight, int extensioncol, int verbose = 0)
```

Extend arrays using a depth-first or breadth-first approach

Parameters

- **goodarrays** – List of arrays to extend
- **depthalg** – Extend using depth-first or breadth-first
- **dextend** – Option structure for the extension
- **dextendsublight** – Data structure for the extensions
- **extensioncol** – Column to extend
- **verbose** – Verbosity level

```
void depth_extend_hybrid(const arraylist_t &alist, depth_extend_t &dextend, int extcol, const OAextend &oaextendx, int verbose)
```

depth-first extension of arrays. depending on the symmetry group of the array to be extended a direct method is used or a method with caching of candidate columns

```
void depth_extend_direct(const arraylist_t &alist, depth_extend_t &dextend, int extcol, const OAextend
                           &oaextendx, int verbose)
    variation of depth_extend for arrays with large symmetry groups

void depth_extend_array(const array_link &al, depth_extend_t &dextend, const arraydata_t &adfull, int
                         verbose, depth_extensions_storage_t *ds = 0, int = 0)
    depth extend a single array

template<class IndexType>
inline Pareto<mvalue_t<long>, IndexType>::pValue calculateArrayParetoJ5Cache(const array_link &al, int
                           verbose, rankStructure
                           &rs)

void addArraysToPareto(Pareto<mvalue_t<long>, array_link &pset, pareto_cb paretofunction, const arraylist_t
                           &arraylist, int jj, int verbose)
    add arrays to set of Pareto results

void addArraysToPareto(Pareto<mvalue_t<long>, array_link &pset, pareto_cb_cache paretofunction, const
                           arraylist_t &arraylist, int jj, int verbose)
    add arrays to set of Pareto results

Jcounter readStatisticsFile(const char *numbersfile, int verbose)
    read statistics object from disk

void writeStatisticsFile(const char *numbersfile, const Jcounter &jc, int verbose)
    write statistics object to disk

Jcounter calculateJstatistics(const char *afile, int jj = 5, int verbose = 1)
    calculate J-value statistics

int compareJ54(const array_link &lhs, const array_link &rhs)
    Return -1 if the first array is smaller in J54 ordering than the second array, 0 if equal and 1 otherwise

struct depth_path_t
    #include <evenodd.h> structure containing current position in search tree
```

Public Functions

```
inline depth_path_t()

inline void updatePositionGEC(int k, int goodextensioncols)

inline void updatePosition(int k, int c, int m, int extensioncols, int goodextensioncols)

inline void show(int depth, int maxentries = 8) const

inline void init(int ncols, int _depthstart = 9)
```

Public Members

```
std::vector<int> ncurr
    vector with current position

std::vector<int> nmax
    vector with target

std::vector<int> necols
    number of extension columns

std::vector<int> ngecols
    number of good extension columns

int depthstart

struct counter_t
    #include <evenodd.h> structure to count and show number of arrays generated, the structure is thread safe
```

Public Functions

```
counter_t(int n)

void addNfound(int col, int num)

long nArrays() const

void addNumberFound(int n, int k)

void clearNumberFound()

void addNumberFound(const counter_t &de)

void showcountscompact() const
    show information about the number of arrays found

void showcounts(const arraydata_t &ad) const
    show information about the number of arrays found

void showcounts(const char *str, int first, int last) const
    show information about the number of arrays found
```

Public Members

std::vector<int> **nfound**

struct **depth_extend_sub_t**

#include <evenodd.h> Helper structure for dynamic extension

In this structure we keep track of pointers to valid column extensions

Public Functions

inline **depth_extend_sub_t**(int nn = 0)

inline void **resize**(int nn)

inline size_t **n()** const

inline std::vector<int> **updateExtensionPointers**(int extcol)

arraylist_t **initialize**(const *arraylist_t* &alist, const *arraydata_t* &adf, const *OAextend* &oaextend)

initialize the new list of extension columns

inline *arraylist_t* **selectArraysZ**(const *arraylist_t* &alist) const

select the arrays with are LMC and hence need to be written to disk

inline *arraylist_t* **selectArraysXX**(const *array_link* &al, const *arraylist_t* &elist) const

inline void **info()** const

Public Members

std::vector<int> **lmctype**

std::vector<int> **lastcol**

last column changed in lmc check

std::vector<double> **strengthcheck**

std::vector<int> **valididix**

int **verbose**

struct **depth_extend_t**

#include <evenodd.h> Helper structure for dynamic extension.

This structure allows for writing the generated arrays to disk. It also contains functions to print progress of the extension.

Multiple copies of this class are made, but they all share the same *counter_t* and *arraywriter_t* object. Also t0 and tp are shared

Public Functions

```

inline depth_extend_t(const arraydata_t *ad_, double _logtime = 10000000, int _discardJ5 = -1)
inline depth_extend_t(const depth_extend_t &de)

inline ~depth_extend_t()

inline void show()

inline void setNarraysMax(long n)

inline void maxArrayCheck()

inline void showsearchpath(int depth) const

inline bool showprogress(int showtime = 1, int depth = 0, int forcelog = 0)
    show information about the progress of the loop

inline void info() const

inline void setposition(int k, int c, int m, int extensioncols = -1, int goodextensioncols = -1)
    set the position in the dextend structure

inline void setpositionGEC(int k, int goodextensioncols)
    set the position in the dextend structure

```

Public Members

```

int verbose

OAextend oaextend

const arraydata_t *ad

int loglevelcol

double logtime
    print progress every x seconds

arraylist_t extension_column_list

int writearrays
    if set to true write arrays to disk

int discardJ5

long discardJ5number
    if true, then we discard the designs which have J5 maximal

```

arraywriter_t ***arraywriter**

counter_t ***counter**

Public Static Attributes

static double **t0**

static double **tp**

Private Members

long **narraysmax**

depth_path_t **searchpath**

struct **depth_extensions_storage_t**

#include <evenodd.h> Helper structure for the even-odd depth extension.

Public Functions

inline void **resize**(size_t s)

inline void **set**(int ai, const *arraylist_t* &goodarrays, const *arraylist_t* &extension_column_list, *depth_alg_t* depthalg, const *depth_extend_sub_t* &dextendsub)

Public Members

std::vector<*arraylist_t*> **columnextensionsList**

std::vector<*arraylist_t*> **goodarrayslist**

std::vector<*depth_alg_t*> **depthalglist**

std::vector<*depth_extend_sub_t*> **dextendsubList**

struct **jindex_t**

#include <evenodd.h> helper class for indexing statistics of designs

The index consists of the number of columns and the value for the J-characteristic

Public Functions

```
inline jindex_t(int colindex, int jvalue)
inline bool operator<(const jindex_t &rhs) const
inline std::string toString() const
```

Public Members

int k
number of columns

int j
J-value.

class **Jcounter**

#include <evenodd.h> object to hold counts of maximum J_k-values

Public Functions

```
inline Jcounter()
inline Jcounter(int N, int jj = 5, int k = -1)
bool validData()
bool hasColumn(int col) const
    return true if specified column is in the data
inline bool isOpen() const
inline void showPerformance() const
long narrays() const
void show() const
    show statistics of the object
int maxCols() const
long getCount(int k, int j) const
std::vector<long> getTotalsJvalue(int jval) const
std::vector<long> getTotals() const
void showcompact() const
    show statistics of the object
Jcounter &operator+=(Jcounter &jc)
void addArrays(const arraylist_t &arraylist, int verbose = 0)
    add list of arrays to object
```

```
void addArray(const array_link &al, int verbose = 0)  
    add single array to statistics object
```

Public Members

int **N**
number of rows

int **jj**

std::vector<int> **fvals**
std::map<*jindex_t*, long> **maxJcounts**

double **dt**
time needed for calculation

Private Functions

```
void init(int N, int jj, int k = -1)
```

7.6 Interface for extension of LMC designs

Contains functions to generate and extend orthogonal arrays.

Enums

enum **dfilter_t**

Values:

enumerator **DFILTER_NONE**

no filtering on D-efficiency

enumerator **DFILTER_BASIC**

filtering on D-efficiency

enumerator **DFILTER_MULTI**

filtering on D-efficiency with multi column prediction

enum **dcalc_mode**

Values:

enumerator **DCALC_ALWAYS**

always calculate efficiency

enumerator **DCALC_COND**

only calculate efficiency for LMC_LESS

Functions

arraylist_t **extend_arraylist**(const *arraylist_t* &array_list, *arraydata_t* &array_class, *OAextend* const &oaextend_options)

Extend a list of orthogonal arrays

See also:

extend_array(const *array_link* &, *arraydata_t* &, *OAextend const* &)

Parameters

- **array_list** – The list of arrays to be extended
- **array_class** – Class of arrays to generate
- **oaextend_options** – Parameters for the extension algorithm

Returns

List of all generated arrays

arraylist_t **extend_arraylist**(const *arraylist_t* &array_list, const *arraydata_t* &arrayclass)

Extend a list of arrays with default options

See also:

extend_array(const *array_link* &, *arraydata_t* &, *OAextend const* &)

int **extend_arraylist**(const *arraylist_t* &array_list, *arraydata_t* &array_class, *OAextend* const &oaextend_options, *colindex_t* extensioncol, *arraylist_t* &extensions)

Extend a list of orthogonal arrays

See also:

extend_array(const *array_link* &, *arraydata_t* &, *OAextend const* &)

Parameters

- **array_list** – The list of arrays to be extended
- **array_class** – Class of arrays to generate
- **oaextend_options** – Parameters for the extension algorithm
- **extensioncol** – Index of column to be added to the designs
- **extensions** – List to append generated designs to

Returns

List of all generated arrays

Returns

Number of candidate arrays generated

arraylist_t extend_array(const *array_link* &*array*, *arraydata_t* &*array_class*, *OAextend* const &*oaextend*)

Extend a single orthogonal array

Parameters

- **array** – The array to be extended
- **array_class** – Class of arrays to generate
- **oaextend** – Parameters for the extension algorithm

arraylist_t extend_array(const *array_link* &*array*, *arraydata_t* &*arrayclass*)

Extend a single orthogonal array with the default LMC algorithm

See also:

extend_array(const *array_link* &, *arraydata_t* &, *OAextend* const &)

int **extend_array**(const *array_link* &*array*, const *arraydata_t* **arrayclass*, const *colindex_t* *extension_column*,
arraylist_t &*extensions*, *OAextend* const &*oaextend*)

Extend an orthogonal array with a single column

See also:

extend_array(const *array_link* &, *arraydata_t* &, *OAextend* const &)

Parameters

- **array** – Array to extend
- **arrayclass** – Array data for the full array
- **extension_column** – Column to extend
- **extensions** – List to which generated valid extensions are added
- **oaextend** – Structure with options

Returns

Number of candidate extensions generated

arraylist_t runExtendRoot(*arraydata_t* *arrayclass*, int *max_number_columns*, int *verbose* = 0)

Run the LMC extension algorithm starting with the root array

See also:

extend_array(const *array_link* &, *arraydata_t* &, *OAextend* const &)

class **OAextend**

#include <extend.h> Options for the extend code.

class containing parameters of the extension and LMC algorithm

Public Types

enum **extendarray_mode_t**

Specification of how to use the generated extensions.

Values:

enumerator **APPENDEXTENSION**

append extension column to extension list

enumerator **APPENDFULL**

append full array to extension list

enumerator **STOREARRAY**

store extension to disk

enumerator **NONE**

do not store generated extensions

Public Functions

inline **OAextend()**

Options for the extension algorithm

inline **OAextend(const OAextend &o)**

Options for the extension algorithm

inline **OAextend(arraydata_t &arrayclass)**

Options for the extension algorithm

The algorithm is automatically determined from the specified arrayclass.

void **setAlgorithm(algorithm_t algorithm, arraydata_t *ad = 0)**

Set the algorithm to use for LMC checks.

void **setAlgorithmAuto(arraydata_t *ad = 0)**

Set the algorithm automatically.

inline **algorithm_t getAlgorithm() const**

Return algorithm used.

inline std::string **getAlgorithmName() const**

Return algorithm used (as string)

void **updateArraydata(arraydata_t *arrayclass = 0) const**

update the options structuer with the specified class of designs

void **info(int verbose = 1) const**

print configuration to stdout

std::string **__repr__() const**

Public Members

double singleExtendTime

time before printing progress of single extension, [seconds]

int nLMC

number of arrays LMC tested before printing progress of single extension

int checkarrays

perform LMC test after generation of array

int check_maximal

if true then return at once if a single extension has been found

int use_row_symmetry

adds a symmetry check to the extension algorithm based in symmetry of row permutations

int init_column_previous

init column with previous column in extension (if in the same column group)

extendarray_mode_t **extendarraymode**

determines how the extension arrays are stored

arrayfile_t storefile

j5structure_t **j5structure**

Public Static Functions

static inline *algorithm_t* **getPreferredAlgorithm**(const *arraydata_t* &arrayclass, int verbose = 0)

Return preferred extension algorithm

Parameters

- **arrayclass** – Class of designs to extend
- **verbose** – Verbosity level

Returns

Algorithm selected to be used for this class

Private Members

algorithm_t **algmode**

Algorithm mode.

```
struct dextend_t
```

```
#include <extend.h> Structure for dynamic extension of arrays based on D-efficiencies.
```

Public Functions

inline **dextend_t()**

```
inline void resize(int nn)
```

```
void DeficiencyFilter(double Dfinal, int k, int kfinal, double Lmax, int verbose = 1)
```

perform filtering using D-efficiency

```
std::vector<int> filterArrays(const array_link &al, const arraylist_t &earrays, arraylist_t &earraysout,  
                           std::vector<std::vector<double>> &edata, int verbose = 1)
```

filter the arrays based on values in filter

Public Members

```
std::vector<lmc_t> lmctype
```

results of minimal form calculations

```
std::vector<int> lastcol
```

last column changed in lmc check

```
std::vector<double> Deff
```

calculated efficiency values

```
std::vector<int> filter
```

indices of filtered arrays

dfilter t filtermode

dcalc mode Dcheck

int directcheck

perform immediate LMC check in extension

long ntotal

total number of arrays found

long **nLMC**

total number of arrays found in LMC form

long **n**

total number of arrays found passing all tests

double **DmaxDiscard**

long **nmaxrnktotal**

Public Static Attributes

static const int **NO_VALUE** = 0

7.7 Interface for graph tools

This file contains definitions and functions related to graphs and designs.

Author: Pieter Eendebak pieter.eendebak@gmail.com, (C) 2016

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Enums

enum **matrix_isomorphism_t**

Isomorphism types for matrices

Isotopy: permute rows, columns and symbols
Matrix isomorphism: permute rows and columns
Conference isomorphism: permute rows, columns and to row and column negations (values in 0, +1, -1)
Orthogonal array isomorphism: permutations of rows, columns and column symbol permutations

Values:

enumerator **ISOTOPY**

isotopy: permute rows, columns and symbols

enumerator **MATRIX_ISOMORPHISM**

permute rows and columns

enumerator **CONFERENCE_ISOMORPHISM**

permute rows, columns and to row and column negations (values in 0, +1, -1)

enumerator **OA_ISOMORPHISM**

permutations of rows, columns and column symbol permutations

Functions

`array_link transformGraph(const array_link &graph, const std::vector<int> vertex_permutation, int verbose = 1)`

Apply a vertex permutation to a graph.

`array_transformation_t reduceOAnauty(const array_link &array, int verbose = 0)`

Reduce an orthogonal array to Nauty minimal form. the array transformation is returned.

`array_transformation_t reduceOAnauty(const array_link &array, int verbose, const arraydata_t &arrayclass)`

Reduce an orthogonal array to Nauty minimal form. the array transformation is returned.

`std::pair<array_link, std::vector<int>> array2graph(const array_link &array, int verbose = 1)`

Convert orthogonal array to graph representation

The conversion method is as in Ryan and Bulutoglu. The resulting graph is bi-partite. The graph representation can be used for isomorphism testing.

`std::pair<array_link, std::vector<int>> array2graph(const array_link &array, int verbose, const arraydata_t &arrayclass)`

Convert orthogonal array to graph representation

The conversion method is as in Ryan and Bulutoglu. The resulting graph is bi-partite. The graph representation can be used for isomorphism testing.

`array_transformation_t oagraph2transformation(const std::vector<int> &pp, const arraydata_t &arrayclass, int verbose = 1)`

From a relabelling of the graph return the corresponding array transformation.

Variables

`const matrix_isomorphism_t CONFERENCE_RESTRICTED_ISOMORPHISM = OA_ISOMORPHISM`

isomorphism type for column and row permutations and column permutations

namespace `nauty`

Functions

`std::vector<int> reduceNauty(const array_link &graph, std::vector<int> colors, int verbose = 0)`

Reduce a colored graph to Nauty minimal form

The transformation returned is from the normal form to the specified graph.

Parameters

- **graph** – Graph in incidence matrix form
- **colors** – Colors of the graph nodes
- **verbose** – Verbosity level

Returns

Relabelling of the graph vertices

7.8 Interface for LMC normal forms

This file contains definitions and functions to perform minimal form tests and reductions.

Author: Pieter Eendebak pieter.eendebak@gmail.com

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Defines

`ORDER_J5_SMALLER`

`ORDER_J5_GREATER`

`ORDER_J45_SMALLER`

`ORDER_J45_GREATER`

`stringify(name)`

`SDSMART`

Typedefs

`typedef unsigned int rowsort_value_t`

`typedef rowindex_t rowsortlight_t`

`typedef larray<rowindex_t> rowpermtypelight`

`typedef larray<colindex_t> colpermtypelight`

`typedef std::vector<int> colpermtype`

`typedef std::vector<colpermtype> colpermset`

`typedef std::tr1::shared_ptr<symmdata> symmdataPointer`

`typedef double jj45_t`

Value representing the ordered combination of J5 and the 5 J4-values in the J54 ordering.

Enums

enum **lmc_t**

Possible results for the LMC check

Values:

enumerator **LMC_LESS**

Found a permutation which leads to a lexicographically smaller array.

enumerator **LMC_EQUAL**

Found a permutation which leads to a lexicographically equal array.

enumerator **LMC_MORE**

Found a permutation which leads to a lexicographically larger array.

enumerator **LMC_NONSENSE**

No valid result.

enum **algorithm_t**

different algorithms for minimal form check

Values:

enumerator **MODE_LMC**

LMC minimal form.

enumerator **MODE_J4**

LMC minimal form with J4 method.

enumerator **MODE_J5ORDER**

J5 minimal form.

enumerator **MODE_J5ORDERX**

J5 minimal form.

enumerator **MODE_INVALID**

enumerator **MODE_AUTOSELECT**

Automatically select the algorithm.

enumerator **MODE_LMC_SYMMETRY**

debugging method

enumerator **MODE_LMC_2LEVEL**

LMC minimal form, specialized for 2-level arrays.

enumerator **MODE_LMC_DEBUG**

debugging method

enumerator **MODE_J5ORDER_2LEVEL**

J5 minimal form for 2-level arrays.

enum **initcolumn_t**

method used for initialization of columns

Values:

enumerator **INITCOLUMN_ZERO**

Initialize column with zeros.

enumerator **INITCOLUMN_PREVIOUS**

Initialize column with values of previous column.

enumerator **INITCOLUMN_J5**

Initialize column with values based on J5 value.

enum **j5structure_t**

variations of the J45 structures

Values:

enumerator **J5_ORIGINAL**

Ordering based in J5 in succesive columns.

enumerator **J5_45**

Ordering based on J5 and the 5-tuple of J4 values. Also called the L5 ordering.

enum **REDUCTION_STATE**

variable indicating the state of the reduction process

Values:

enumerator **REDUCTION_INITIAL**

the reduction is equal to the initial

enumerator **REDUCTION_CHANGED**

the reduction was changed

enum **OA_MODE**

main mode for the LMC routine: test, reduce or reduce with initialization

Values:

enumerator **OA_TEST**
 test for minimal form

enumerator **OA_REDUCE**
 reduce to minimal form

enumerator **OA_REDUCE_PARTIAL**
 reduce to partial minimal form

enum **INIT_STATE**
 initial state for reduction algorithm
 Values:
 enumerator **INIT_STATE_INVALID**
 enumerator **COPY**
 copy from array argument
 enumerator **INIT**
 initialized by user
 enumerator **SETROOT**
 set initial state to root array

Functions

inline std::string **algorithm_t_list()**
 Return string representation of available algorithm modes.

std::string **algnames**(*algorithm_t* m)
 return name of the algorithm

static inline bool **operator<**(const rowsort_t &a, const rowsort_t &b)
 Comparision operator for the rowsort_t structure.

static inline bool **operator>**(const rowsort_t &a, const rowsort_t &b)
 Comparision operator for the rowsort_t structure.

void **apply_hadamard**(array_link &al, colindex_t hcolumn)
 Apply Hadamard transformation to orthogonal array.

LMCreduction_helper_t *acquire_LMCreduction_object()
 return static structure from dynamic global pool, return with releaseGlobalStatic

void **release_LMCreduction_object**(*LMCreduction_helper_t* *p)

void **clear_LMCreduction_pool()**
 release all objects in the pool

`bool valid_ptr(const symmdataPointer &sd)`

Return true if the (smart) symmdataPointer pointer is allocated

`template<class Type>`

`void insert_if_not_at_end_of_vector(std::vector<Type> &cp, const Type &value)`

Append element to vector if the element the element is not at the end of vector.

`bool is_root_form(const array_link &array, int strength)`

Return True if the array is in root form

Parameters

- **array** – Array to check
- **strength** – Strength to use

Returns

True if the array is in root form for the specified strength

`lmc_t LMCreduction_train(const array_link &al, const arraydata_t *ad, LMCreduction_t *reduction, const OAextend &oaextend)`

helper function for LMC reduction

`lmc_t LMCcheck(const array_t *array, const arraydata_t &ad, const OAextend &oaextend, LMCreduction_t &reduction)`

Perform LMC check or reduction on an array.

`lmc_t LMCcheck(const array_link &array, const arraydata_t &ad, const OAextend &oaextend, LMCreduction_t &reduction)`

Perform LMC check or reduction on an array.

`lmc_t LMCcheck(const array_link &array)`

Perform LMC check on an orthogonal array

Parameters

array – Array to be checked for LMC minimal form

Returns

Result of the LMC check

`lmc_t LMCcheckOriginal(const array_link &array)`

Perform LMC check on a 2-level orthogonal array

The algorithm used is the original algorithm from “Complete enumeration of pure-level and mixed-level orthogonal arrays”, Schoen et al, 2009

Parameters

array – Array to be checked for LMC minimal form

Returns

Result of the LMC check

`void reduceArraysGWLP(const arraylist_t &input_arrays, arraylist_t &reduced_arrays, int verbose, int dopruning = 1, int strength = 2, int dolmc = 1)`

reduce arrays to canonical form using delete-1-factor ordering

`array_transformation_t reductionDOP(const array_link &array, int verbose = 0)`

Caculate the transformation reducing an array to delete-on-factor normal

The normal form is described in “A canonical form for non-regular arrays based on generalized wordlength pattern values of delete-one-factor projections”, Eendebak, 2014

Parameters

- **array** – Orthogonal array
- **verbose** – Verbosity level

Returns

The transformation that reduces the array to normal form

`array_link reduceDOPform(const array_link &array, int verbose = 0)`

Reduce an array to canonical form using delete-1-factor ordering

The normal form is described in “A canonical form for non-regular arrays based on generalized wordlength pattern values of delete-one-factor projections”, Eendebak, 2014

Parameters

- **array** – Orthogonal array
- **verbose** – Verbosity level

Returns

The array transformed to normal form

`void selectUniqueArrays(arraylist_t &input_arrays, arraylist_t &output_arrays, int verbose = 1)`

select the unique arrays in a list, the original list is sorted in place. the unique arrays are append to the output list

`std::vector<GWLPvalue> projectionDOFvalues(const array_link &array, int verbose = 0)`

Calculate projection values for delete-of-factor algorithm

`array_link reduceLMCform(const array_link &array)`

reduce an array to canonical form using LMC ordering

`std::vector<int> LMCcheckLex(arraylist_t const &list, arraydata_t const &ad, int verbose = 0)`

Apply LMC check (original mode) to a list of arrays

`lmc_t LMCcheckLex(array_link const &array, arraydata_t const &arrayclass)`

Perform minimal form check with LMC ordering.

`lmc_t LMCcheckJ4(array_link const &array, arraydata_t const &arrayclass, LMCreduction_t &reduction, const OAextend &oaextend, int jj = 4)`

Perform minimal form check with J4 ordering.

`lmc_t LMCcheckJ5(array_link const &array, arraydata_t const &arrayclass, LMCreduction_t &reduction, const OAextend &oaextend)`

Perform minimal form check for J5 ordering (in the paper this is called the L5 ordering)

`void print_rowsort(rowsort_t *rowsort, int N)`

Print the contents of a rowsort structure.

Parameters

- **rowsort** – Pointer to rowsort structure
- **N** – Number of elements

`void print_column_rowsort(const array_t *arraycol, rowsort_t *rowsort, int N)`

Variables

```
const algorithm_t MODE_ORIGINAL = MODE_LMC
```

```
struct LMCreduction_helper_t
```

#include <lmc.h> Contains structures used by the LMC reduction or LMC check.

Part of the allocations is for structures that are constant and are re-used each time an LMC calculation is performed. Some other structures are temporary buffers that are written to all the time.

Public Functions

```
LMCreduction_helper_t()
```

```
~LMCreduction_helper_t()
```

```
inline void show(int verbose = 1) const
```

```
void init(const arraydata_t *adp)
```

```
void freeall()
```

```
int update(const arraydata_t *adp)
```

update structure with new design specification

```
int needUpdate(const arraydata_t *adp) const
```

```
void init_root_stage(levelperm_t *&lperm_p, colperm_t *&colperm_p, const arraydata_t *adp)
```

```
void init_nonroot_stage(levelperm_t *&lperm_p, colperm_t *&colperm_p, colperm_t *&localcolperm_p, dyndata_t **&dynd_p, int &dynd_p_nelem, array_t *&colbuffer, const arraydata_t *adp) const
```

```
inline void init_rootrowperms(int &totalperms, rowperm_t *&rootrowperms, levelperm_t *&lperm_p)
```

Static initialization of root row permutations.

```
inline void init_rootrowperms_full(int &totalperms, rowperm_t *&rootrowperms, levelperm_t *&lperm_p)
```

Static initialization of root row permutations (full group)

Public Members

```
int LMC_non_root_init
```

```
int LMC_root_init
```

```
int LMC_reduce_root_rowperms_init
```

```
arraydata_t *ad
```

```

int LMC_root_rowperms_init

int nrootrowperms
    number of root row permutations

rowperm_t *rootrowperms
    pointer to row permutations that leave the root unchanged

int LMC_root_rowperms_init_full

int nrootrowperms_full
rowperm_t *rootrowperms_full

array_t *colbuffer

dyndata_t **dyndata_p
    buffer for a single column

colindex_t **colperm_p
    dynamic data; row permutations

colindex_t **localcolperm_p
    column permutations

array_transformation_t *current_trans
    local column permutation

struct LMCreduction_t
    #include <lmc.h> Class to describe an LMC reduction.

    The most important variable is the transformation itself, contained in transformation. The state contains information about how the reduction was performed.

Public Functions

LMCreduction_t(const LMCreduction_t &at)
    LMCreduction_t(const arraydata_t *arrayclass)
        copy constructor
    ~LMCreduction_t()
    LMCreduction_t &operator=(const LMCreduction_t &at)
    inline array_link getArray() const
        Assignment operator.

```

```
inline void setArray(const array_link al)
inline void setArray(const array_t *array, int nrows, int ncols)
inline void updateSDpointer(const array_link al, bool cache = false)
    update the pointer to the symmetry data based on the specified array
inline void releaseStatic()
    release internal LMCreduction_helper_t object
inline void initStatic()
    acquire a reference to a LMCreduction_helper_t object
inline LMCreduction_helper_t &getReferenceReductionHelperreset()
    reset the reduction: clears the symmetries and sets the transformation to zero
void show(int verbose = 2) const
std::string __repr__() const
void updateFromLoop(const arraydata_t &ad, const dyndata_t &dynd, levelperm_t *lperms, const array_t
    *original)
    called whenever we find a reduction
void updateTransformation(const arraydata_t &ad, const dyndata_t &dynd, levelperm_t *lperms, const
    array_t *original)
inline void updateLastCol(int col)
```

Public Members

array_t ***array**

array_transformation_t ***transformation**

pointer to transformation_t structure

OA_MODE **mode**

REDUCTION_STATE **state**

INIT_STATE **init_state**

int **maxdepth**

maximum depth for search tree

int **lastcol**

last column visited in algorithm

```
long nred  
    counter for number of reductions made  
  
int targetcol  
  
int mincol  
  
int nrows  
  
int ncols  
  
LMCreduction_helper_t *staticdata  
  
symmdataPointer sd
```

Private Functions

```
void free()
```

```
class rowsorter_t  
#include <lmc.h> Structure to sort rows of arrays.
```

Public Functions

```
rowsorter_t(int number_of_rows)  
~rowsorter_t()
```

Public Members

```
int number_of_rows  
  
rowsort_t *rowsort
```

Private Functions

```
void reset_rowsort()
```

```
struct dyndata_t  
#include <lmc.h> Contains dynamic data of an array.
```

The dynamic data are used in the inner loops of the LMC algorithm. In particular they keep track of the current row ordering and column permutation. By not applying these transformations to the array we can save calculation time.

We try to prevent copying the object, so it is re-used at different levels in the algorithm.

- N: static
 - col: changes at each column level
- rowsort: changes at each column level, used mainly in non-root stage
- colperm: changes at all levels

See also:

arraydata_t

Public Functions

```
dyndata_t(int N, int col = 0)
dyndata_t(const dyndata_t *dd)
dyndata_t(const dyndata_t&)
~dyndata_t()

dyndata_t &operator=(const dyndata_t&)

void show() const
void reset()

inline void setColperm(const colperm_t perm, int n)
inline void setColperm(const larray<colindex_t> &perm)
inline void setColperm(const std::vector<colindex_t> &perm)

void getRowperm(rowperm typelight &rp) const
    get lightweight row permutation
void getRowperm(rowperm_t &rperm) const
    get row permutation
rowperm typelight getRowperm() const
    return lightweight row permutation
colperm typelight getColperm() const
    return column permutation
void getColperm(colperm typelight &cp) const
    set column permutation

inline void allocate_rowsortl()
    allocate lightweight rowsort structure
inline void deleterowsortl()
inline void initrowsortl()
    initialize rowsortl from rowsrt
inline void rowsortl2rowsrt()
    copy rowsortl variable to rowsrt
void copydata(const dyndata_t &dd)
```

Public Members

colindex_t **col**

active column

rowindex_t **N**

number of rows

rowsort_t ***rowsort**

ordering of rows

rowsortlight_t ***rowsortl**

colperm_t **colperm**

current column permutation

Private Functions

void **initdata**(const *dyndata_t* &dd)

7.9 Interface for MD5 sums

Contains functions to calculate MD5 sums.

Functions

std::string **md5**(void *data, int number_of_bytes)

calculate md5 sum of a data block in memory

std::string **md5**(const std::string &filename)

calculate md5 sum of a file on disk

7.10 Interface for Pareto optimality

Class for calculation the *Pareto* optimal elements from a set of multi-valued objects.

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Defines

myprintf

```
template<class ValueType, class IndexType>  
struct pareto_element  
#include <pareto.h> helper class for the Pareto class to hold elements
```

Public Types

```
typedef std::vector<ValueType> pValue
```

Public Functions

```
inline bool dominates(pValue v)  
    return true if the argument element dominates this value  
inline bool isdominated(pValue v)  
    return true if the argument element is dominated by this value  
inline bool equal(pValue v)  
    return true if the argument element is equal to this element
```

Public Members

```
pValue value
```

```
std::vector<IndexType> indices
```

```
template<class ValueType, class IndexType>
```

class **Pareto**

```
#include <pareto.h> Class to calculate Pareto optimal elements.
```

The class is templated by the type of values to be compared and an index type. The index type is used to index the elements.

For elements added to the *Pareto* structure larger is better.

Public Types

`typedef std::vector<ValueType> pValue`

type for values of *Pareto* elements

`typedef pareto_element<ValueType, IndexType> pElement`

a pareto element consists of a pair (value, index)

Public Functions

`inline Pareto()`

Create an empty *Pareto* class.

`inline ~Pareto()`

`inline int number() const`

return the total number of *Pareto* optimal values

`inline int numberindices() const`

return the total number *Pareto* optimal objects

`inline std::string __repr__() const`

`inline void show(int verbose = 1)`

show the current set of *Pareto* optimal elements

`inline std::deque<IndexType> allindicesdeque() const`

return all indices of the *Pareto* optimal elements as a std::deque

`inline std::vector<IndexType> allindices() const`

return all indices of the *Pareto* optimal elements

`inline std::vector<pValue> allvalues() const`

return the values of all *Pareto* optimal elements

`inline bool addvalue(const pValue value, const IndexType idx)`

add a new element

Public Members

`int verbose`

Verbosity level.

`std::deque<pareto_element<ValueType, IndexType>> elements`

contains a list of all *Pareto* optimal elements

Public Static Functions

```
static inline void showvalue(const pValue p)  
    show a Pareto element
```

**CHAPTER
EIGHT**

REFERENCES

**CHAPTER
NINE**

INDICES AND TABLES

- genindex
- modindex
- search

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For more information contact (pieter.eendebak@gmail.com or eric.schoen@tno.nl).

This package also uses code from other works:

- Eigen (see <http://eigen.tuxfamily.org/>, MPL2 license)
- InfInt (by Sercan Tutar, MPL2 license)
- bitarray (by Isaac Turner, MIT license)
- md5.cpp (by RSA Data Security)
- msstdint.h (by Alexander Chemeris, see <https://code.google.com/p/msinttypes/>)
- oapackage._scanf (from <https://github.com/joshburnett/scanf>, MIT license)

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